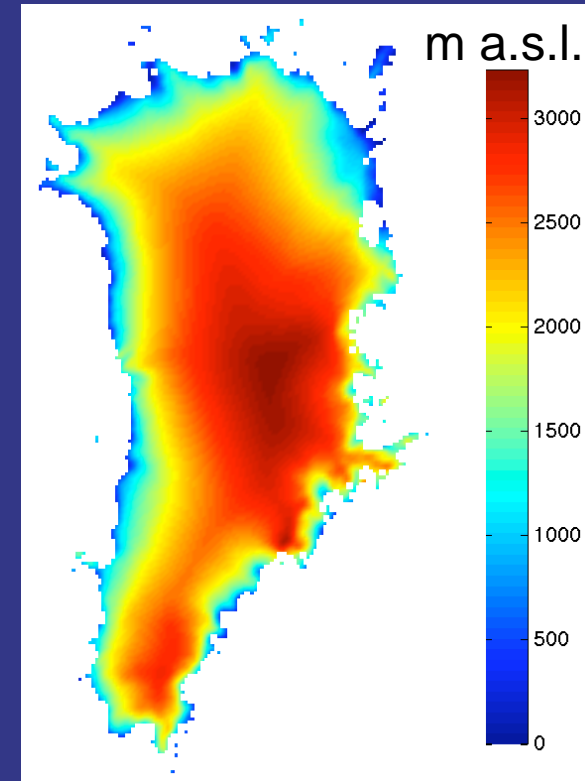


Improving degree-day melt modeling of the Greenland ice sheet in the Parallel Ice Sheet Model (PISM)



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Andy Aschwanden²,
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Dani Dellagiu¹
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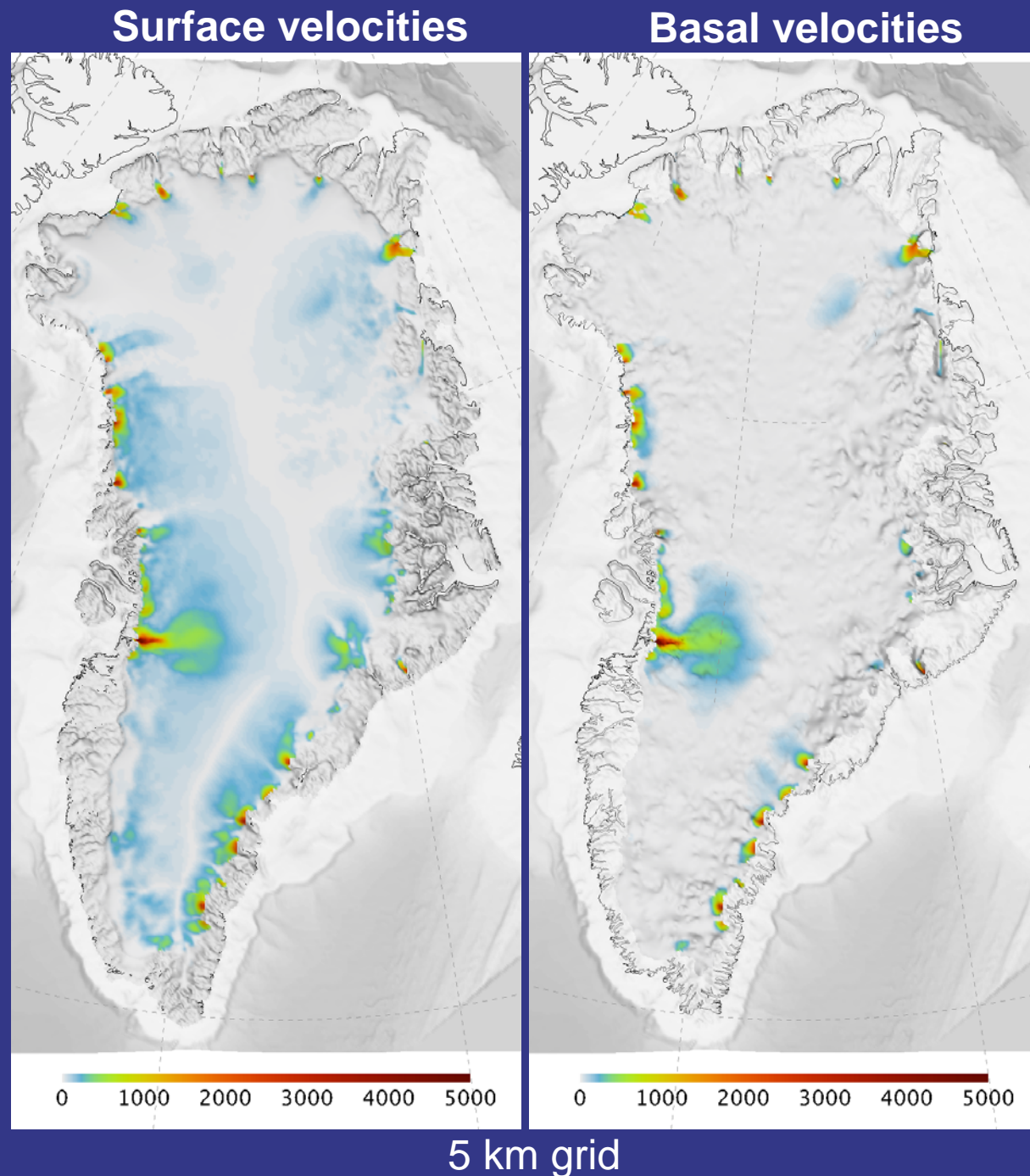
³*Institute for Marine and Atmospheric Research, Utrecht University, The Netherlands*

■ Background: PISM

- **Parallel Ice Sheet Model** is an open source, fully-parallel, high-resolution ice sheet model
- one of the models used in *SeaRISE* assessment (*Sea-level Response to Ice Sheet Evolution*) to project the ice sheet contributions to sea level in the next 100-200 years

Features:

- a hierarchy of available stress balances, including shallow ice and shelf approximations, a hybrid of these, and a (planned) higher-order scheme
- a polythermal, enthalpy-based conservation of energy scheme
- complete documentation for users and developers
- www.pism-docs.org



■ PISM: Surface mass balance

Classical degree-day approach

The diagram shows the equation $\dot{M} = f_{snow/ice} \sum_{1}^n (T - T_0)$ inside a yellow-to-white gradient box. Three orange arrows point from text labels to parts of the equation: 'Melt rate' points to \dot{M} , 'Degree-day factor' points to $f_{snow/ice}$, and 'degree-day sum' points to the summation term $\sum_{1}^n (T - T_0)$.

$$\dot{M} = f_{snow/ice} \sum_{1}^n (T - T_0)$$

Melt rate

Degree-day factor

degree-day sum

T = air temperature

T_0 = threshold temperature below which there is no melt;
in PISM: $T_0 = 0^{\circ}\text{C}$

Typical values for snow = 3-5 mm/d/K, ice = 6-10 mm/d/K

- **degree-day sum** is computed from positive temperatures multiplied by the duration (in days) when it is $> 0^{\circ}\text{C}$
- **degree-day factors** according to Greve (2005), *Ann. Glac.*,
--> function of latitude and mean July temperature

• Greve, R. (2005). Relation of measured basal temperatures and the spatial distribution of the geothermal heat flux for the Greenland ice sheet. *Ann. Glaciol.*, 42, 424-432.

■ Objectives

to improve the melt model in PISM:

- **How good is the degree-day melt model that is currently implemented in PISM ?**
- **How do degree-day factors vary spatially and what do they depend on ?**
- **How can degree-day factors be parameterized in a better way that can be implemented into PISM ?**



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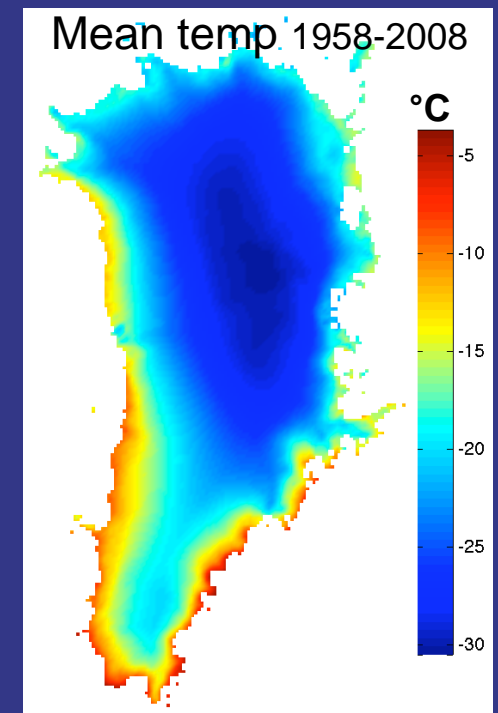
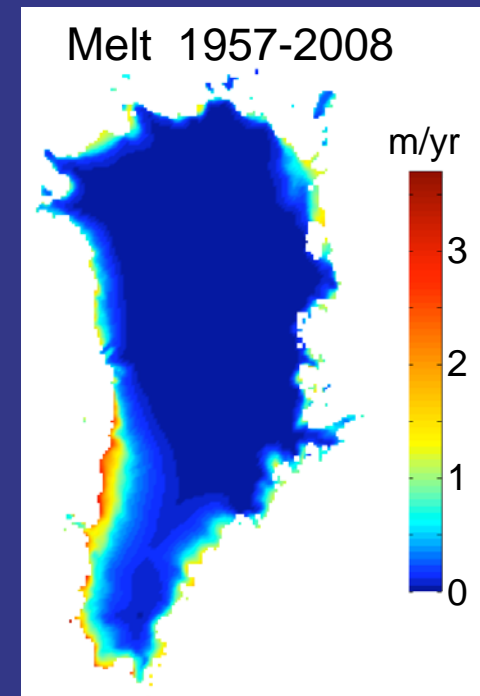
■ Data

Model

- RACMO2/GR Regional Climate Model
- lateral atmospheric forcings: ERA40 and ECMWF operational analysis
- resolution 11 km
- September 1957 - December 2008 (51.3 years)

Data

- Monthly melt
- Daily mean 2 m air temperatures from which positive monthly degree-day sums are computed
- Monthly near-surface glacier density (to distinguish between snow and ice)



■ How good is the degree-day melt model in PISM ?

- $DDF_{\text{snow}} = 3 \text{ mm/d/K}$ for entire Greenland ice sheet
- DDF_{ice} :
 - South of 72°N : 7 mm/d/K
 - North of 72°N : function of mean July temperature

$$\beta_{\text{ice}} = \begin{cases} \beta_{\text{ice}}^w & T_{\text{mj}} \geq T_w, \\ \beta_{\text{ice}}^w + \frac{\beta_{\text{ice}}^c - \beta_{\text{ice}}^w}{(T_w - T_c)^3} (T_w - T_{\text{mj}})^3 & T_c \leq T_{\text{mj}} \leq T_w, \\ \beta_{\text{ice}}^c & T_{\text{mj}} \leq T_c, \end{cases}$$

Degree-day factors after
Greve (2005)

based on Tarasov and Peltier, 1999

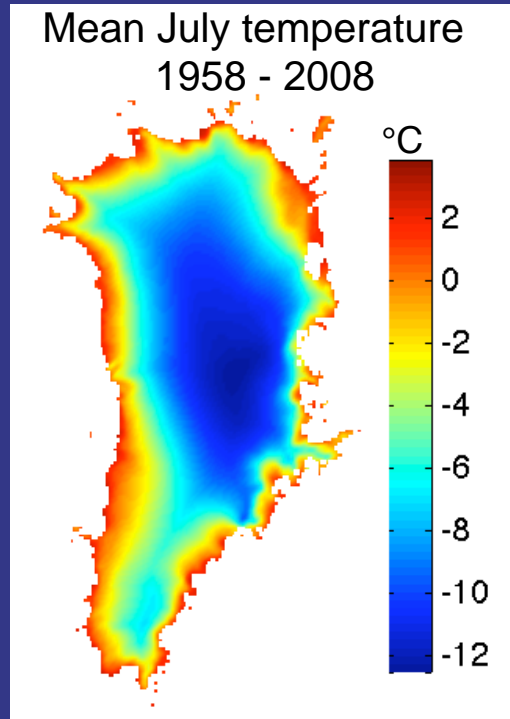
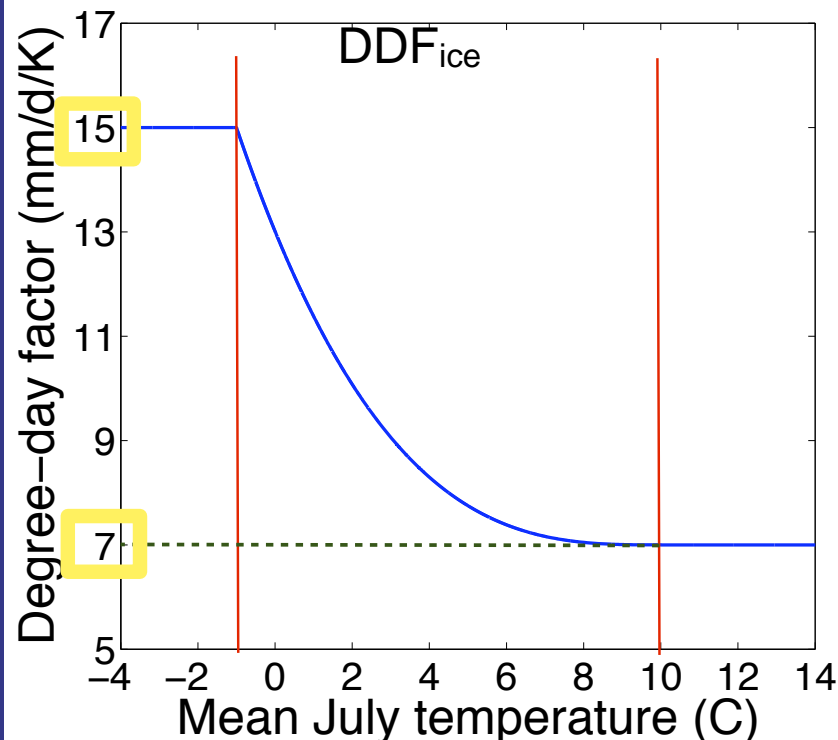
■ How good is the degree-day melt model in PISM ?

