

Greenland ice sheet flow computations

scaling-up to high spatial resolution and fast boundary processes

Ed Bueler

Dept. of Mathematics and Statistics
Geophysical Institute
University of Alaska, Fairbanks

with help from

Andy Aschwanden, ARSC, Fairbanks
Jed Brown, VAW ETH, Zürich
Constantine Khroulev, GI, Fairbanks
Gudfinna Aðalgeirsdóttir, DMI, Copenhagen



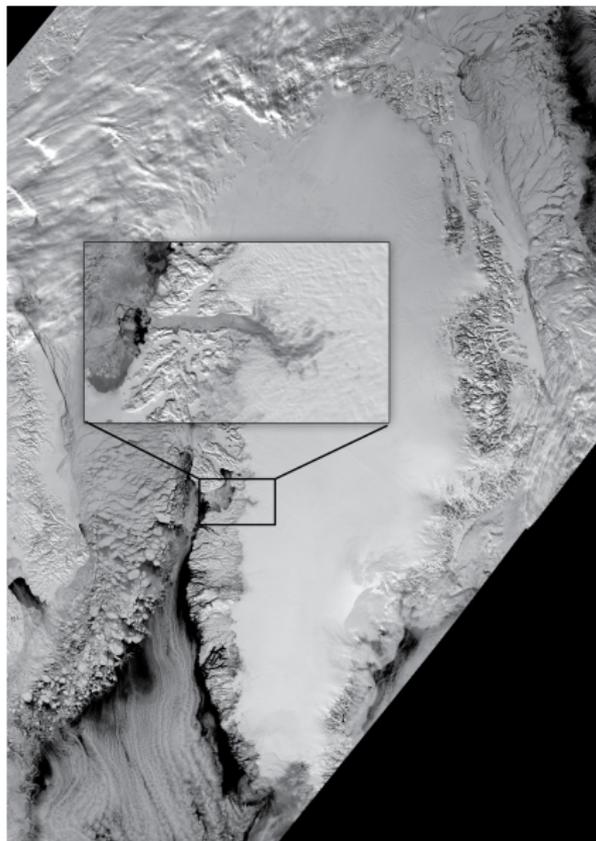
Outline

why compute Greenland's flow?

ice sheets: modeling and observations

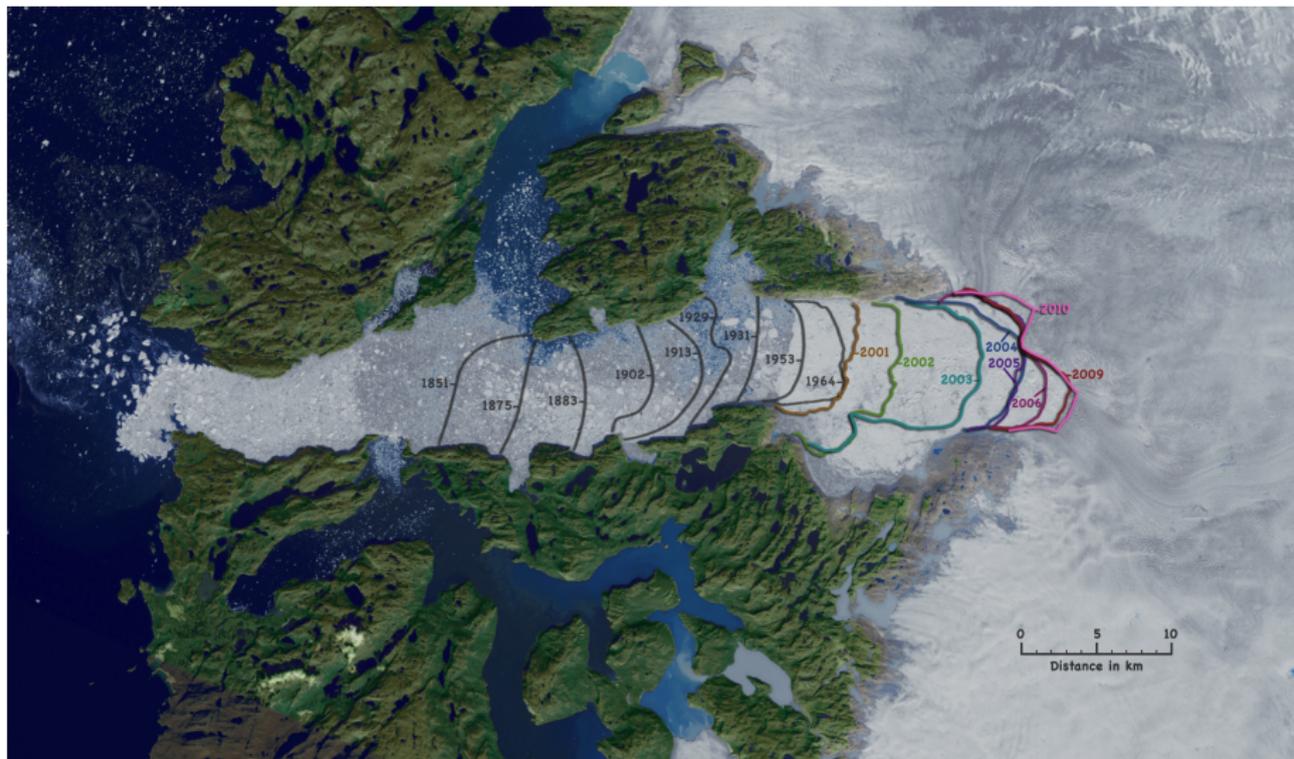
scaling-up: how to get more ISM from HPC

Jakobshavn Isbræ, west Greenland



*MODIS image
M. Fahnestock*

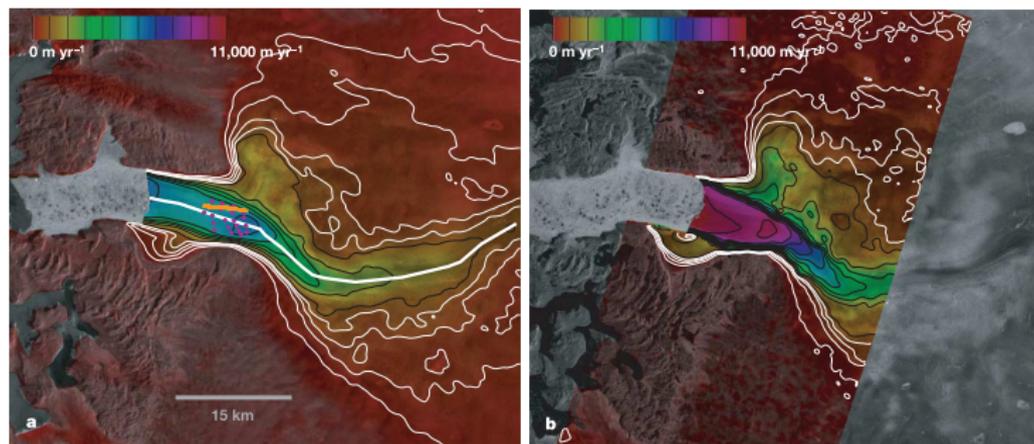
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NASA/Goddard Space Flight Center Scientific Visualization Studio

