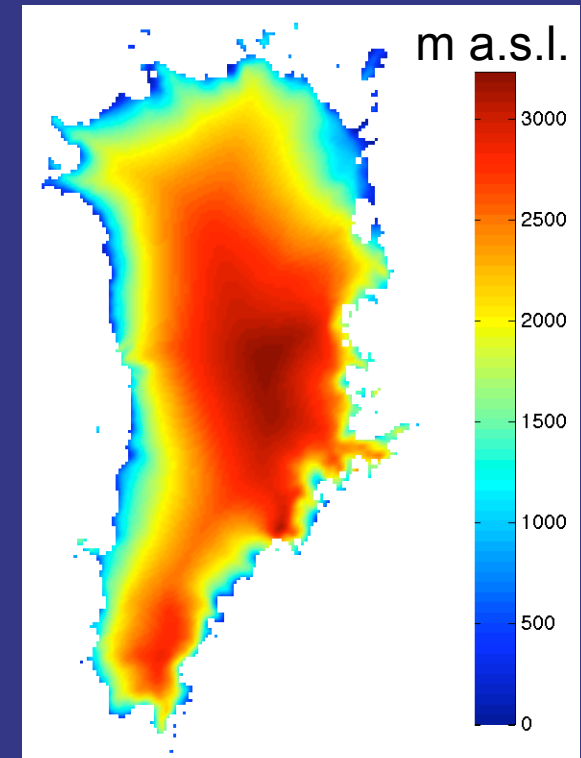


Parameterizing Greenland's surface mass balance in the Parallel Ice Sheet Model (PISM)



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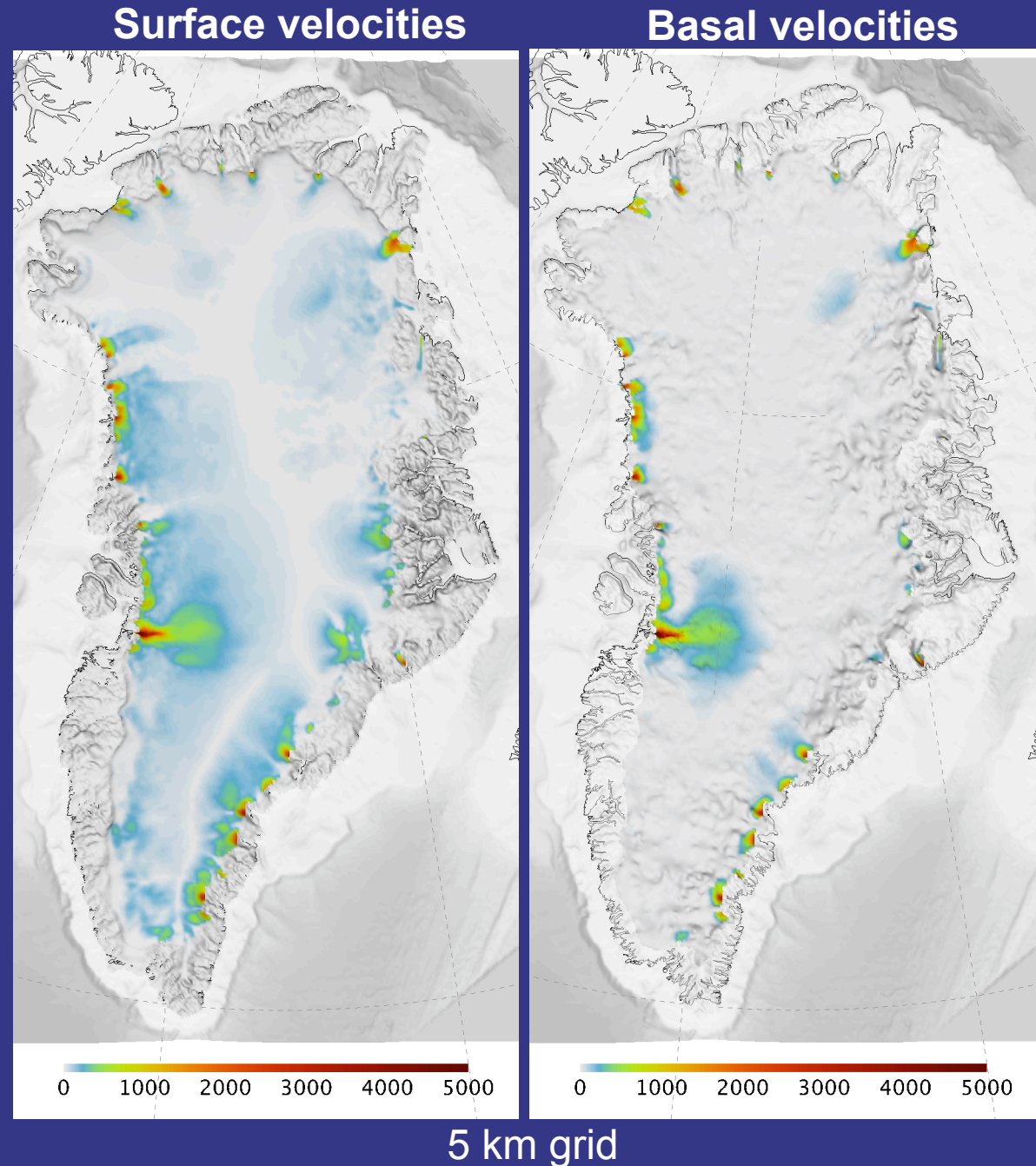
³*Institute for Marine and Atmospheric Research, Utrecht University, The Netherlands*