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Degree-day factors after
Greve (2005)

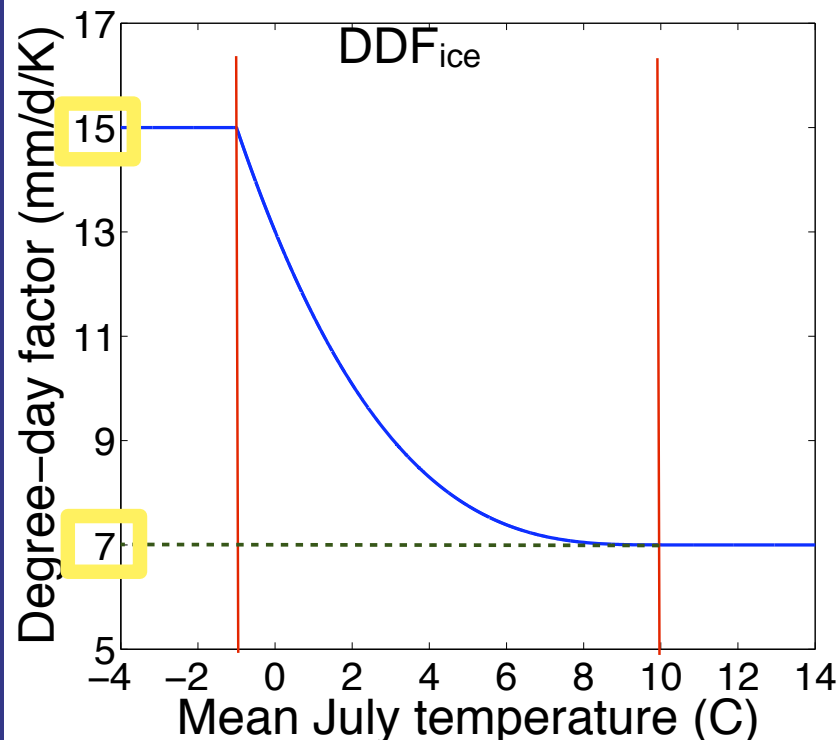
based on Tarasov and Peltier, 1999



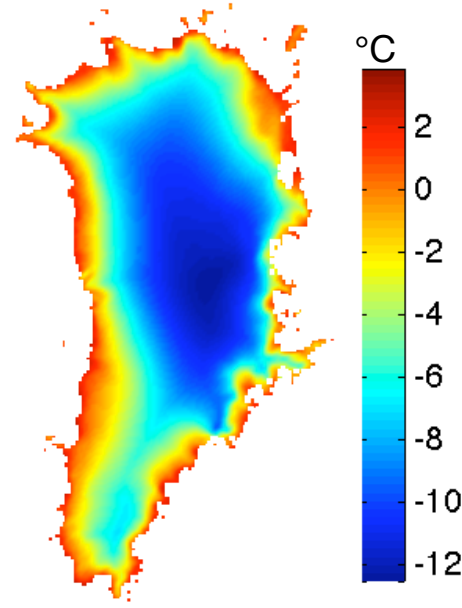
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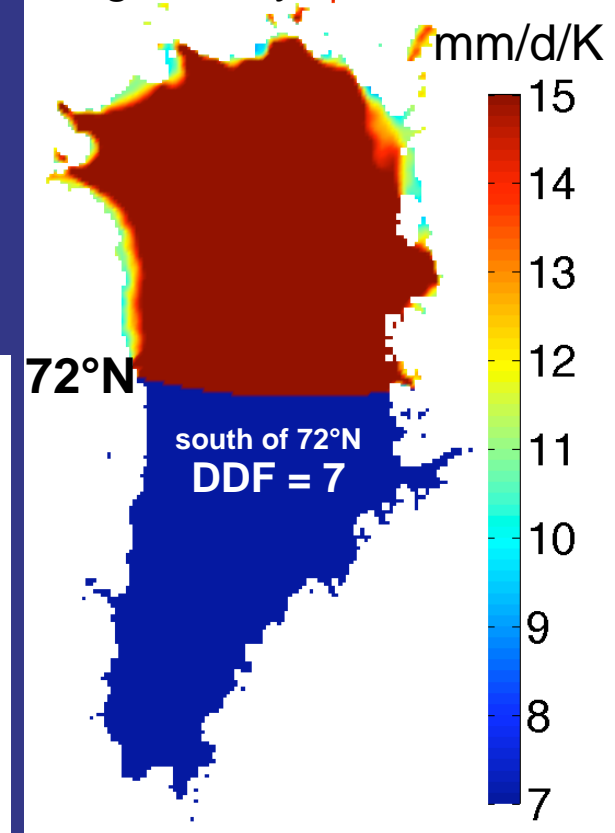
Mean July temperature
1958 - 2008



Degree-day factors after Greve (2005)

based on Tarasov and Peltier, 1999

Degree-day factor ice



■ PISM: Melt after Greve (2005)

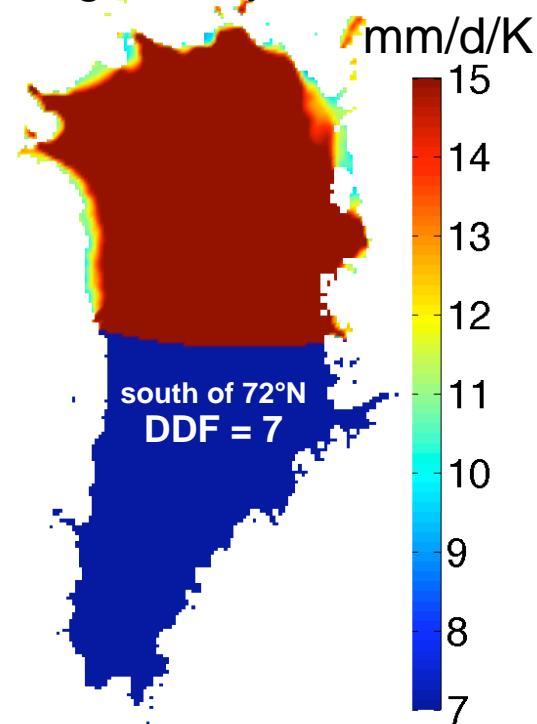
$f_{\text{snow}} = 3 \text{ mm/d/K}$
over entire
Greenland

$$\dot{M} = f_{\text{snow/ice}} \sum_{1}^n (T - T_0)$$

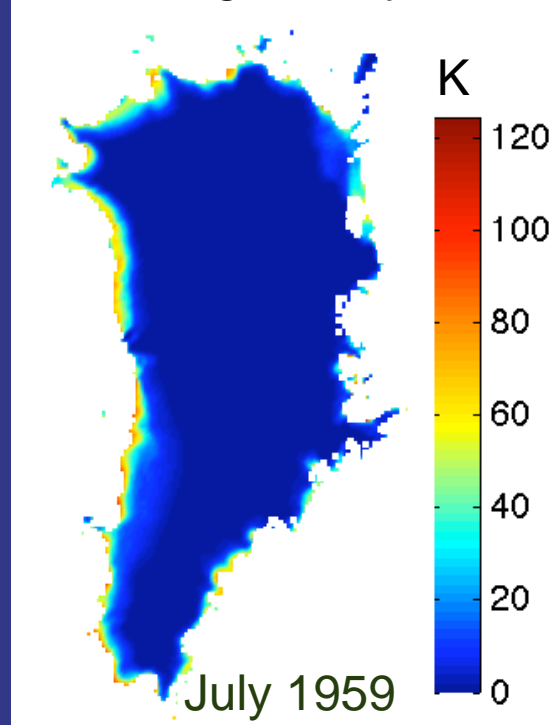
Degree-day
factor

Degree-day sum

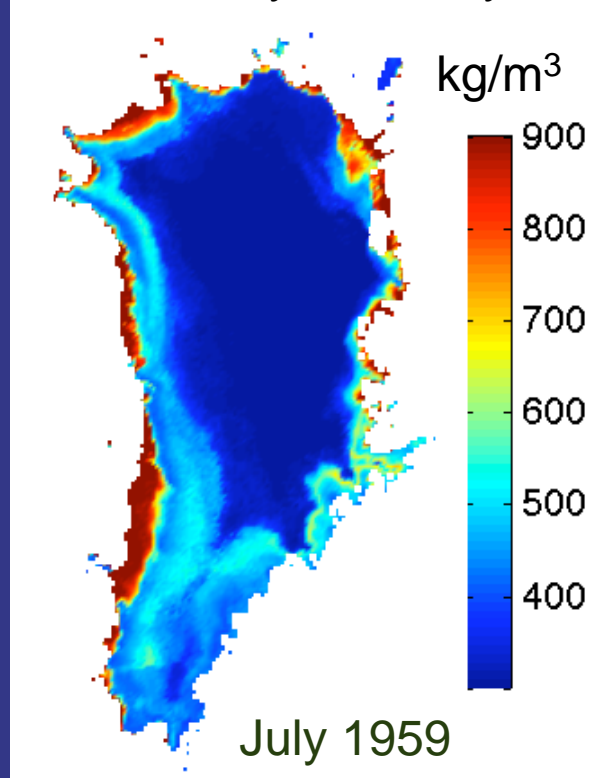
Degree-day factor ice



Pos. degree-days



Surface layer density

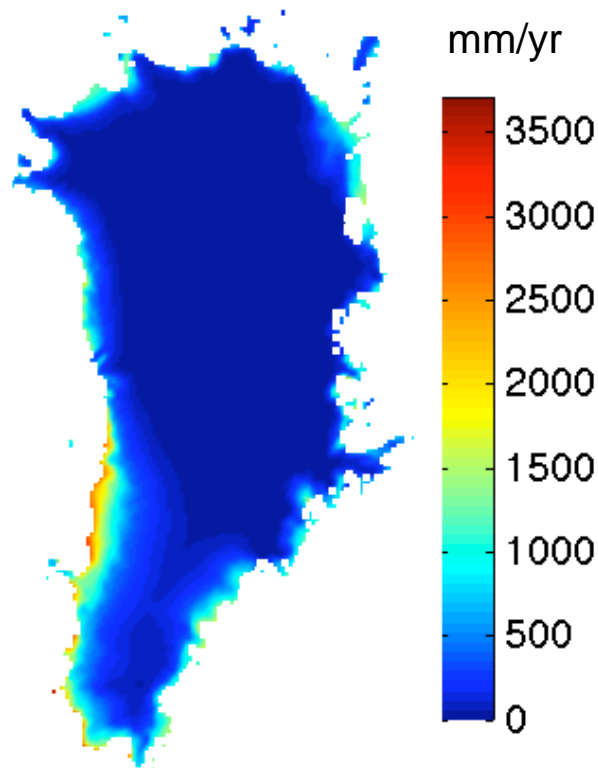


Density fields used to decide
whether surface is ice or snow
 $< 350 \text{ kg/m}^3 = \text{snow: } f_{\text{snow}},$
 $> 850 \text{ kg/m}^3 = \text{ice: } f_{\text{ice}}$
 linear interpolation of DDFs
 in between

■ How does the PDD model (Greve, 2005) compare to RACMO ?