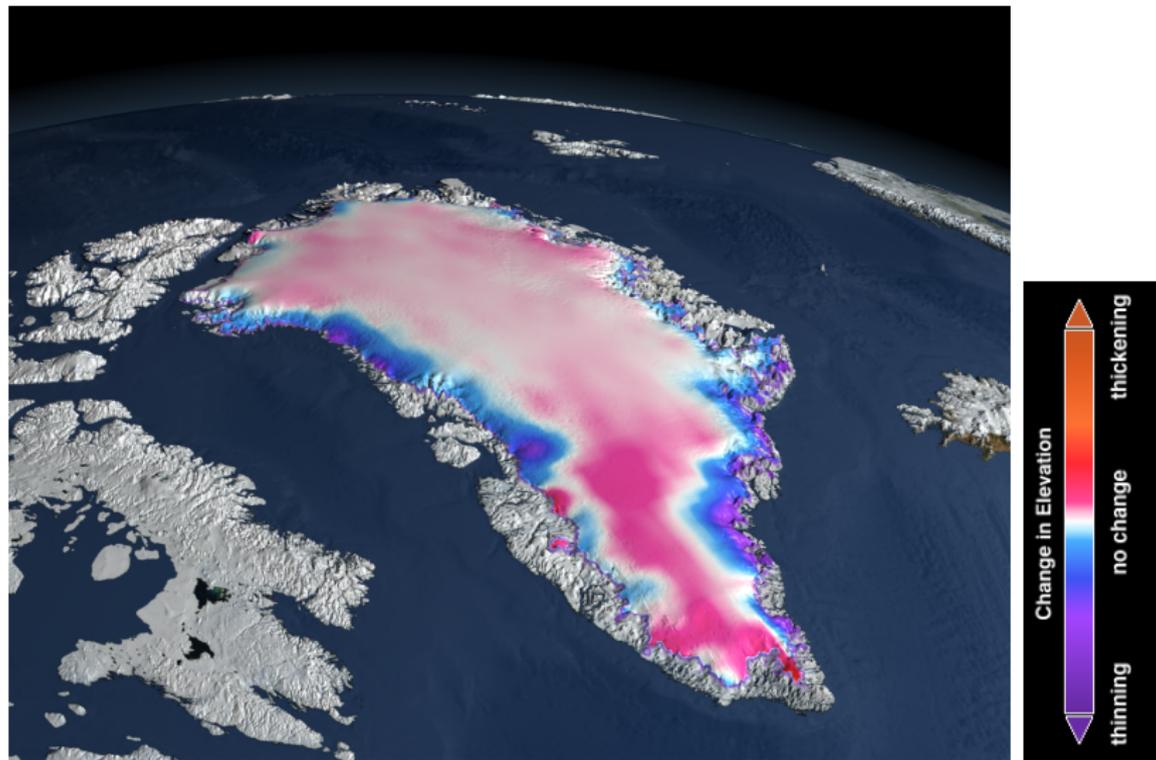
Speed-up of Jakobshavn Isbræ

- ▶ almost doubled its flow speed between the 1992 and 2000:
 - ▷ probably started by increase in ocean temperature from 1.7 C° in 1995 to 3.3 C° in 1998
 - ▷ ... thus increased melting under floating tongue
 - ▷ loss of floating tongue and its “backpressure” on upstream grounded ice
 - ▷ speed-up of grounded ice
- ▶ now drains about 7% of the entire ice sheet



Joughin et al. (2004)

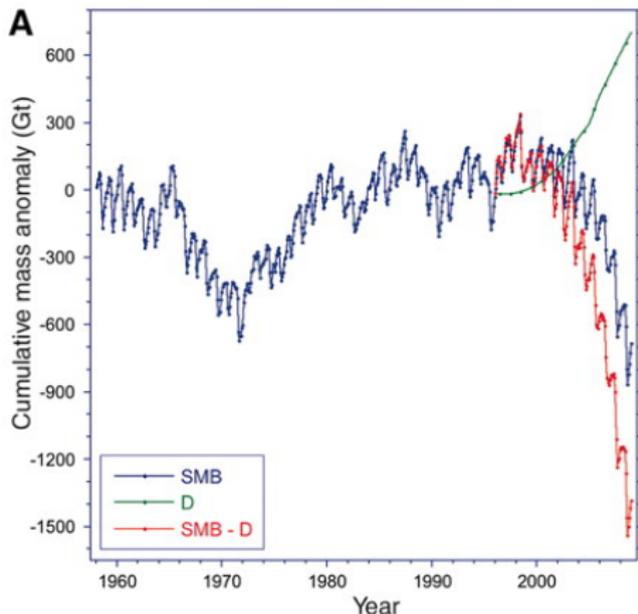
Elevation changes: surface melt and “discharge”



IceSAT observations over 2003–2006 period; NASA/Goddard Space Flight Center Scientific Visualization Studio

The future of Greenland is the question

- ▶ before mid-90s mass loss was dominated by surface mass balance (= precipitation minus surface melt/runoff)
- ▶ since 2000, mass balance has been persistently negative
 - ▷ decrease in surface mass balance (**more melting beats more precipitation**)
 - ▷ increase in discharge (**calving**) from ice flow
- ▶ future mass loss partitioning: **unknown**
- ▶ models need to predict which climate changes have which effects



van den Broeke et al. (2009)

Why Greenland?

- ▶ its changes affect future sea level rise
 - ▷ 7 m rise if completely melted ... unlikely ... is 1 or 2 m likely?
- ▶ observations over the past decades show:
 - ▷ rapid acceleration of outlet glaciers
 - ▷ thinning around the margin
 - ▷ increased mass loss
- ▶ it's a testbed for ice sheet modeling:
 - ▷ recent observational attention: lots of flights, ground measurements
 - ▷ exhibits the kind of worrying dynamics we want to "explain"
 - ▷ Antarctic ice sheet has $10\times$ the area thus $10\times$ the cost