■ Background: PISM

- **Parallel Ice Sheet Model** is an open source, fully-parallel, high-resolution ice sheet model
- one of the models used in *SeaRISE* assessment (*Sea-level Response to Ice Sheet Evolution*) to project the ice sheet contributions to sea level in the next 100-200 years

Features:

- a hierarchy of available stress balances, including shallow ice and shelf approximations, a hybrid of these, and a (planned) higher-order scheme
- a polythermal, enthalpy-based conservation of energy scheme
- complete documentation for users and developers
- www.pism-docs.org



■ PISM: Surface mass balance

Classical degree-day approach

The diagram shows the equation $\dot{M} = f_{\text{snow/ice}} \sum_{1}^n (T - T_0)$ inside a yellow box. Three orange arrows point from labels to parts of the equation: 'Melt rate' points to \dot{M} , 'Degree-day factor' points to $f_{\text{snow/ice}}$, and 'degree-day sum' points to the summation term $\sum_{1}^n (T - T_0)$.

$$\dot{M} = f_{\text{snow/ice}} \sum_{1}^n (T - T_0)$$

Melt rate

Degree-day factor

degree-day sum

T = air temperature

T_0 = threshold temperature below which there is no melt;
in PISM: $T_0 = 0^\circ\text{C}$

Typical values for snow = 3-5 mm/d/K, ice = 6-10 mm/d/K

- **degree-day sum** is computed from positive temperatures multiplied by the duration (in days) when it is $> 0^\circ\text{C}$
- **degree-day factors** according to Greve (2005), *Ann. Glac.*, --> function of latitude and mean July temperature

• Greve, R. (2005). Relation of measured basal temperatures and the spatial distribution of the geothermal heat flux for the Greenland ice sheet. *Ann. Glaciol.*, 42, 424-432.

■ Purpose

to improve the degree-day model in PISM:

- **How do degree-day factors vary spatially ?**
- How do they vary in time: seasons, trends ?
- What do they depend on ?
- **How good is the degree-day model that is currently implemented in PISM ?**
- How can degree-day factors be parameterized in a way that can be implemented into PISM ?



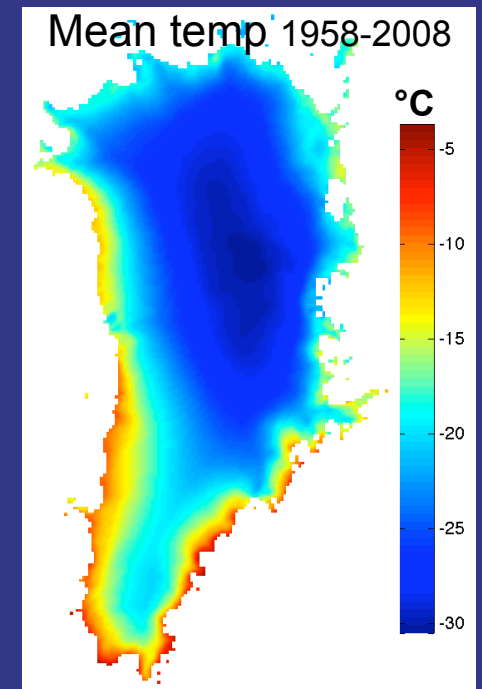
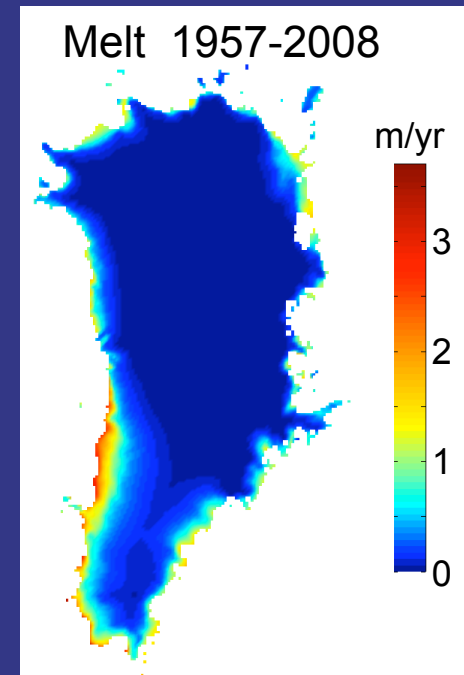
■ Data