Mean over 1957-2008

RACMO

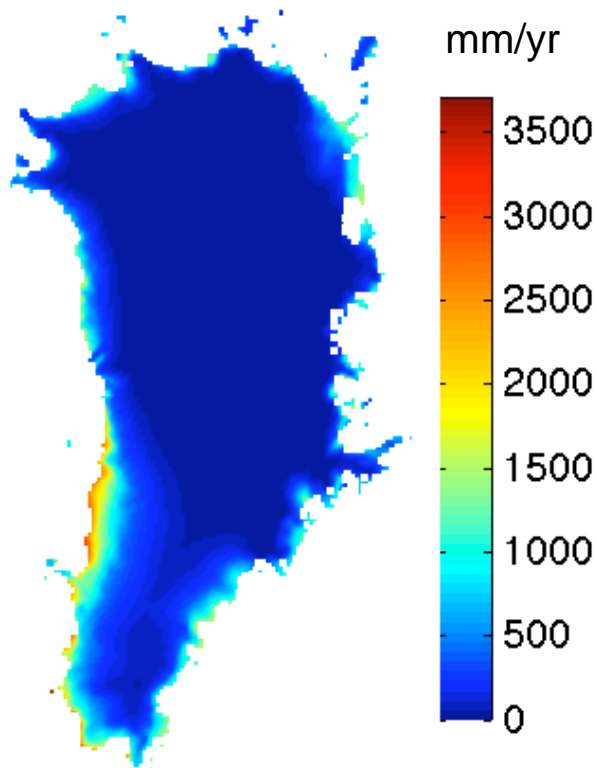


Mean annual melt
243 mm/yr
427 Gt/yr

■ How does the PDD model (Greve, 2005) compare to RACMO ?

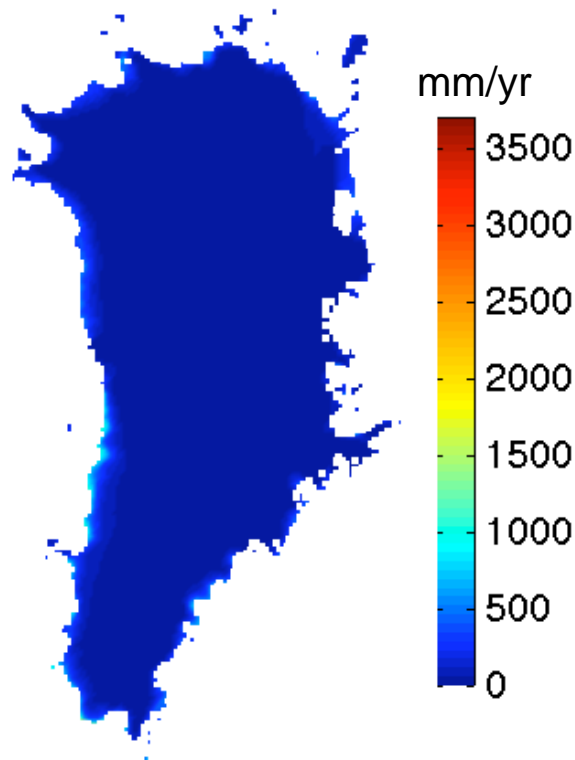
Mean over 1957-2008

RACMO



Mean annual melt
243 mm/yr
427 Gt/yr

DDF (Greve)

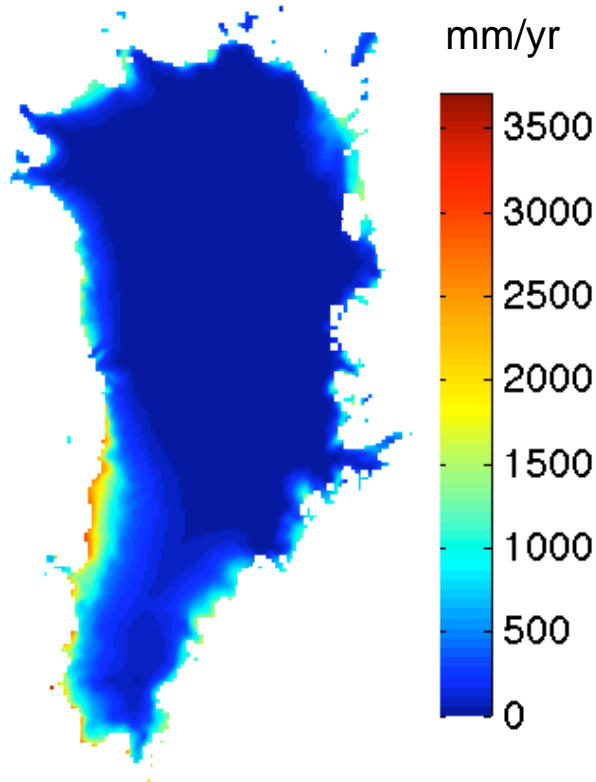


Mean annual melt
55 mm/yr
93 Gt/yr

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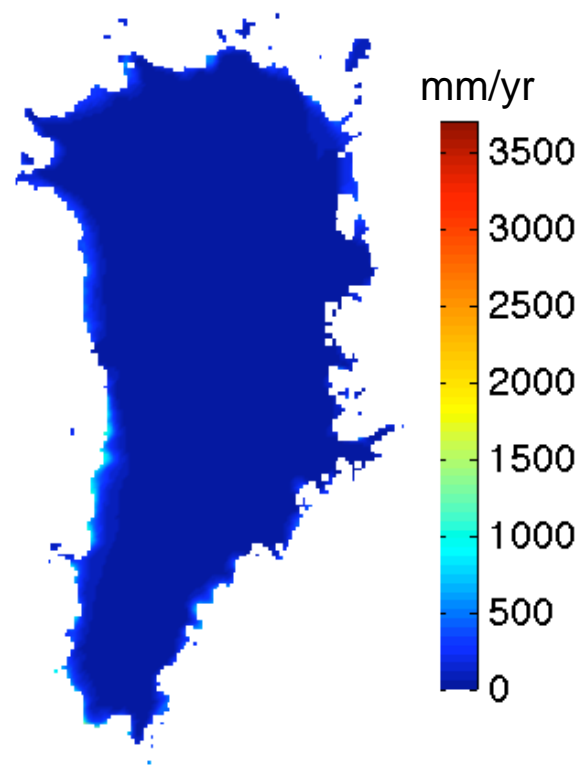
Mean over 1957-2008

RACMO



Mean annual melt
243 mm/yr
427 Gt/yr

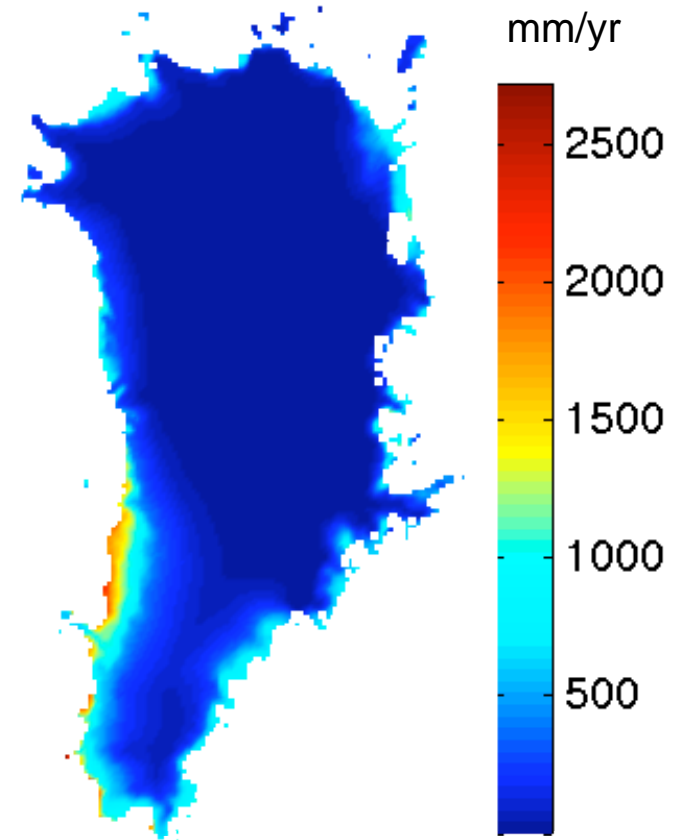
DDF (Greve)



Mean annual melt
55 mm/yr
93 Gt/yr

Difference

RACMO minus Degree-day



Difference
190 mm/yr
333 Gt/yr !!!

■ Objectives

to improve the surface mass model in PISM:

- **How good is the degree-day melt model that is currently implemented in PISM ?**
- How do degree-day factors vary spatially and what do they depend on ?
- How can degree-day factors be parameterized in a way that can be implemented into PISM ?



■ Objectives

to improve the surface mass model in PISM:

- How good is the degree-day factor that is currently implemented in PISM ?
- How do degree-day factors vary spatially and what do they depend on ?
- How can degree-day factors be parameterized in a way that can be implemented into PISM ?

No good



■ Objectives

to improve the surface mass model in PISM:

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- **How do degree-day factors vary spatially and what do they depend on ?**
- How can degree-day factors be parameterized in a way that can be implemented into PISM ?



■ Degree-days factors averaged over 1957-2008

DDF for grid cells with > 10 mm/yr melt and annual PDD > 10 dK, and DDF < 20 mm/d/K

$$\dot{M} = f_{snow/ice} \sum_{1}^n (T - T_0)$$

Degree-day
factor

Degree-day sum

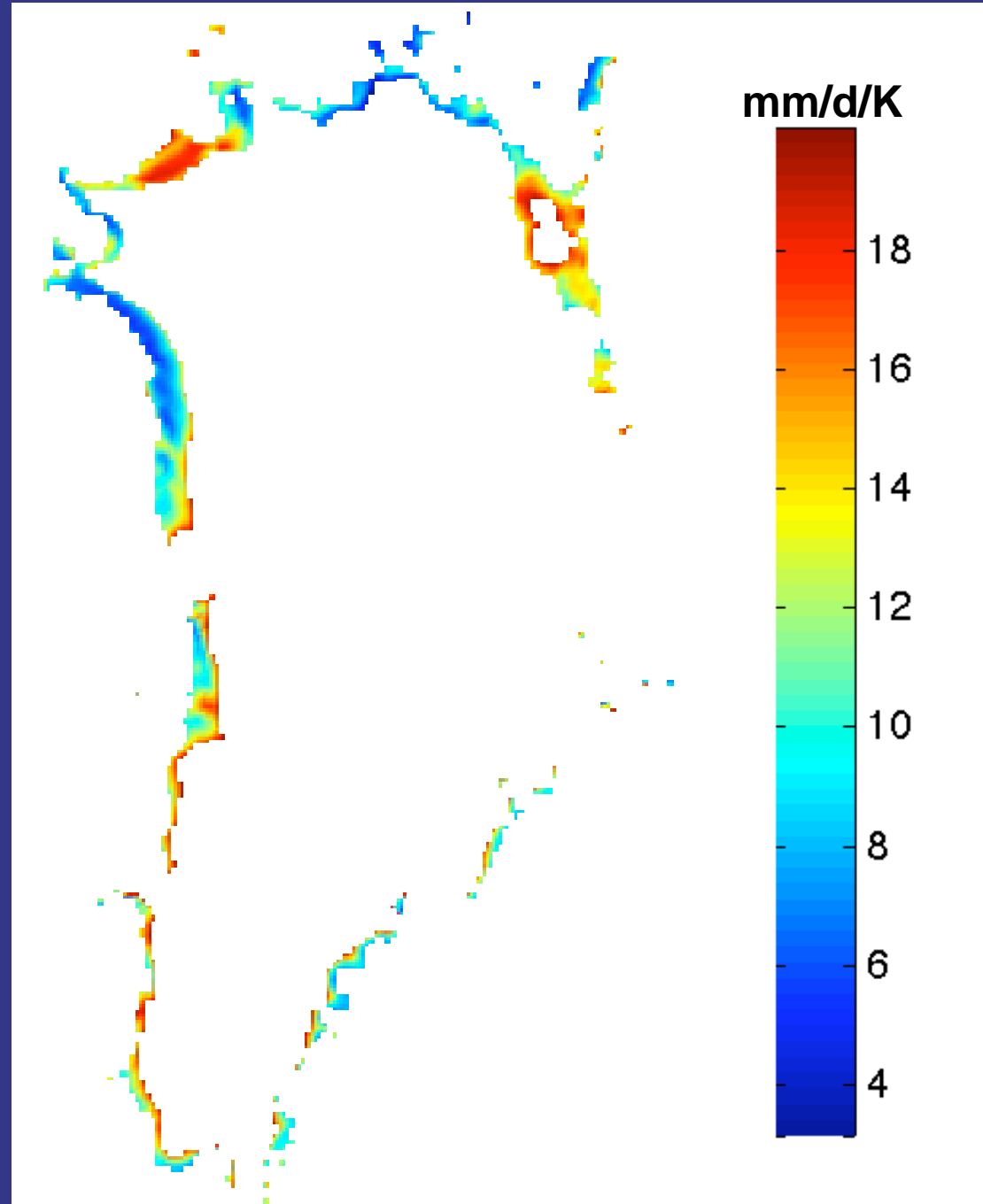
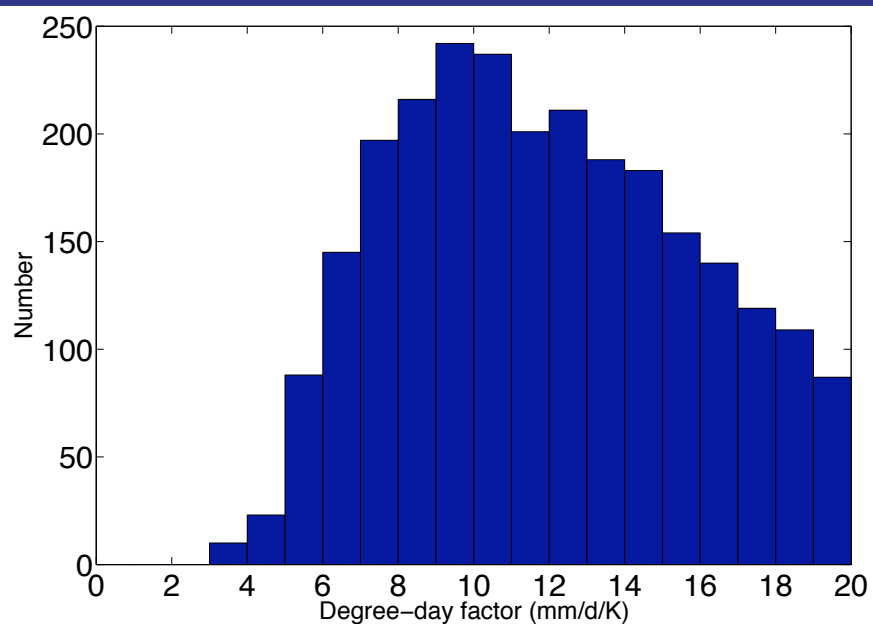
Degree-days factors averaged over 1957-2008