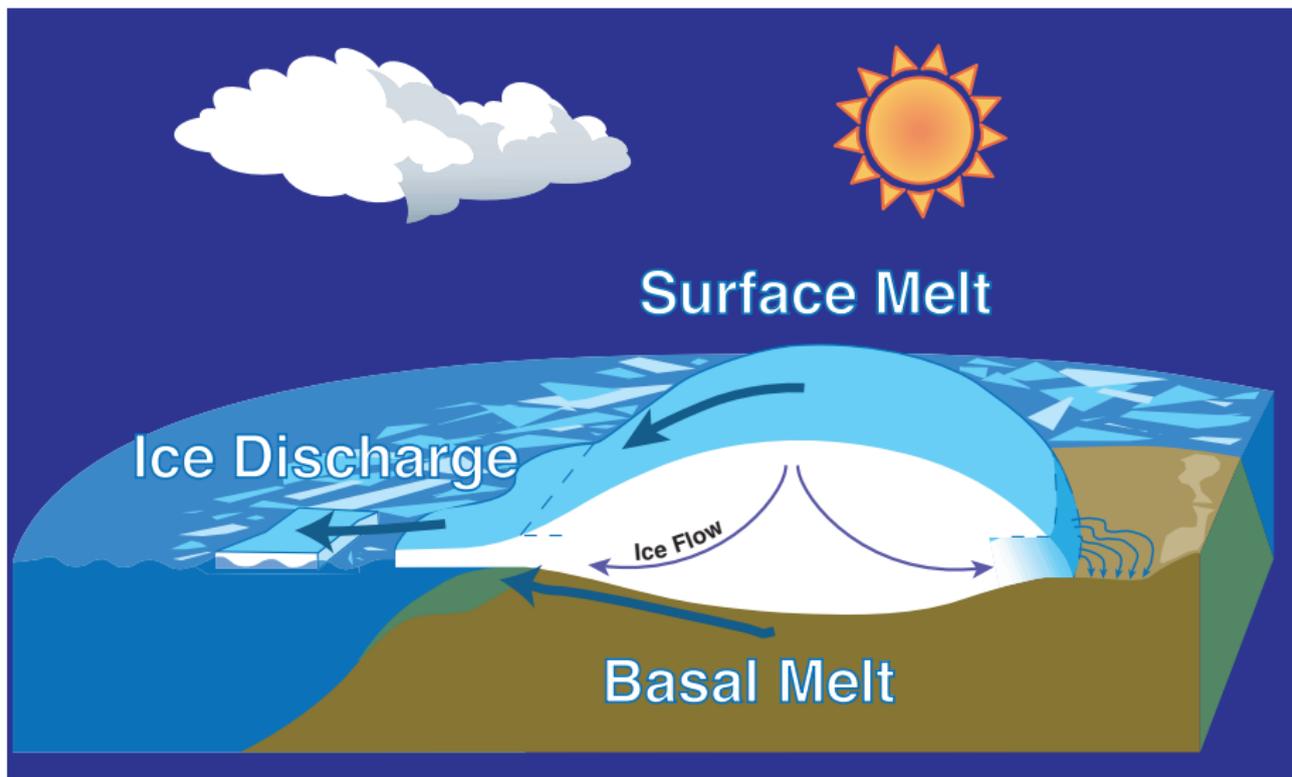
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How does an ice sheet lose mass?



modified from ICESat brochure

IPCC and ice sheet models

IPCC (2007), Box 4.1: Ice Sheet Dynamics and Stability

“...but recent changes in ice sheet margins and ice streams cannot be simulated accurately with these models, ...”

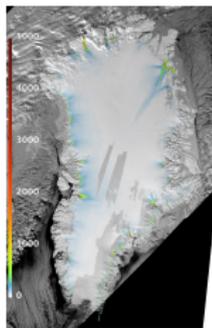
- ▶ IPCC = Intergovernmental Panel on Climate Change
= {2007 Nobel Peace Prize winners} \ {Al Gore}
- ▶ above statement \implies lots of attention from modelers

progress report 2011:

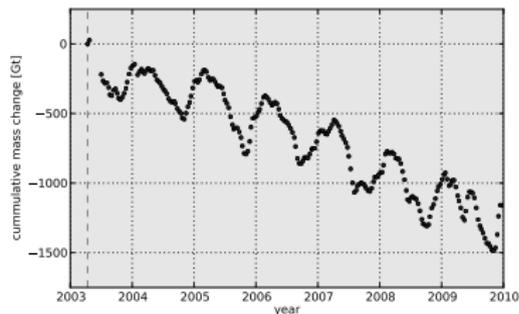
- ▶ PISM is doing a decent job reproducing the past two decades
 - ▷ before anything else, get the present, observed period right!
 - ▷ [model validation](#)

Ice sheet model validation using

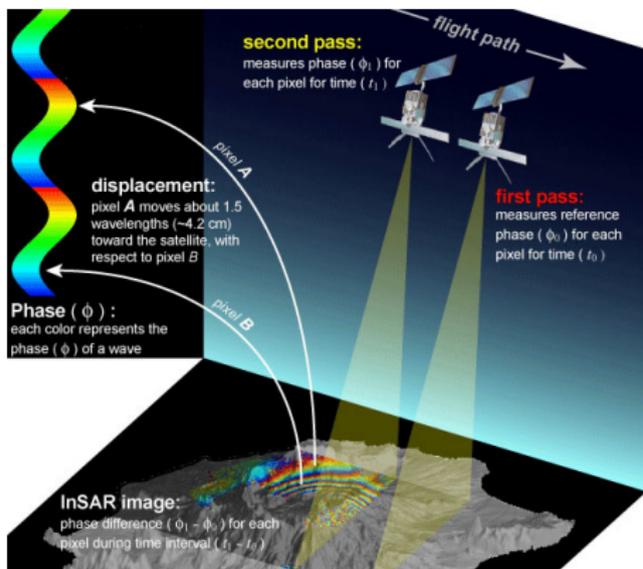
- ▶ observed mean flow speed from 2000, 2006–2008 (InSAR)



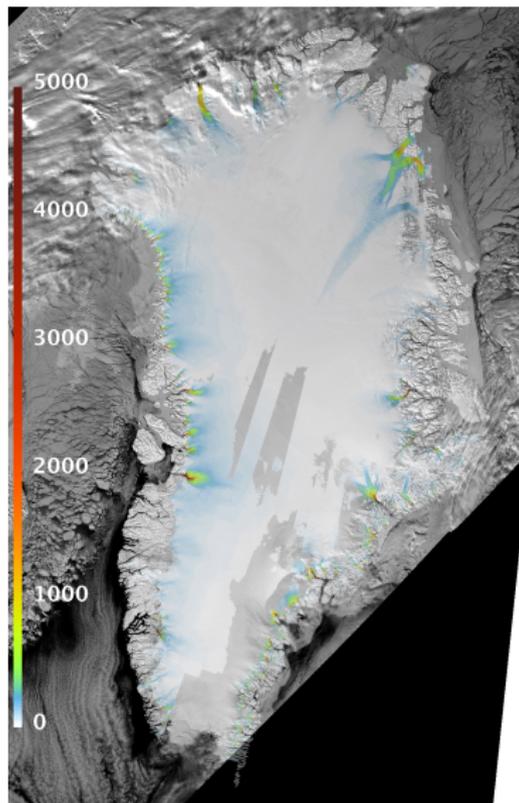
- ▶ observed cumulative mass change from 2003–2009 (GRACE)