DDF for grid cells with > 10 mm/yr melt and annual PDD > 10 dK, and DDF < 20 mm/d/K

$$\dot{M} = f_{\text{snow/ice}} \sum_{1}^n (T - T_0)$$

Degree-day
factor

Degree-day sum



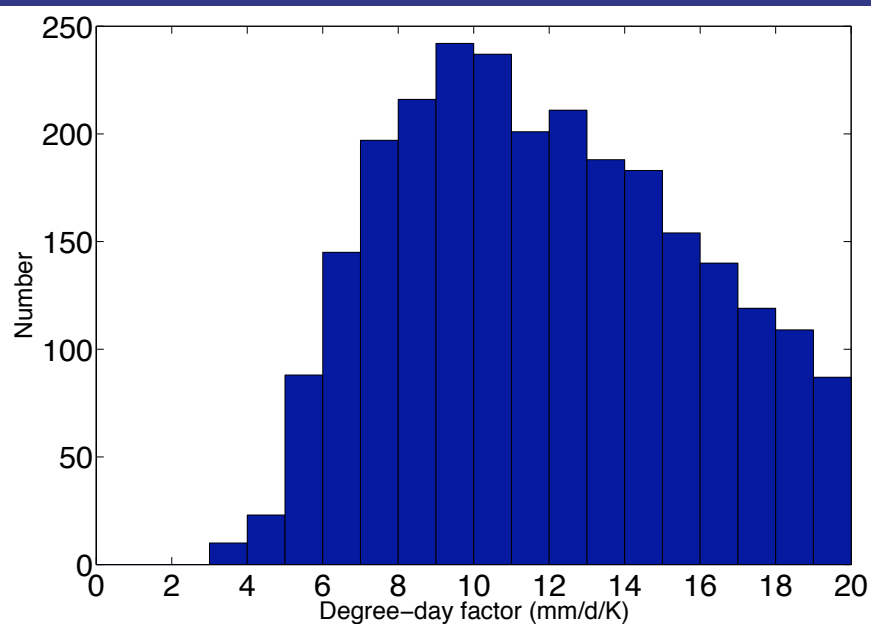
Degree-days factors averaged over 1957-2008

DDF for grid cells with > 10 mm/yr melt and annual PDD > 10 dK, and DDF < 20 mm/d/K

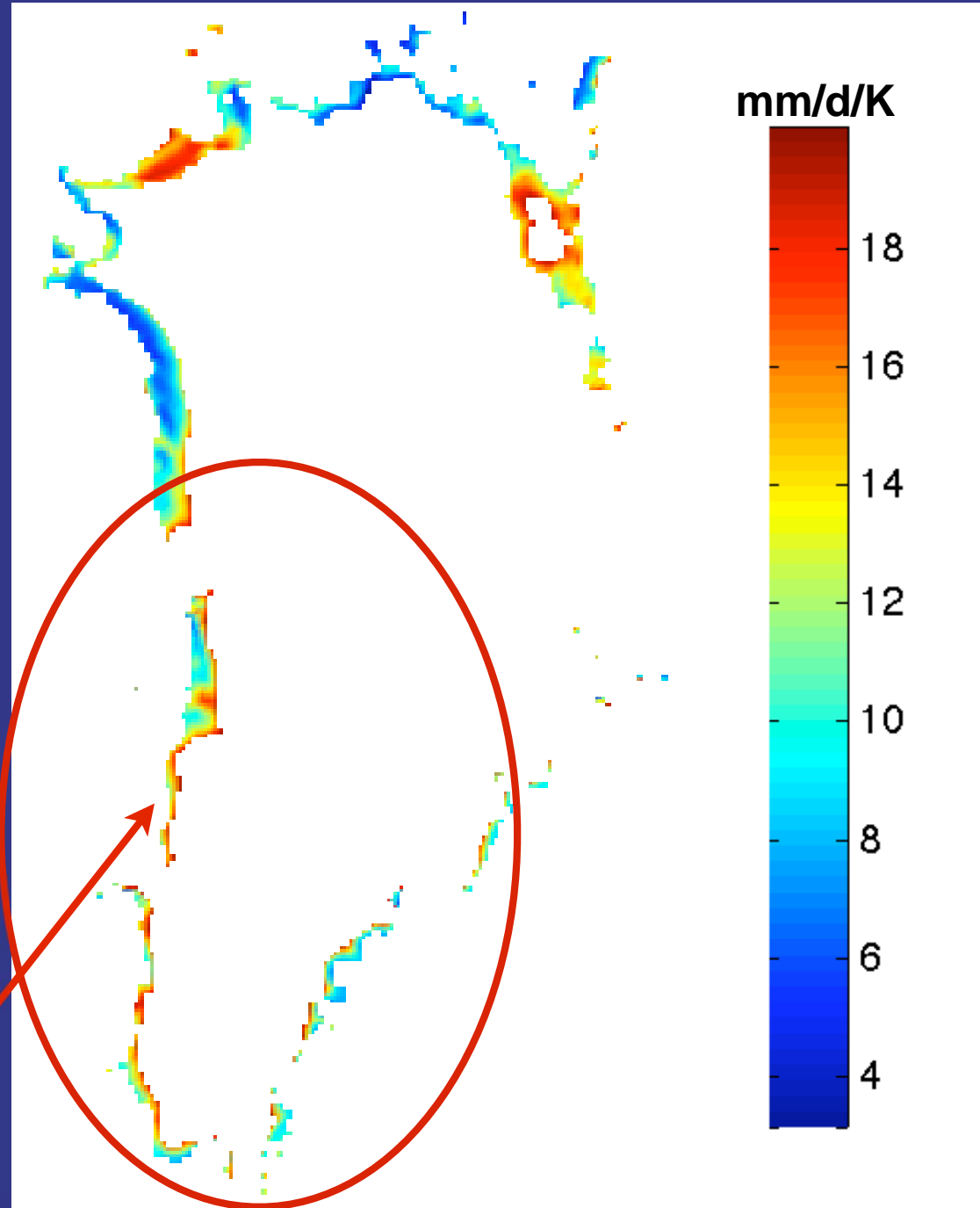
$$\dot{M} = f_{\text{snow/ice}} \sum_{1}^n (T - T_0)$$

Degree-day
factor

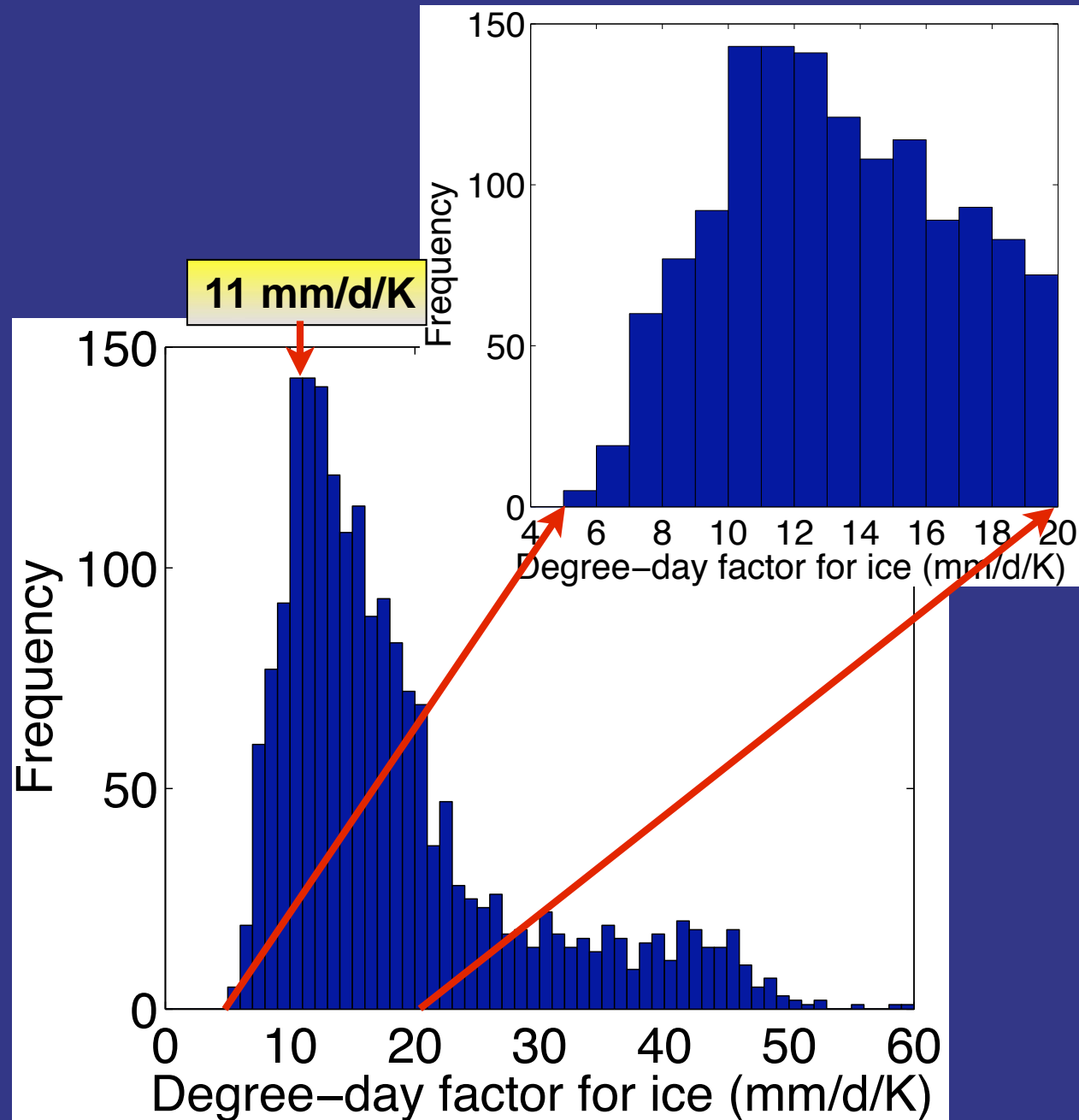
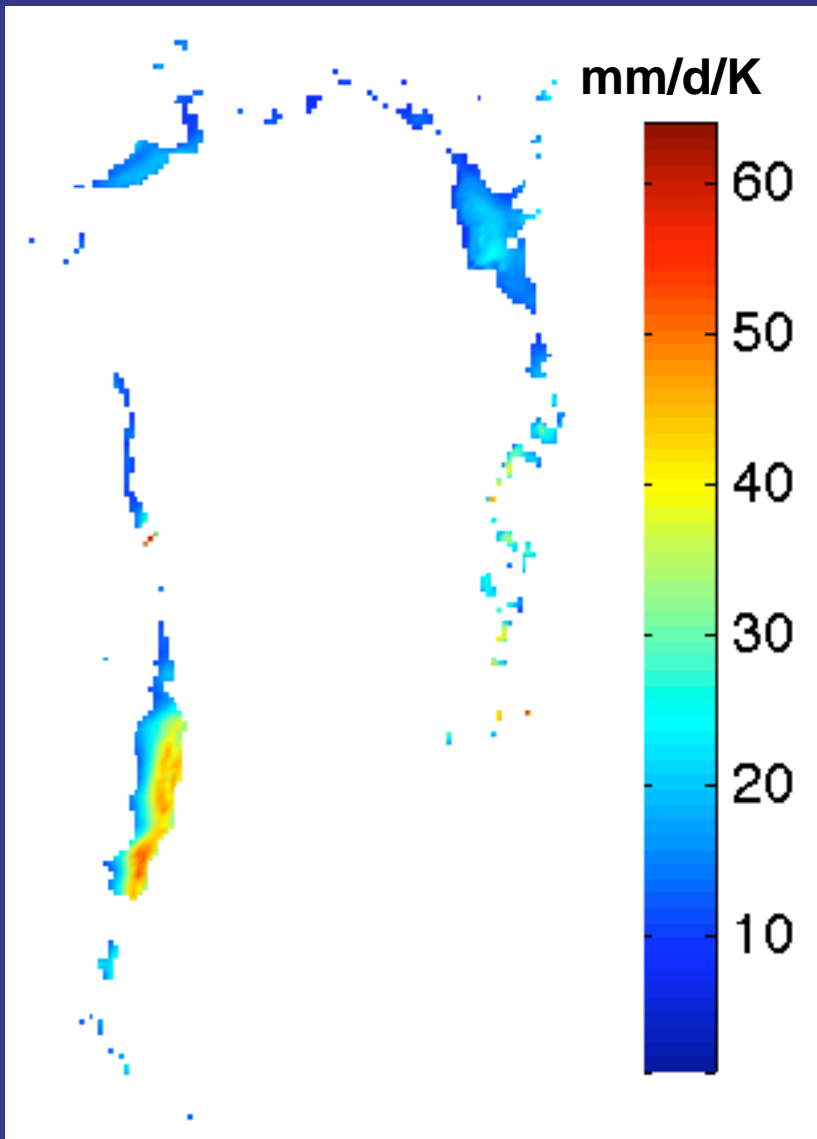
Degree-day sum



Degree-day factors
increase with
elevation

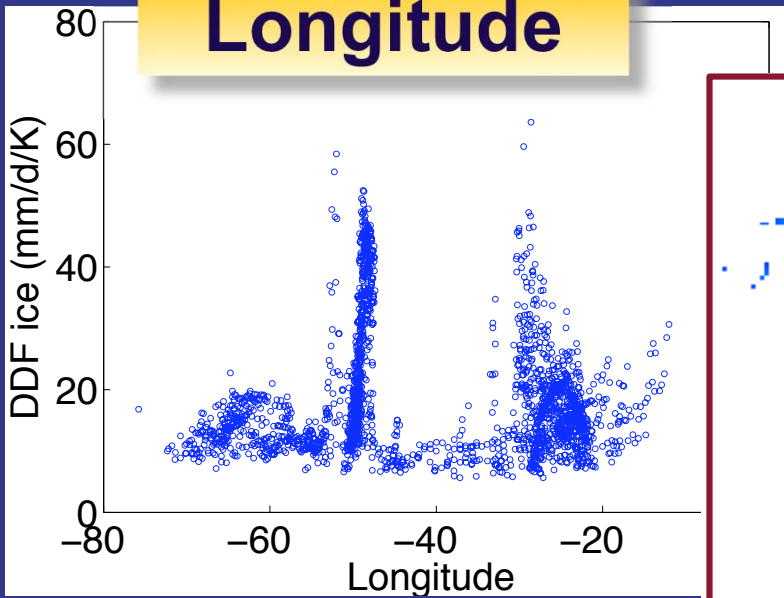


■ Degree-days factors for ice averaged over 1958-2008

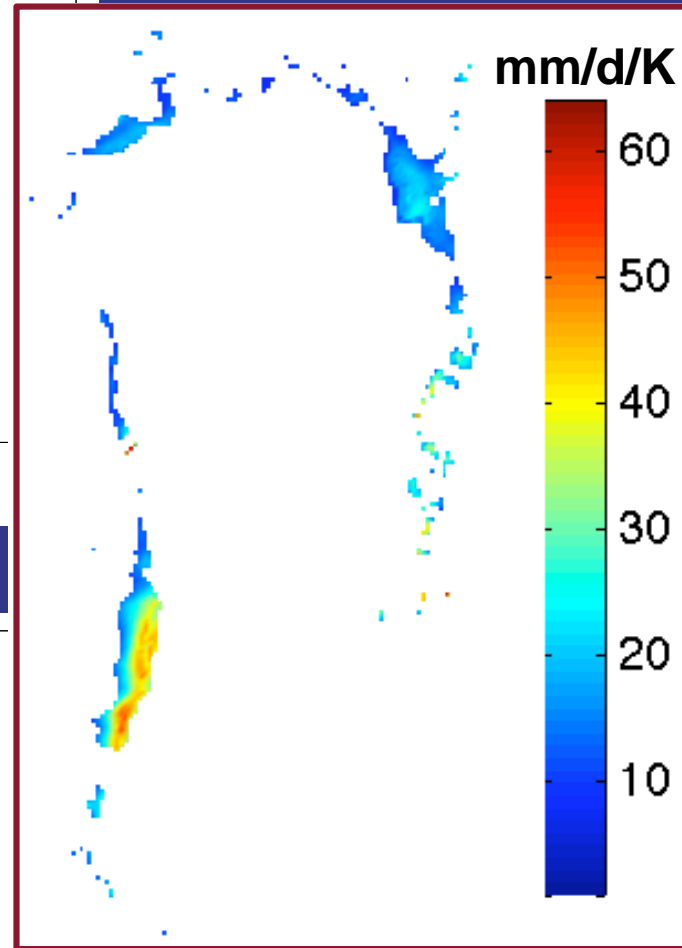
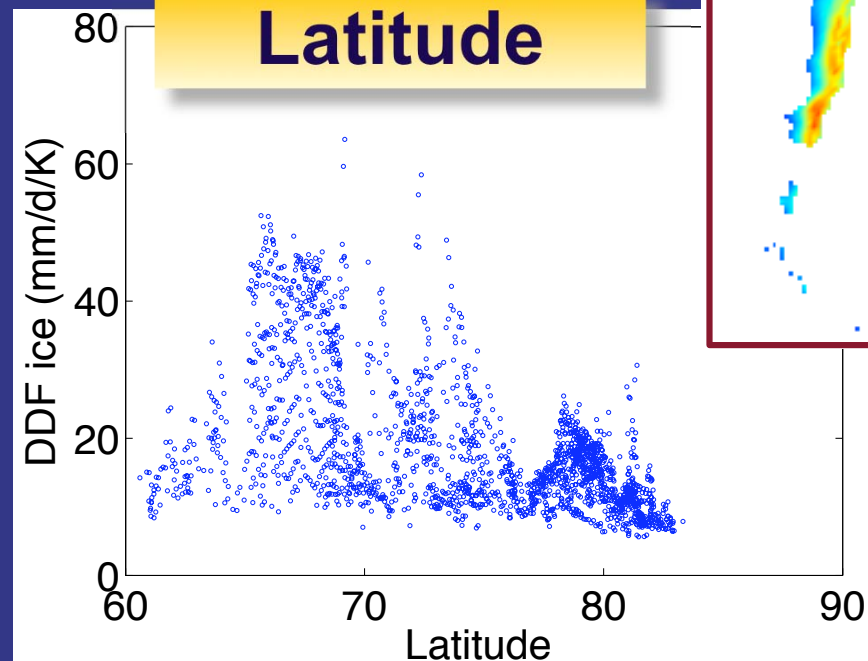


What do the degree-day factors for ice depend on?

Longitude



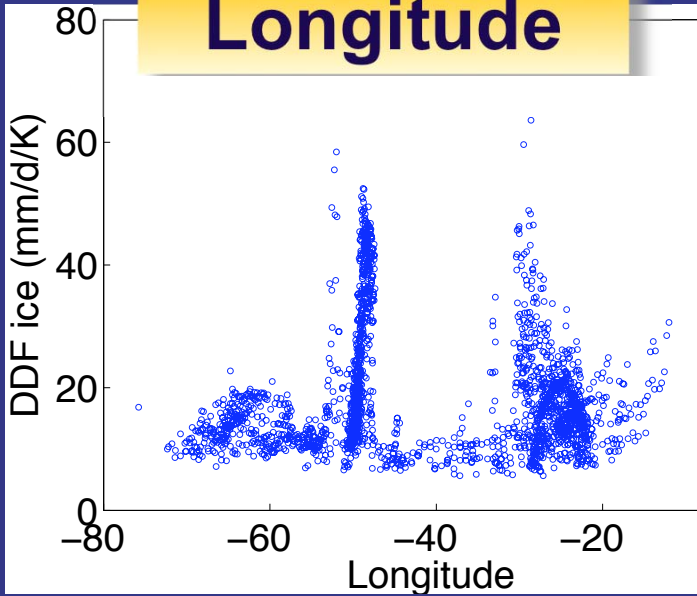
Latitude



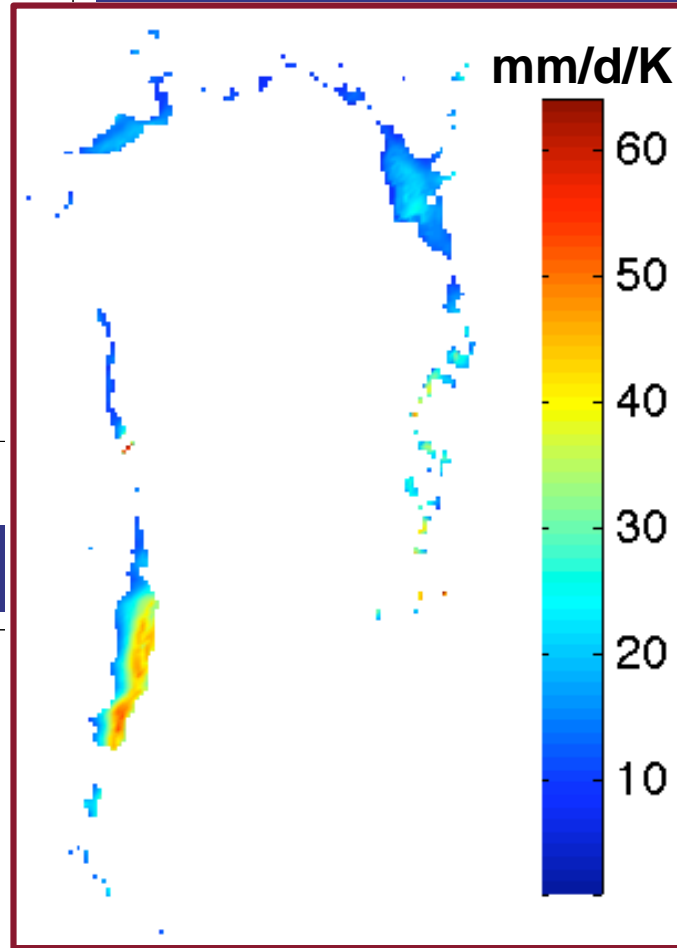
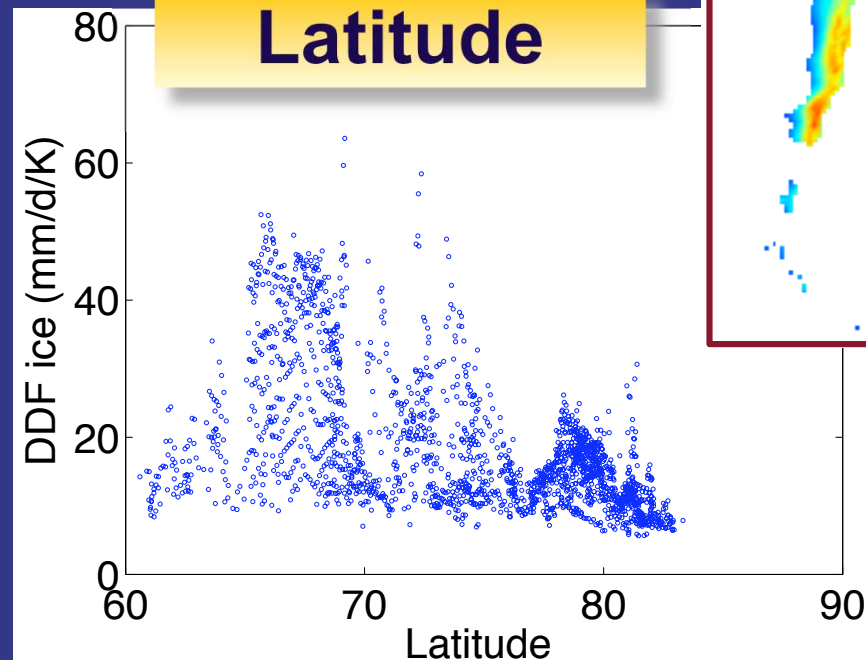
Means over ice-covered months 1958 - 2008 for each pixel

What do the degree-day factors for ice depend on?