Flow speed from InSAR

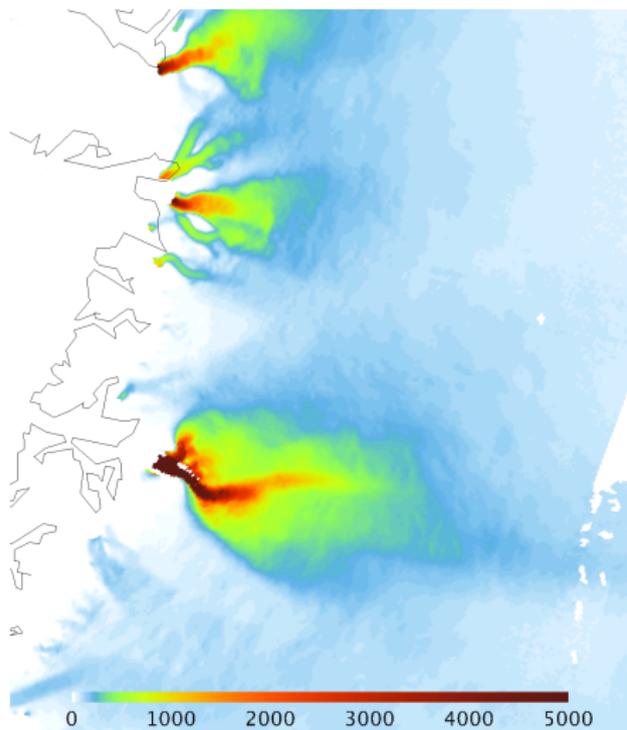


credit: USGS

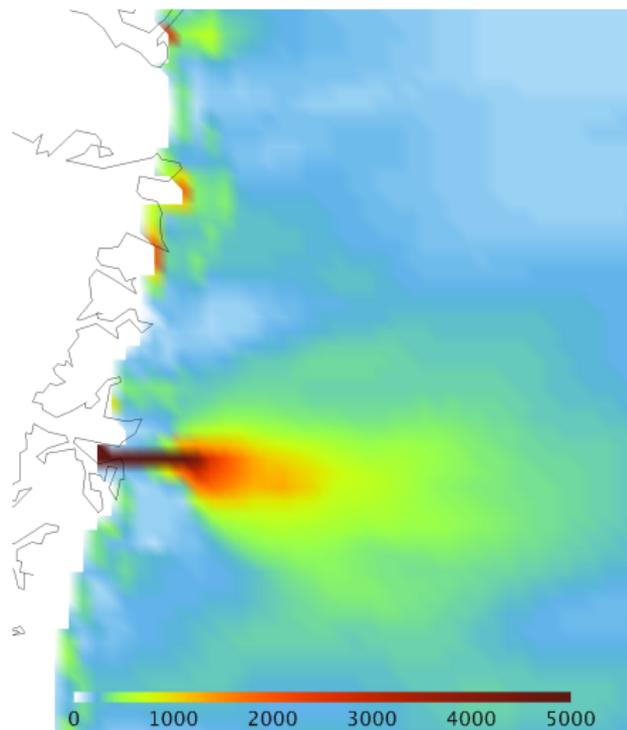


credit: I. Joughin

Results: Jakobshavn Isbræ

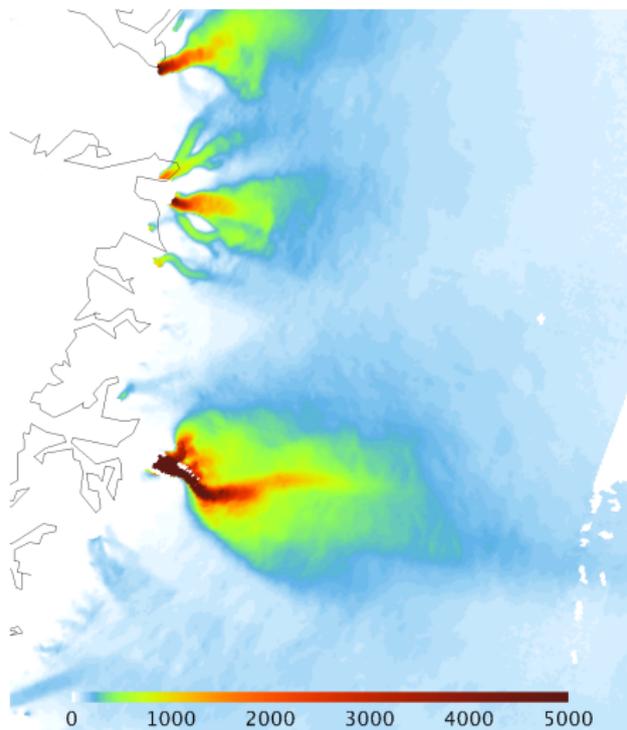


InSAR (*Joughin et al., 2010*)