Longitude

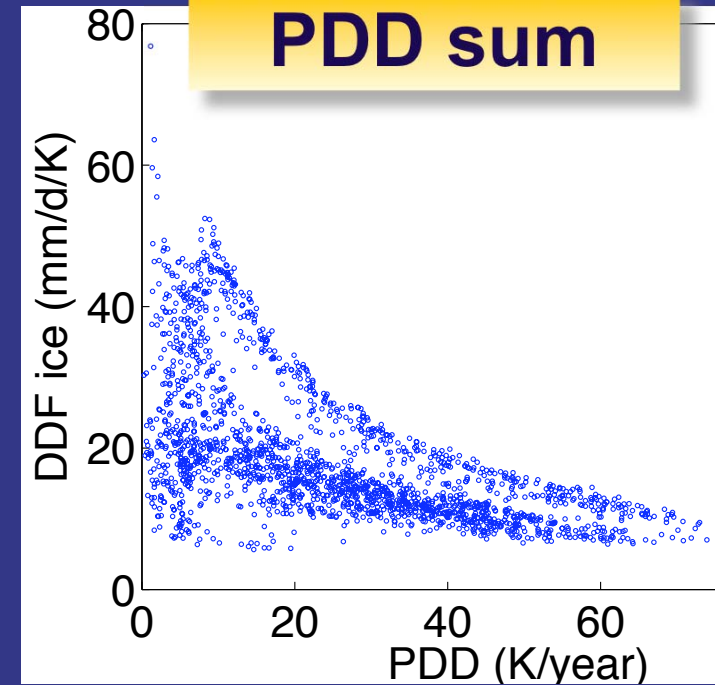


Latitude

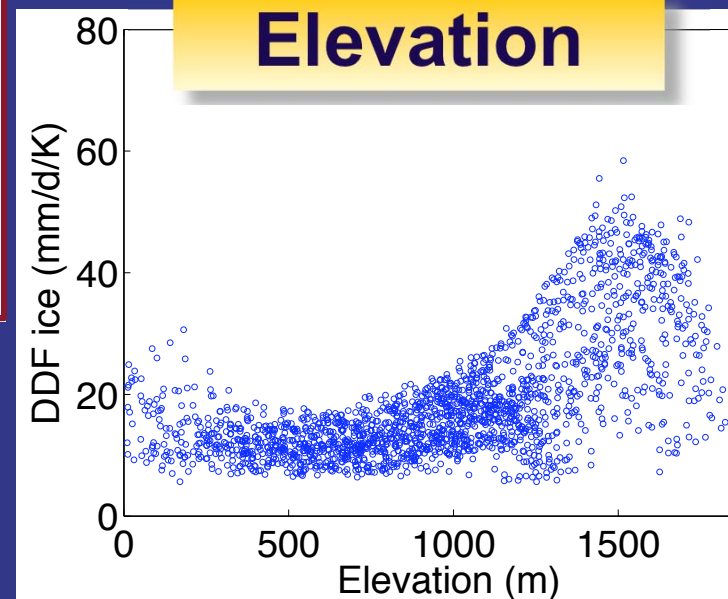


Means over ice-covered months 1958 - 2008 for each pixel

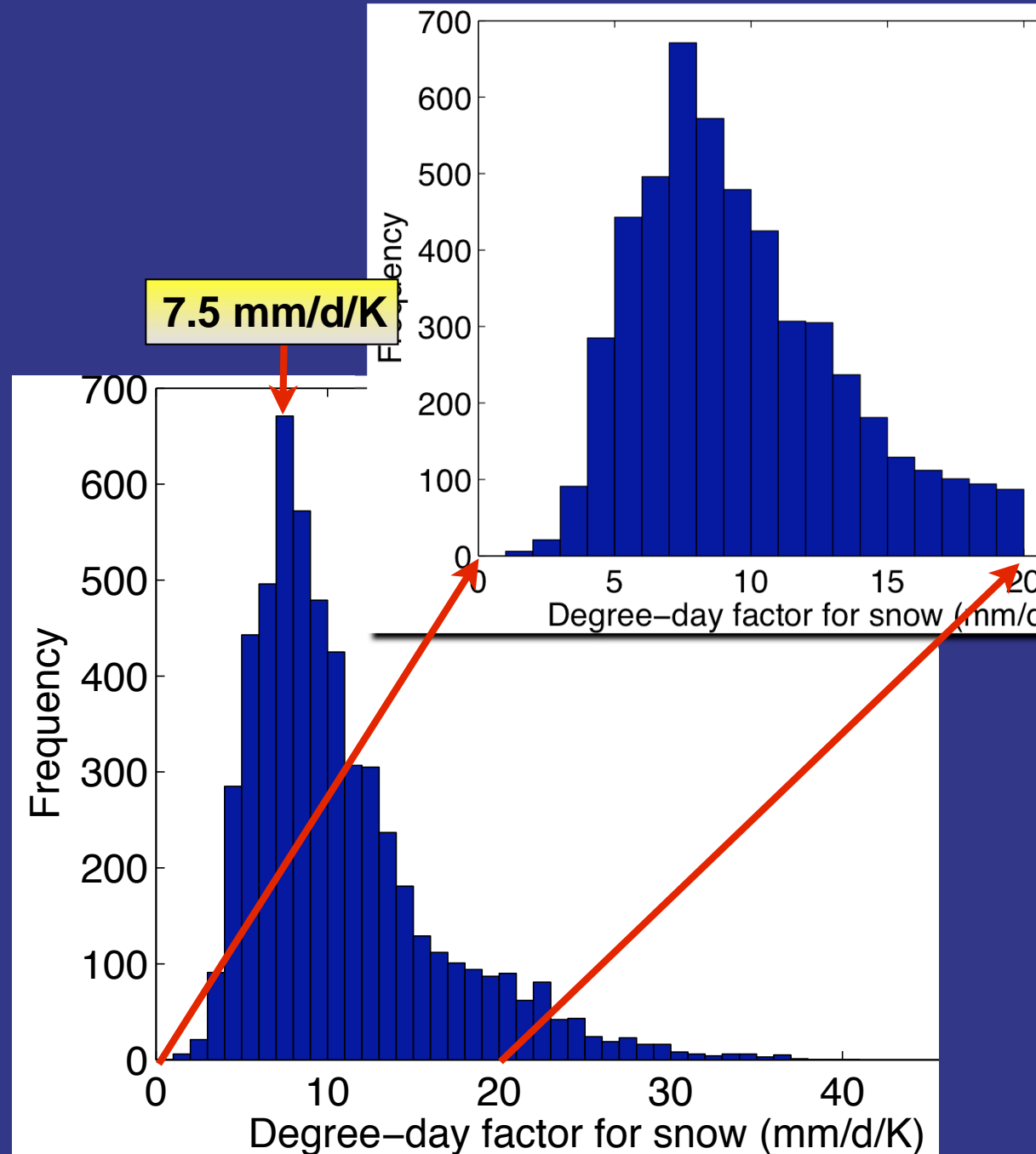
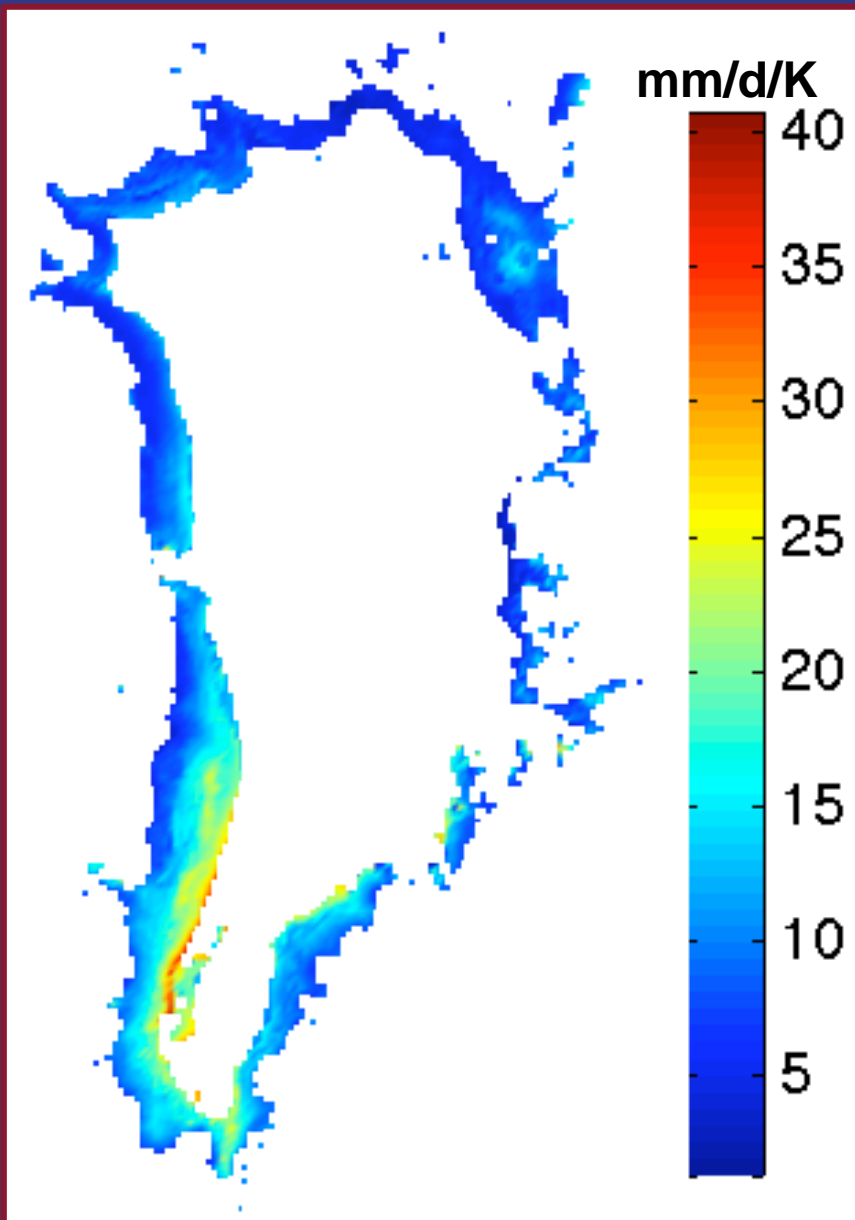
PDD sum