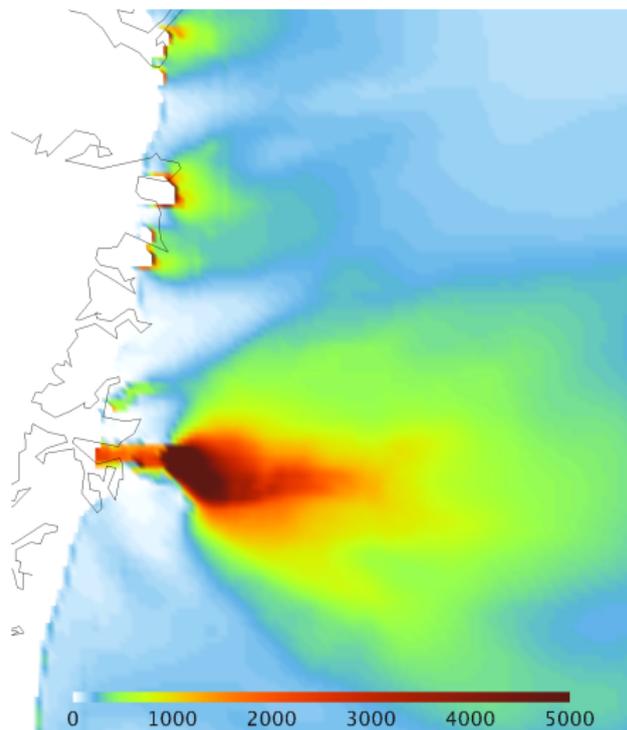


PISM: 5 km grid resolution

Results: Jakobshavn Isbræ

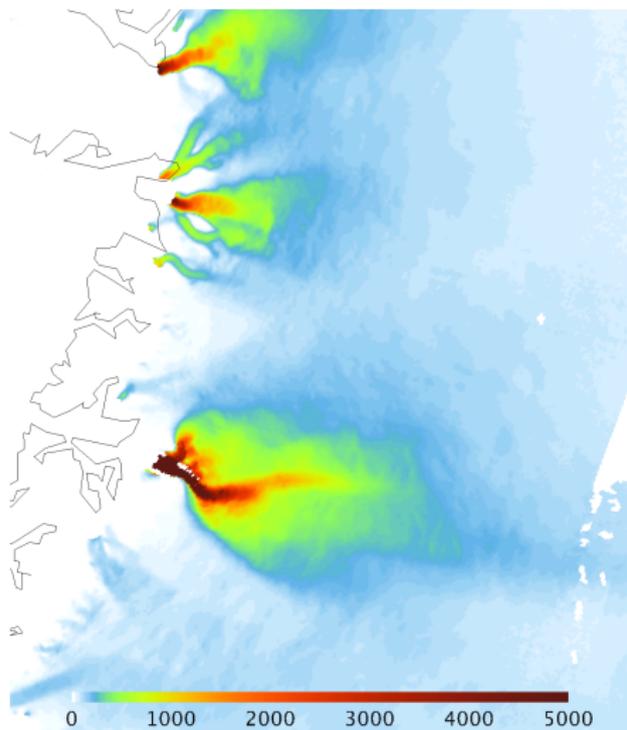


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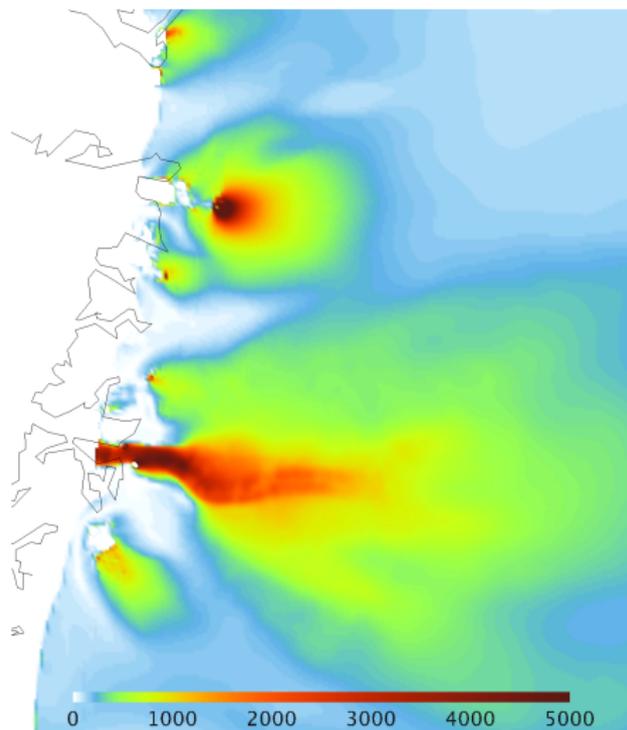


PISM: 2 km grid resolution

Results: Jakobshavn Isbræ

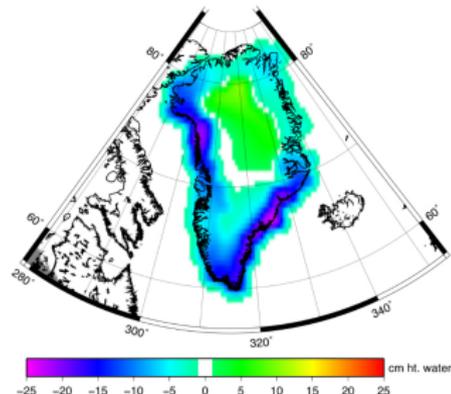
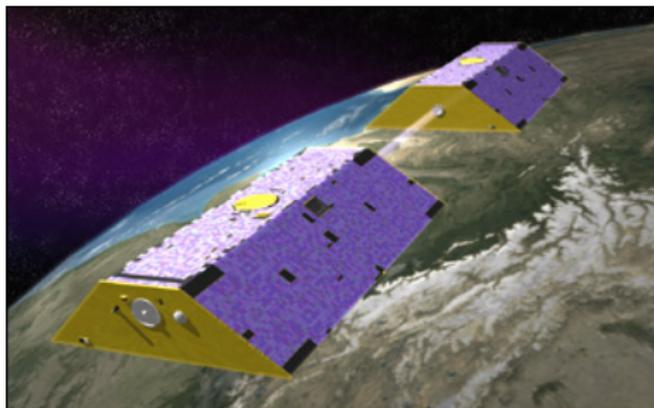


InSAR (*Joughin et al., 2010*)



PISM: 1 km grid resolution

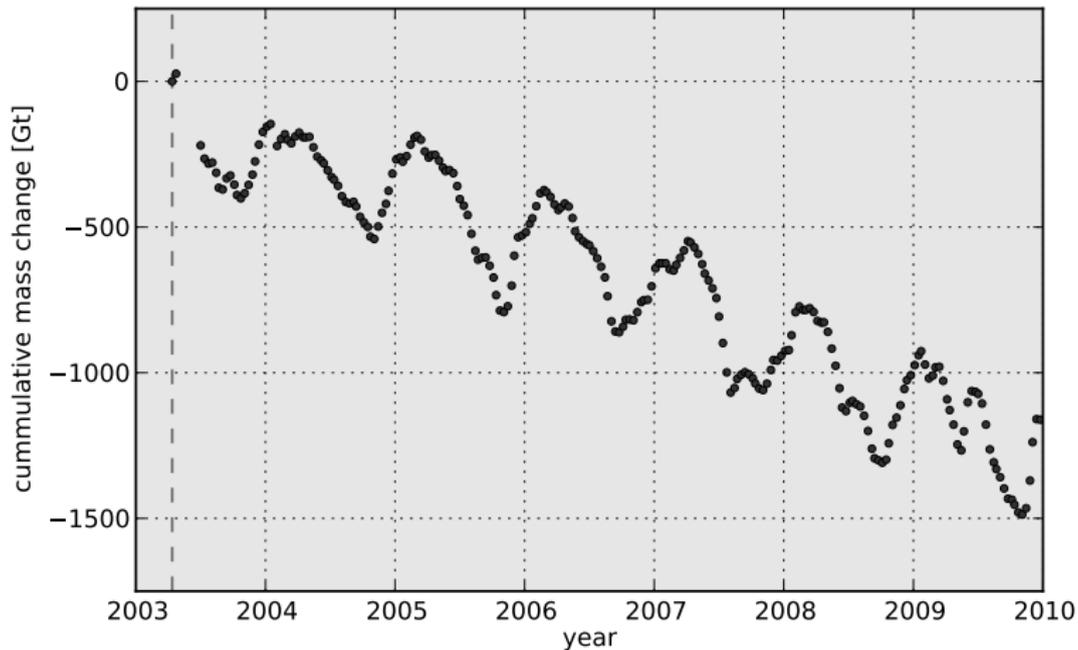
Gravity Recovery and Climate Experiment (GRACE)



thanks to A. Arendt

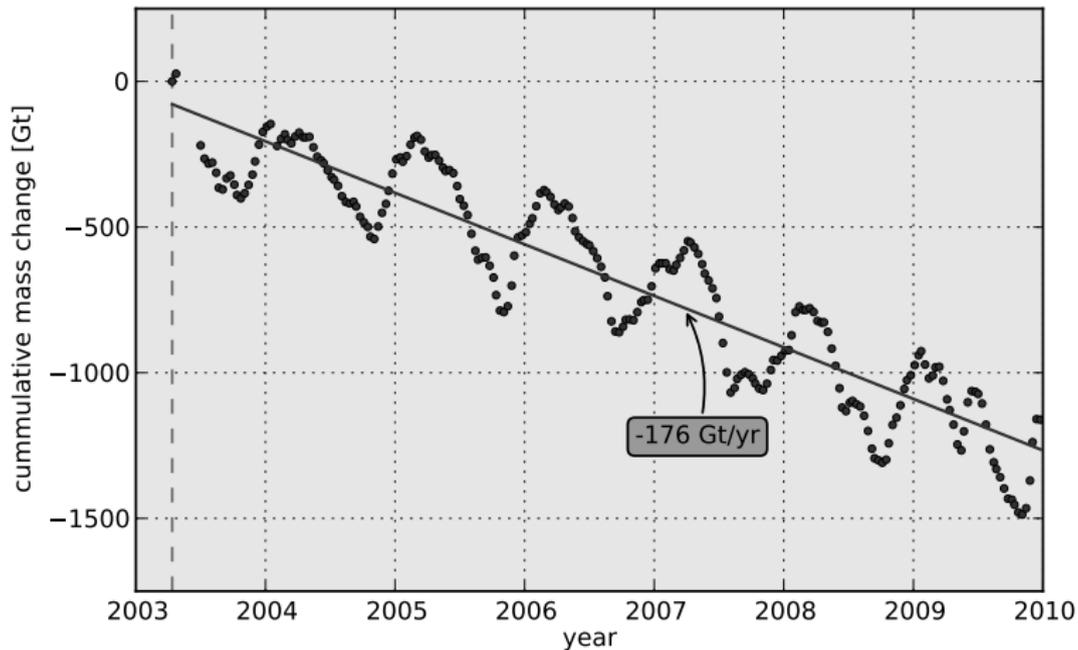
- ▶ precisely measures distance between pair of satellites
- ▶ estimates deviation of gravity field from uniform sphere shape