Elevation

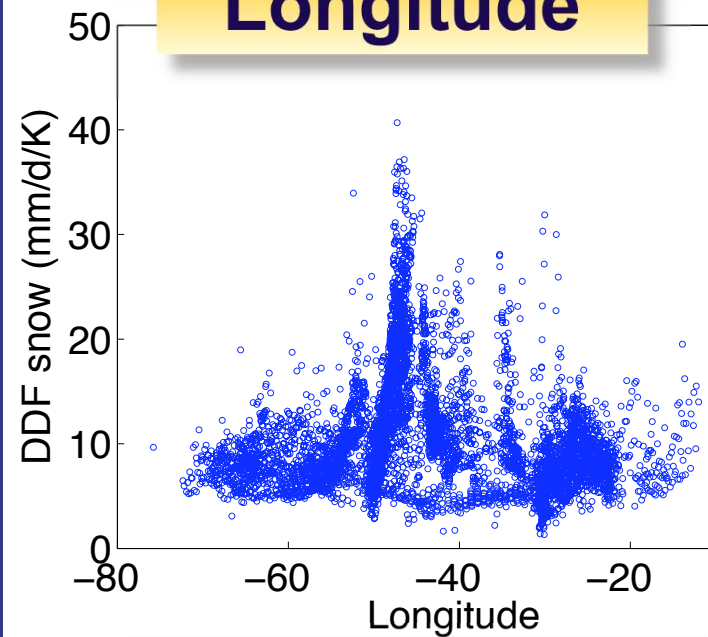


Degree-days factors for snow averaged over 1958-2008

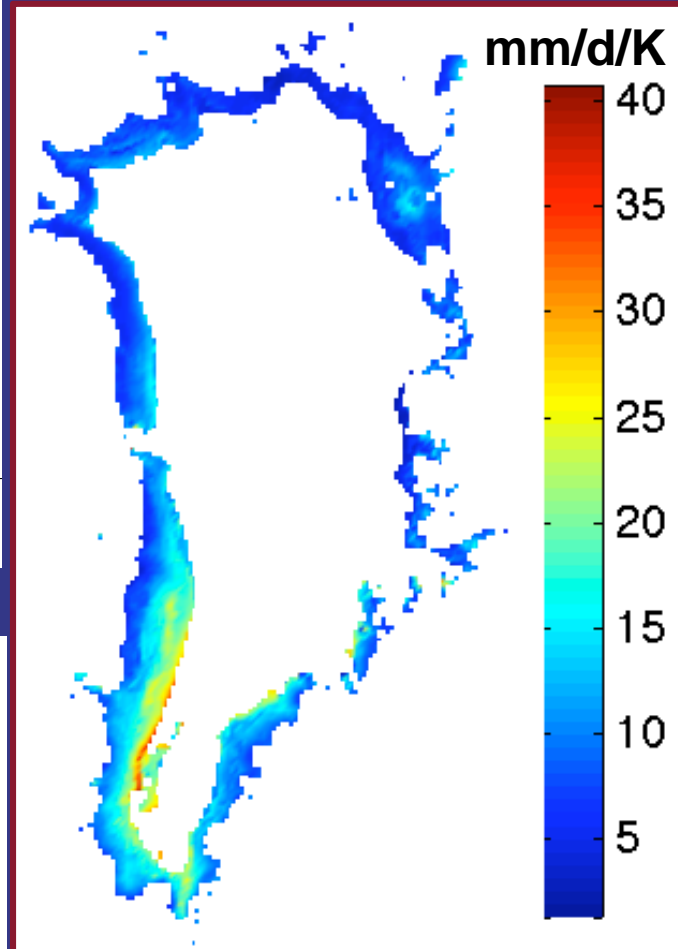
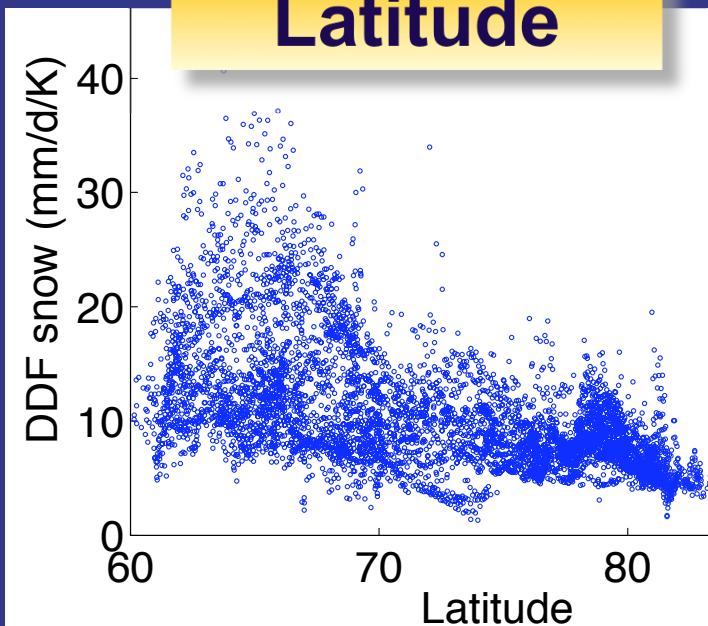


What do the degree-day factors for snow depend on?

Longitude



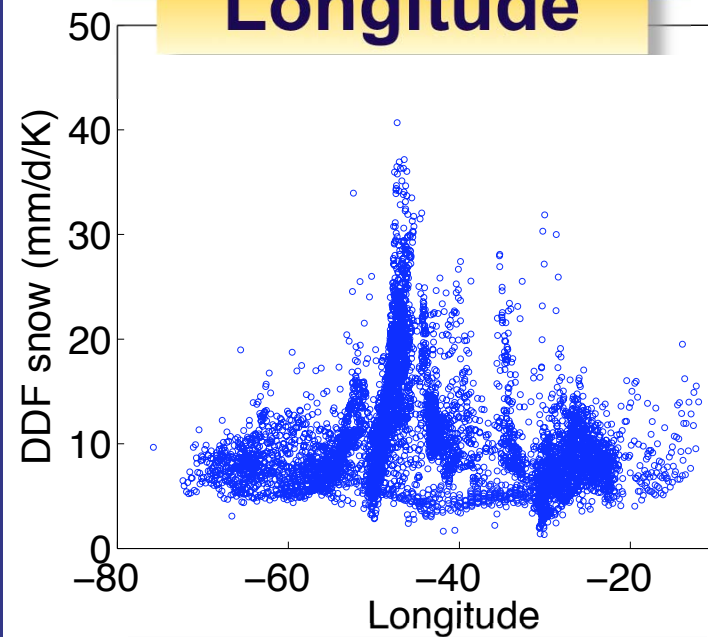
Latitude



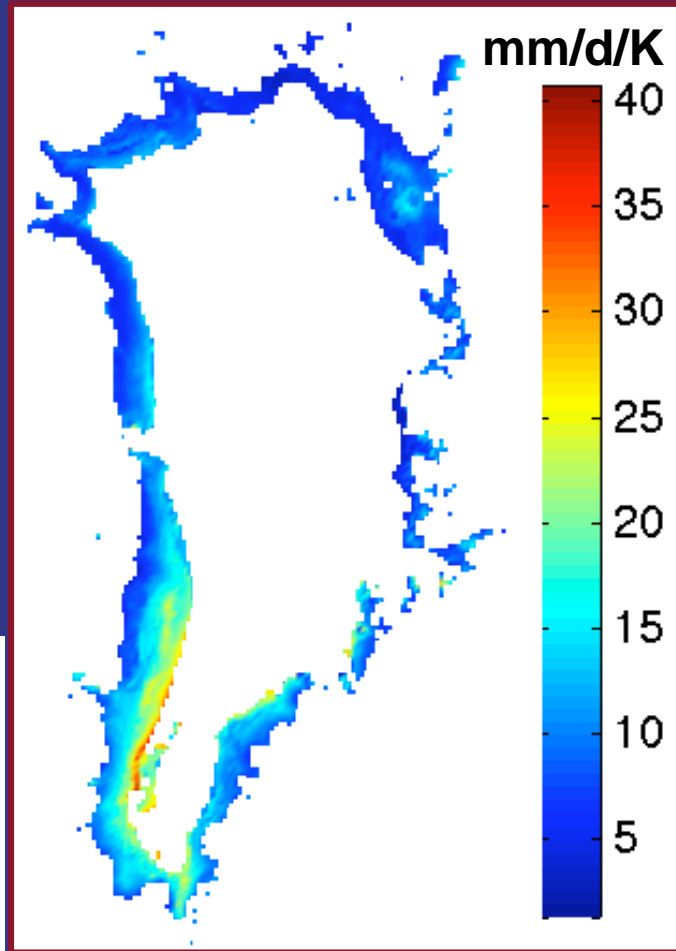
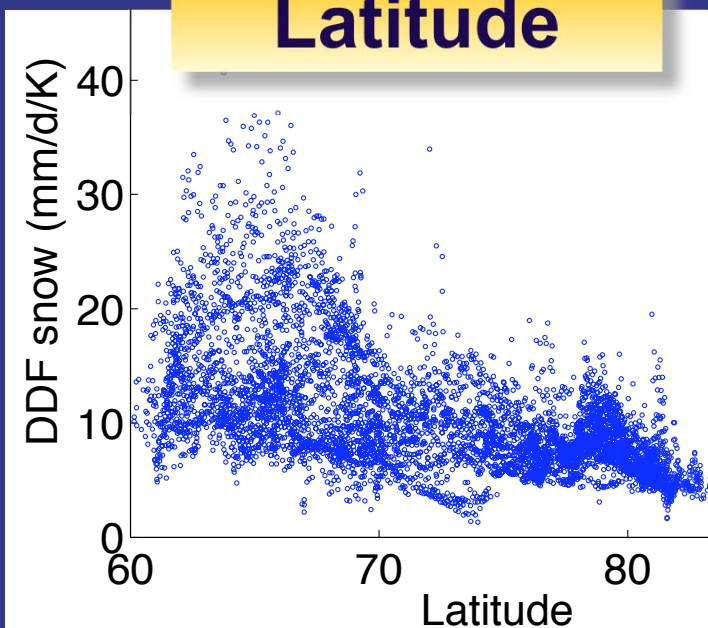
Means over ice-covered months 1958 - 2008 for each pixel

What do the degree-day factors for snow depend on?

Longitude

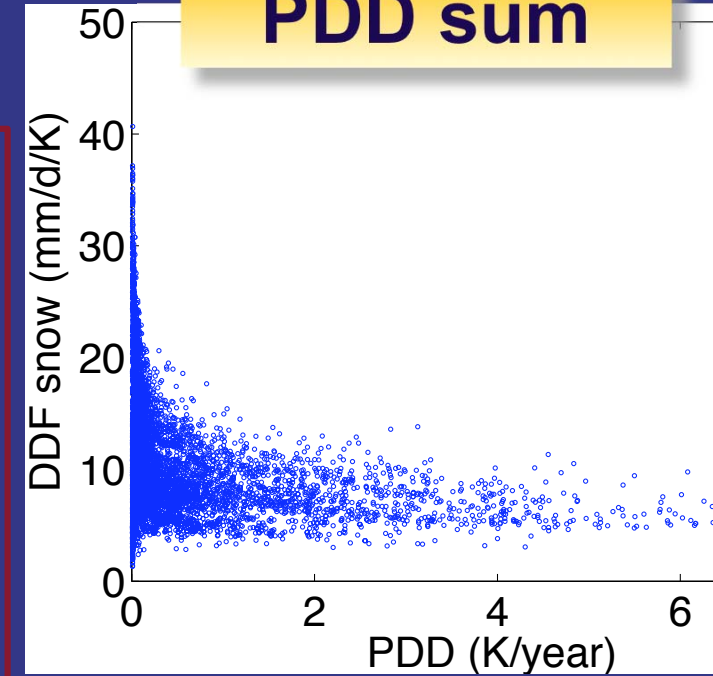


Latitude

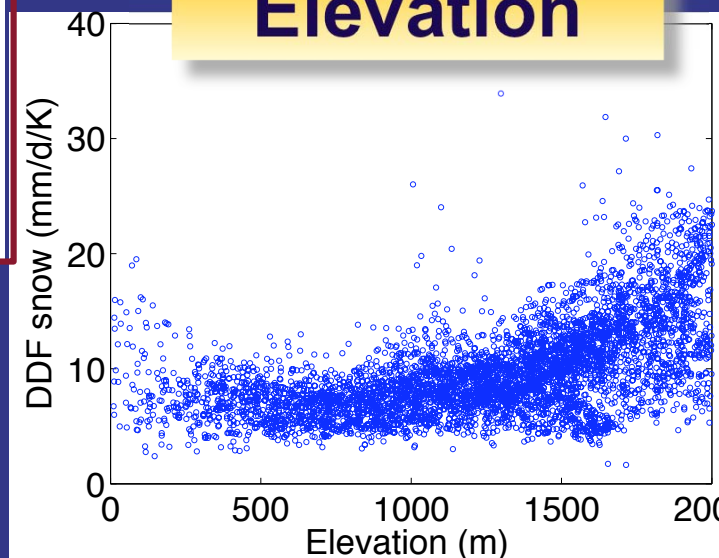


Means over ice-covered months 1958 - 2008 for each pixel

PDD sum



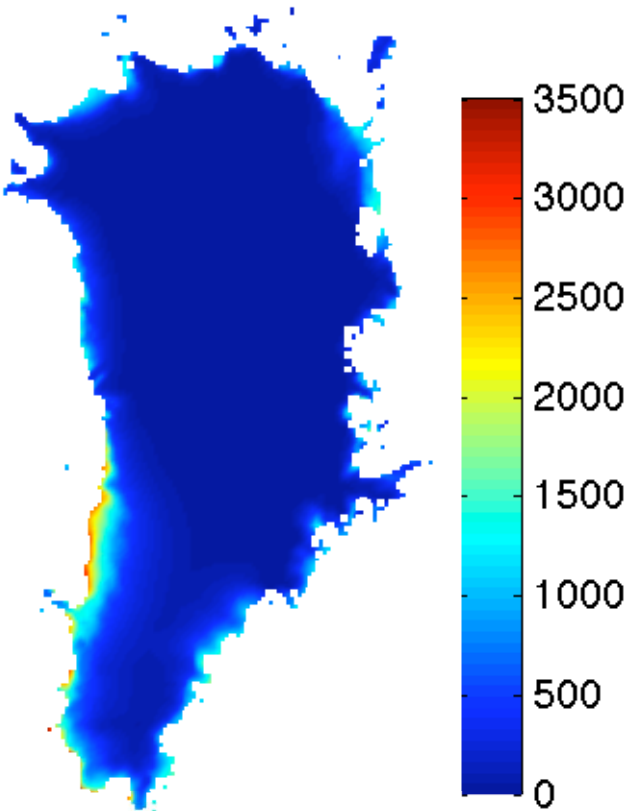
Elevation



■ Using spatially constant mean degree-day factors

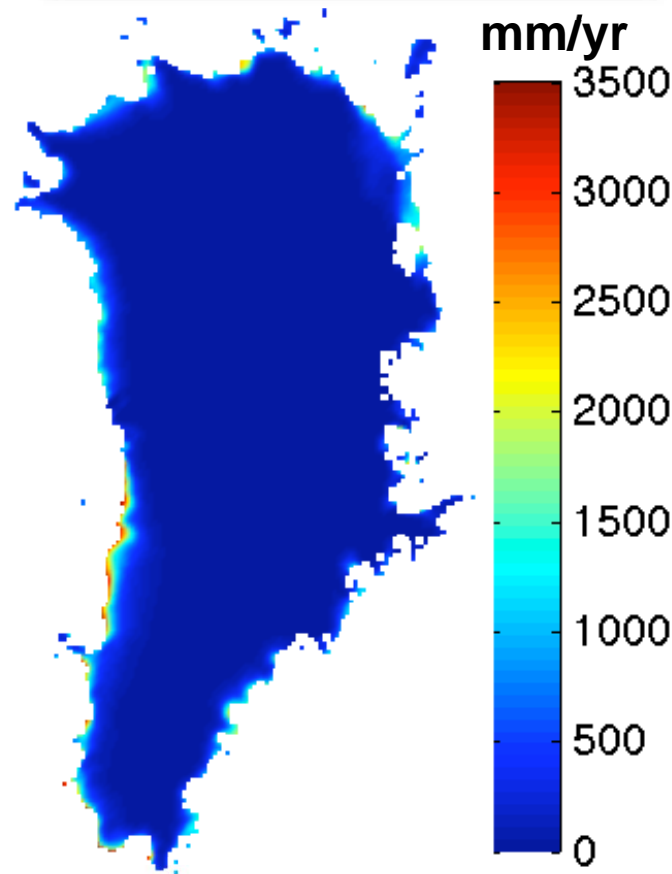
DDF_snow = 10.8 mm/d/K; DDF_ice = 18.7 mm/d/K