Observed mass changes



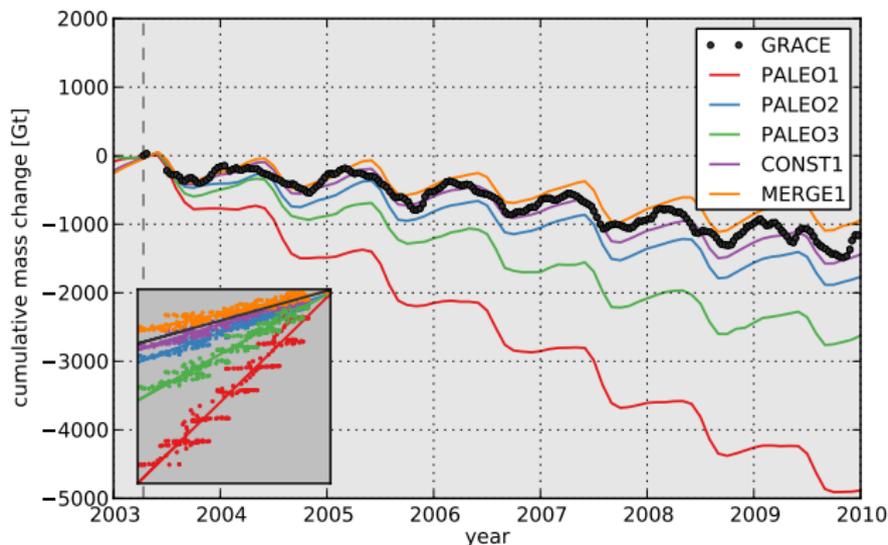
Luthcke, et al. (unpublished; new high-resolution solutions)

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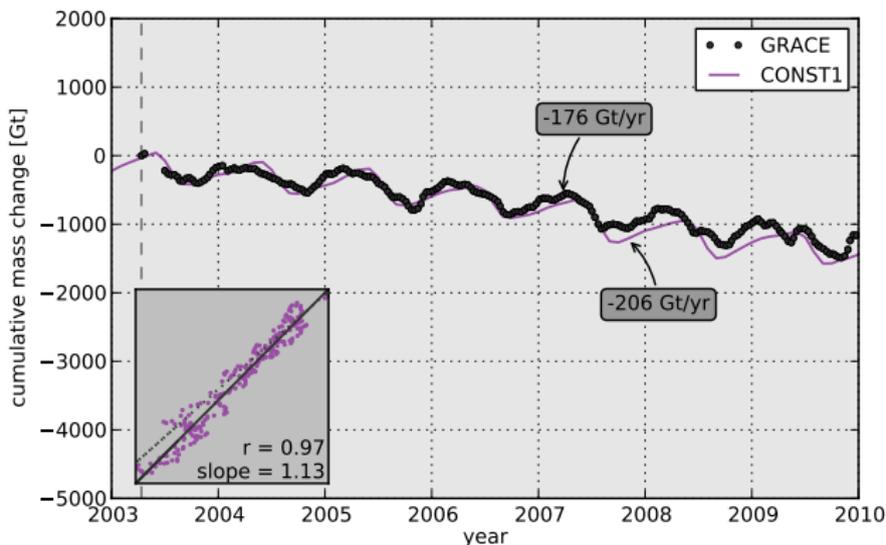
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Modeled and observed mass changes



- ▶ new coupled models of Greenland
 - ▷ PISM + regional climate model (HIRHAM at DMI Copenhagen)

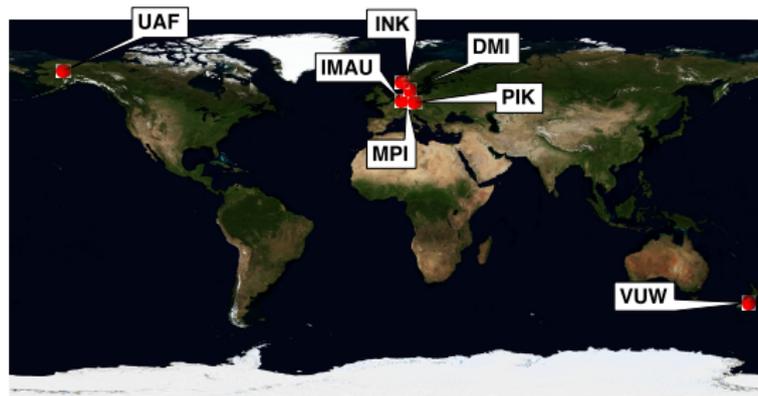
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What is PISM?

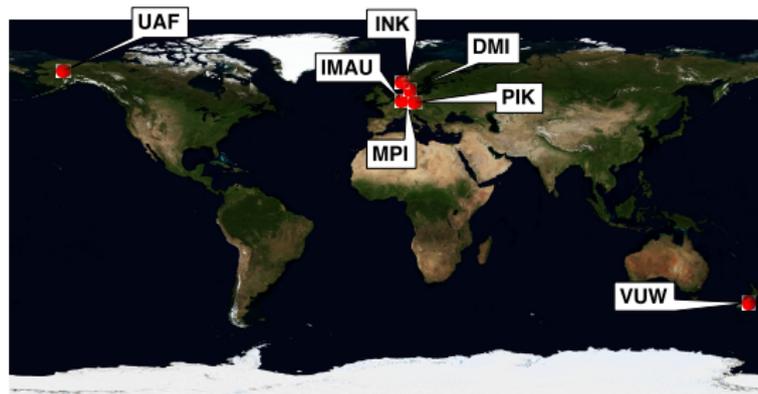
- ▶ PISM = Parallel Ice Sheet Model www.pism-docs.org
- ▶ open source (C++, python), PETSc-over-MPI, regular grid
- ▶ adaptive time-stepping
- ▶ supported by NASA; now a joint project with PIK in Germany
- ▶ the best ice sheet model in the world
- ▶ ... was developed in Fairbanks



user base:

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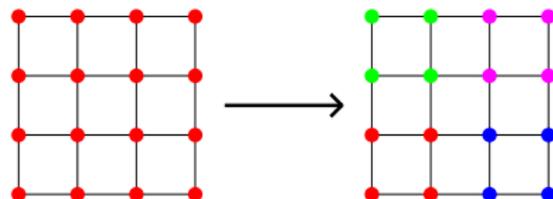
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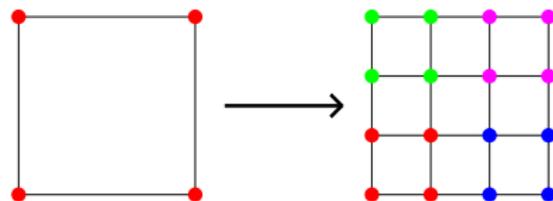
scaling-up: how to get more ISM from HPC

Scaling

- ▶ plan for the rest of my talk: beat up PISM because it scales badly
- ▶ ... though it scales way better than any other current ISM
- ▶ definitions in convenient 2D grid case:
 - ▷ **strong scaling**: for fixed problem,
 $4\times$ the number of processors \implies (1/4)th the execution time



- ▷ **weak scaling**: for fixed number of d.o.f.s *per processor*,
 $4\times$ the number of processors \implies *same* execution time



Min prerequisite for weak scaling: convergence

- ▶ six runs, each 100 model year with same data
- ▶ on refining grids: 40, 20, 10, 5, 2.5 km
- ▶ surface velocity (m/year) →
- ▶ my first informal study

- ▶ results:

res	procs	wall clock
40 km	1	8 sec
20 km	1	75 sec
10 km	64	57 sec
5 km	64	14 min
3 km	128	56 min
2 km	128	285 min

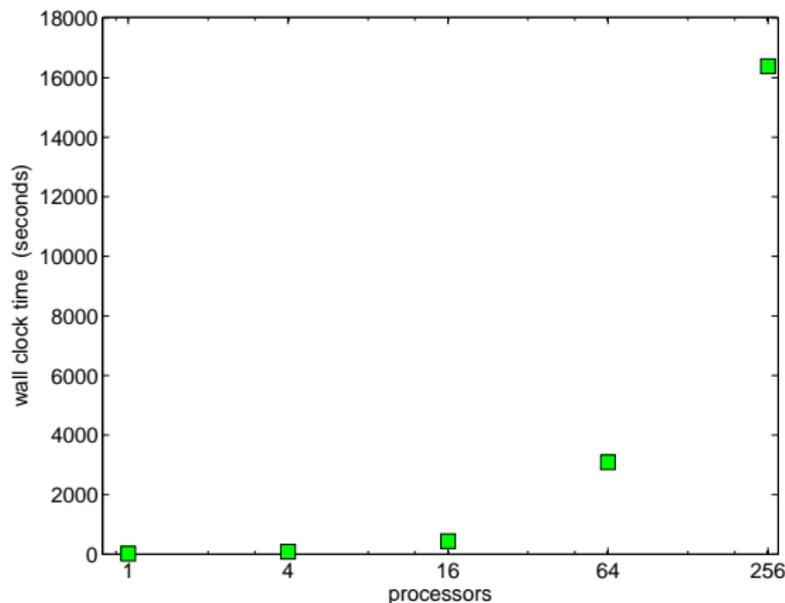
- ▶ on Cray XT5
 - ▷ `pingo.arsc.edu`

Weak scaling: the reality

- ▶ here's the problem →

- ▷ 100 model year runs
- ▷ increase d.o.f.s and processors in proportion
 - ▶ a la weak scaling
- ▷ it is **not** giving constant-time for whole run
- ▷ it is giving constant-time per model time step
 - ▶ but who cares

- ▶ we observe: short time steps on fine grids blocks weak scaling

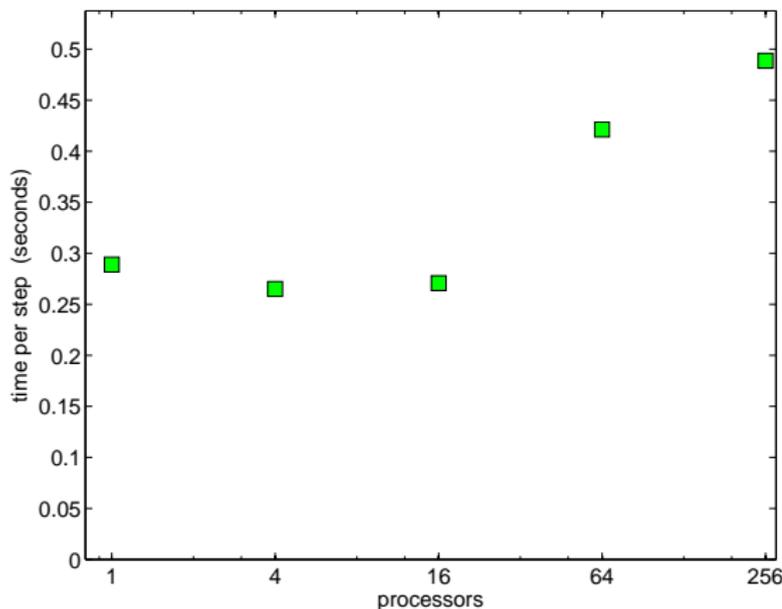


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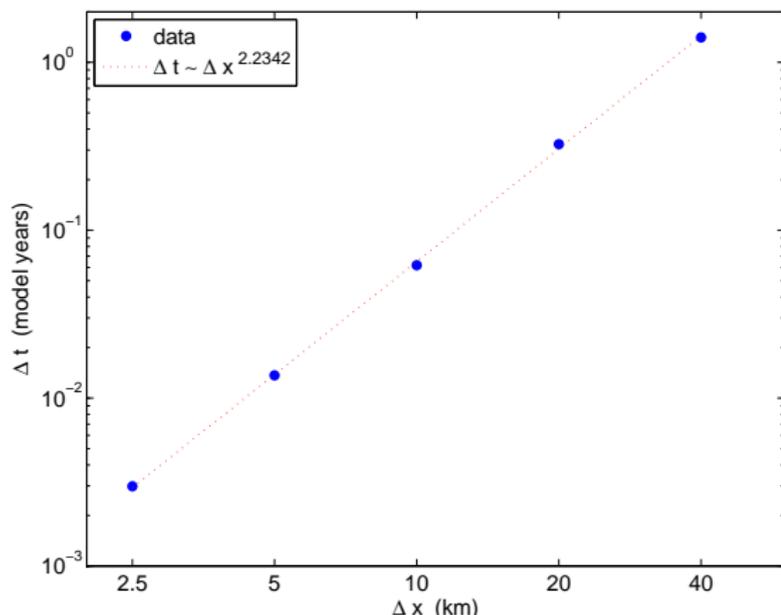
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Weak scaling: the troubles

1 PISM evolves temperature and geometry by **explicit** time-stepping

- ▷ major evolution equation is wildly-nonlinear diffusion
- ▷ ice thickness H changes by

$$\frac{\partial H}{\partial t} \stackrel{*}{=} \nabla \cdot (CH^5 |\nabla H|^2 \nabla H)$$