RACMO melt



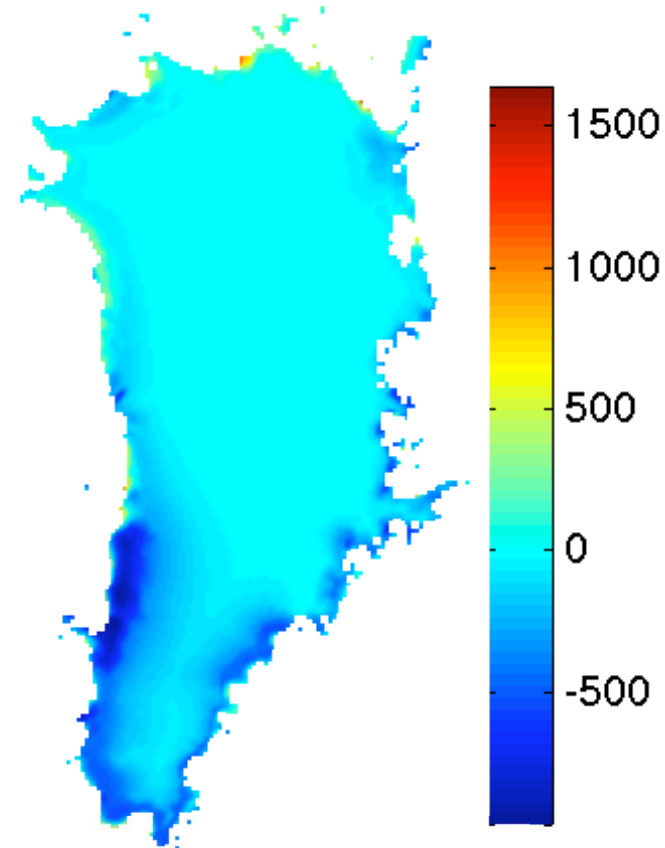
243 mm/yr
427 Gt/yr

Modeled melt



170 mm/yr
299 Gt/yr

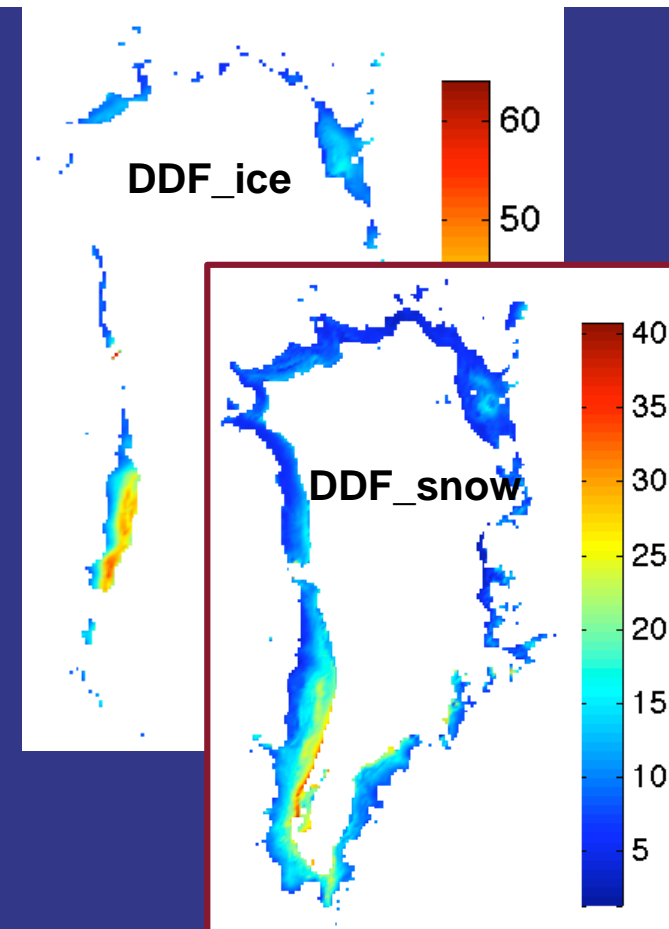
Difference (Modeled minus RACMO)



73 mm/yr
128 Gt/yr

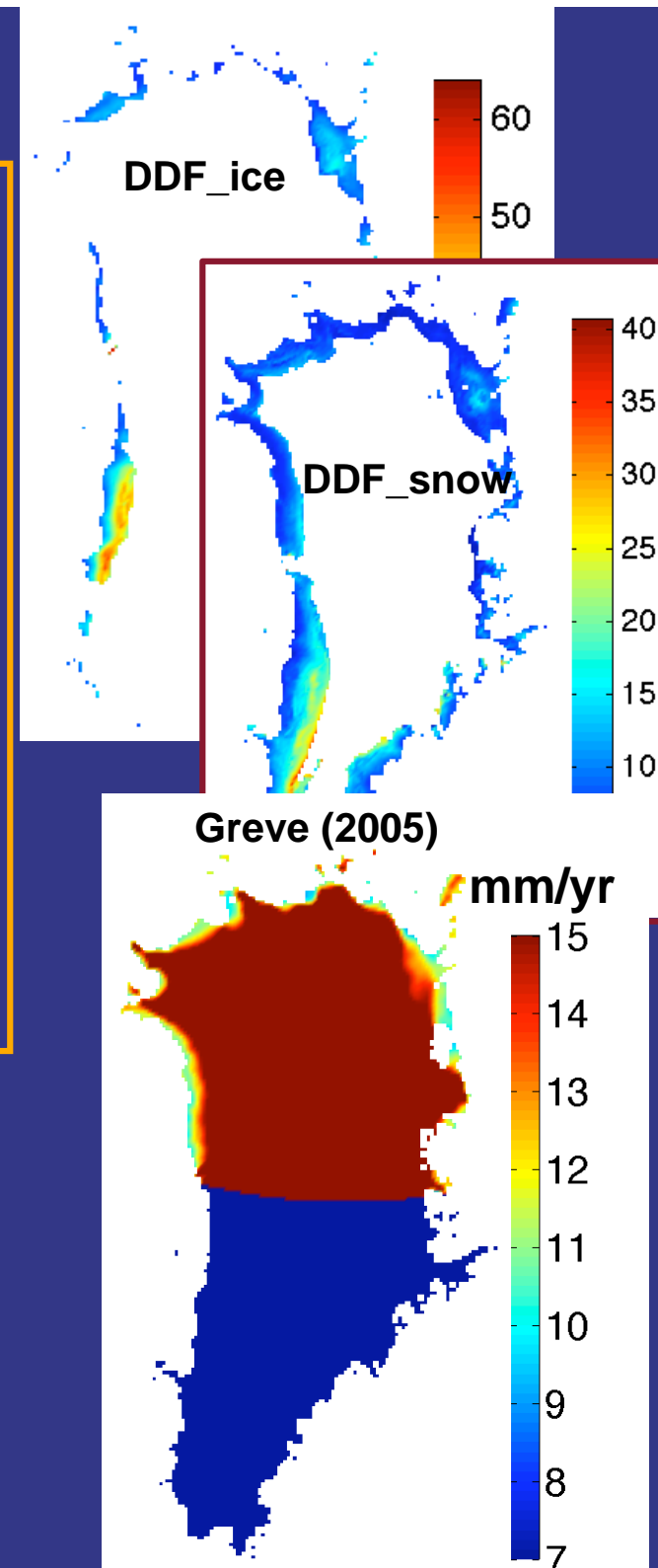
■ Conclusions

- Degree-day factors vary strongly in space; no clear geographical pattern; increase with elevation
- Uncertainties in degree-day estimates due to the uncertainties in RACMOs temperature, melt rates and surface densities



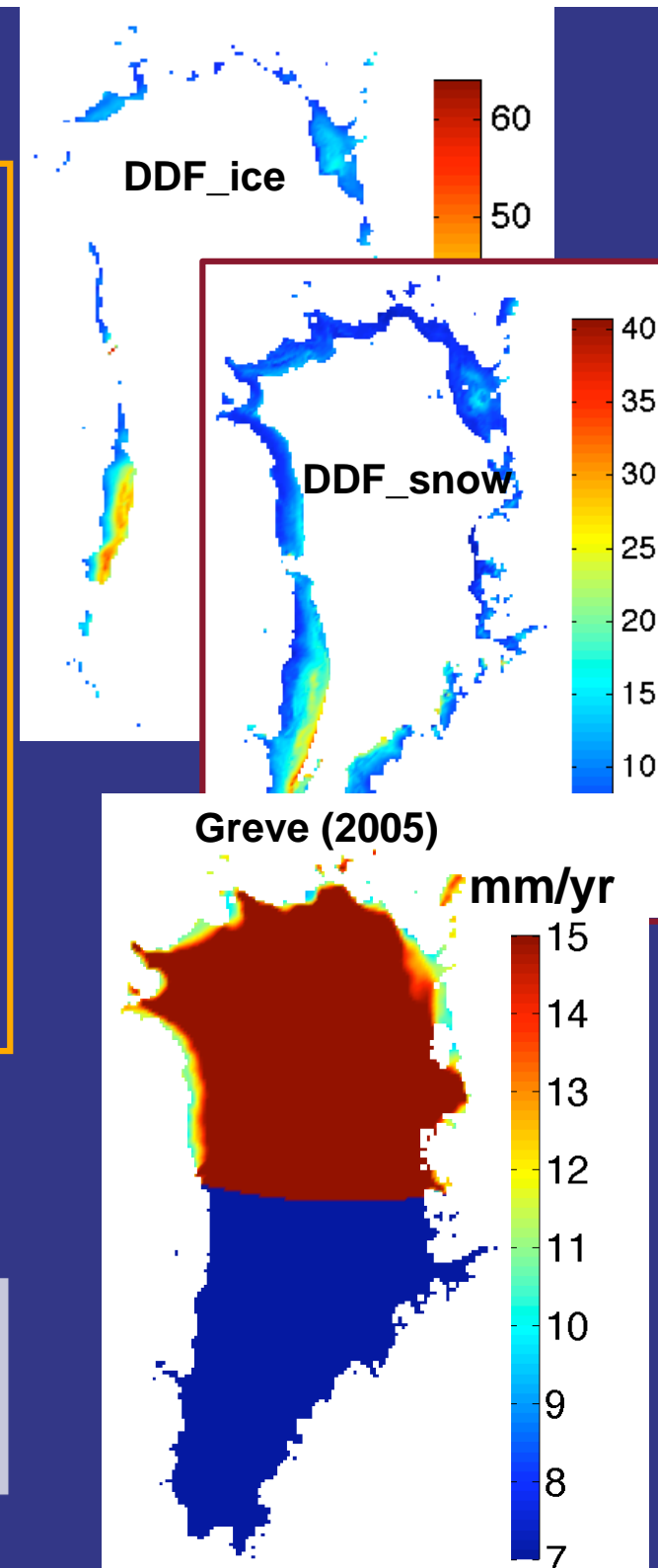
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The project is funded by the NASA Modeling, Analysis, and Prediction program (grant # NNX09AJ38G)