- ▷ explicit method scales badly because

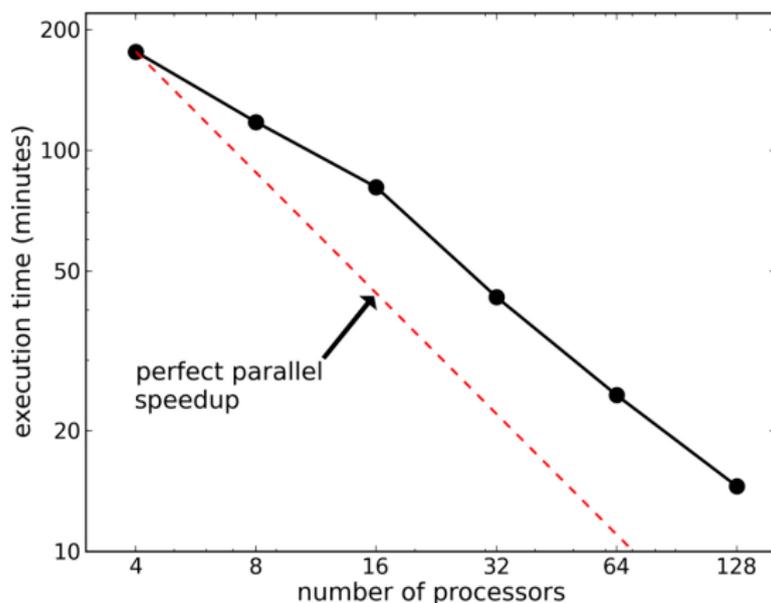
$$\Delta t \sim \Delta x^2$$

- ▷ *implicit time steps, you idiot!*
- ▷ but we are not solving PDEs; boundary value problem is * subject to inequality

$$H \geq 0$$

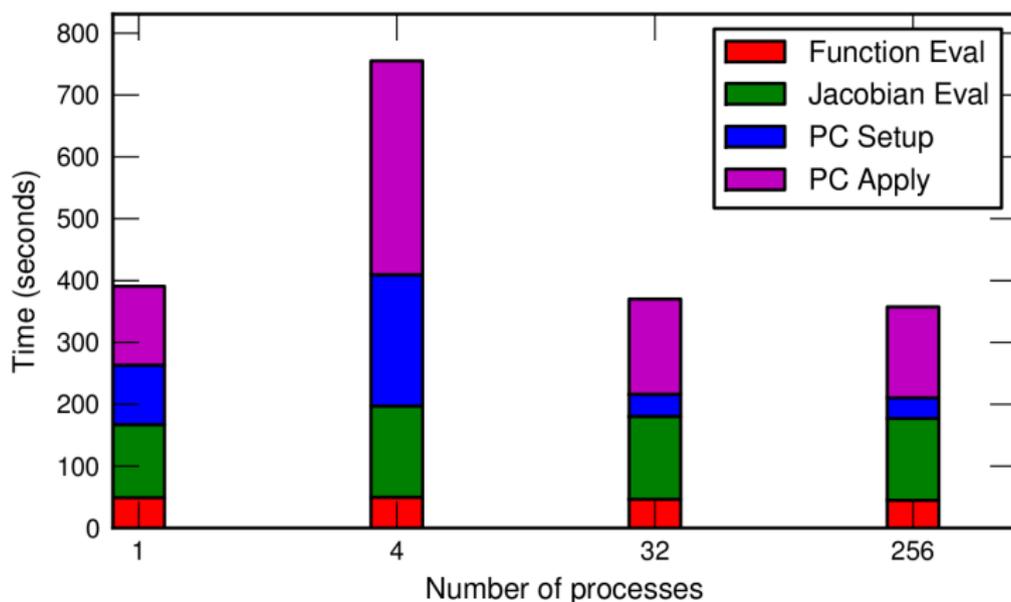
- ▷ so we don't really know how to solve well-posed implicit time steps

Scaling: results so far; idealized ice sheets



- ▶ PISM: strong scaling on time-dependent run including many 2D stress solutions
- ▶ Jed Brown's hydrostatic ice solver [*submitted 2011*]: awesome weak scaling on time-independent 3D stress solver; *not yet in PISM!*

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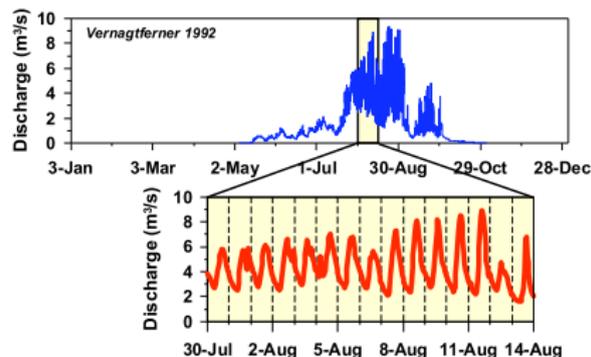
Weak scaling: the troubles

2 liquid water at boundaries

- ▷ big lakes form and drain ... in 90 minutes (upper)
- ▷ hydrograph shows brief summer period of surface melt (lower)
- ▷ ice flow model must “see” liquid runoff at surface *and* its effect on subglacial resistance
 - ▶ boundary liquid timescales are minutes–weeks
 - ▶ ice sheet model runs are decades–millenia



S. Das

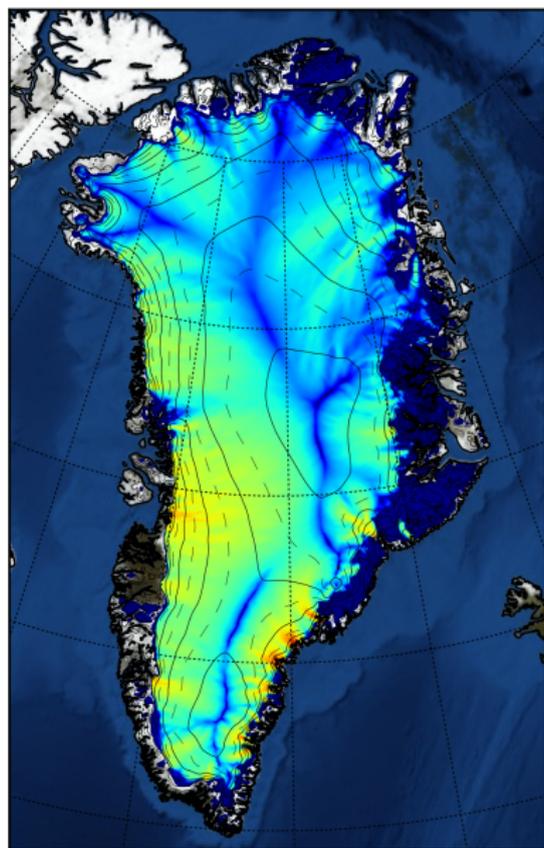


R. Hock et al. (2005)

Weak scaling: the troubles

3 solve PDEs on domain with fractal boundary

- ▷ velocity is big near the boundary
- ▷ boundary is a **coastline** ... Mandelbrot warned us about those things
- ▷ at each timestep, want to solve nonlinear elliptic problems on this fractal



Summary

- ▶ model Greenland ice sheet flow! it is on the move!
- ▶ PISM is getting good fit to observed flow speeds, mass changes
- ▶ challenges to scaling:
 - ▶ equations need new thinking
 - need well-posed implicit time steps
 - and better solvers too
 - ▶ short time-scale processes on all ice sheet surfaces
 - liquid water
 - ▶ fast ice dynamics along fractal boundaries
- ▶ much bigger Antarctic ice sheet in the background
- ▶ thanks for your attention!