Model

- RACMO2/GR Regional Climate Model
- lateral atmospheric forcings: ERA40 and ECMWF operational analysis
- resolution 11 km
- September 1957 - December 2008 (51.3 years)

Data

- Monthly melt
- Monthly and daily mean 2 m air temperatures
- Daily near-surface glacier density (to distinguish between snow and ice)



■ Degree-day factors

Classical degree-day approach

Melt rate $\dot{M} = f_{snow/ice} \sum_{1}^n (T - T_0)$ **Daily data**

Degree-day factor $f_{snow/ice}$

degree-day sum $\sum_{1}^n (T - T_0)$

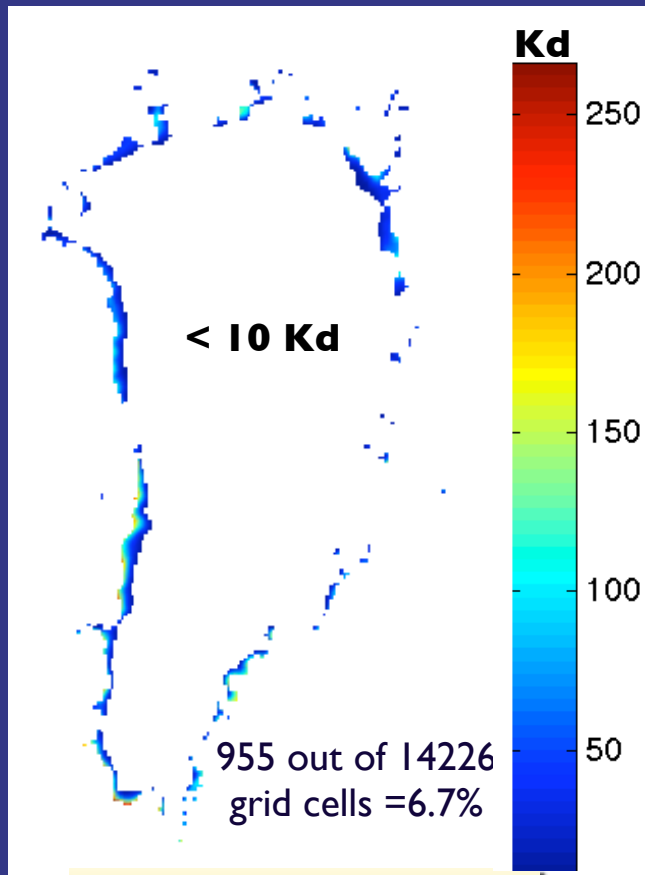
T = air temperature

T_0 = threshold temperature below which there is no melt;
in PISM: $T_0 = 0^{\circ}\text{C}$

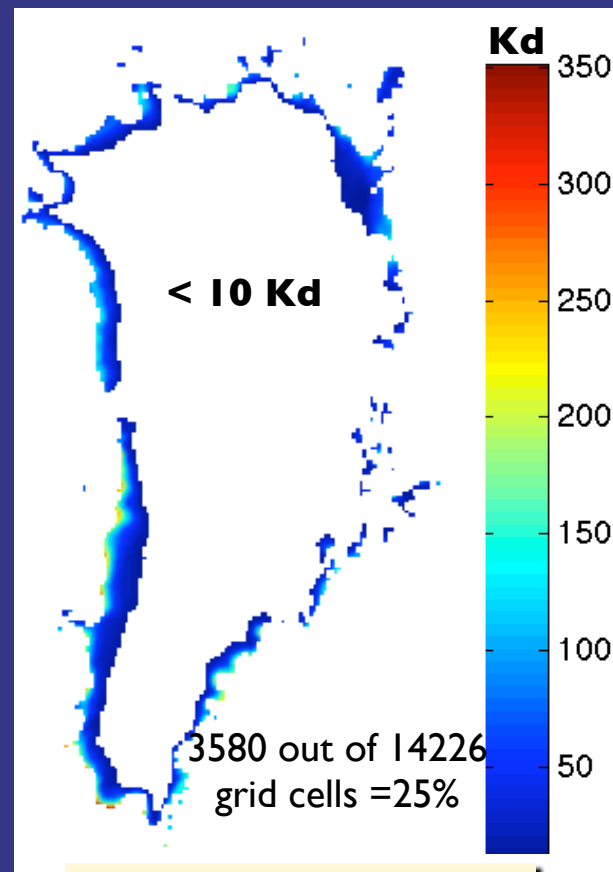
$\dot{M} = f_{snow/ice} T_{month}^{+}$ **Monthly data**

Positive degree-days and annual melt 1957-2008

Positive degree-days, PDD (Kd)

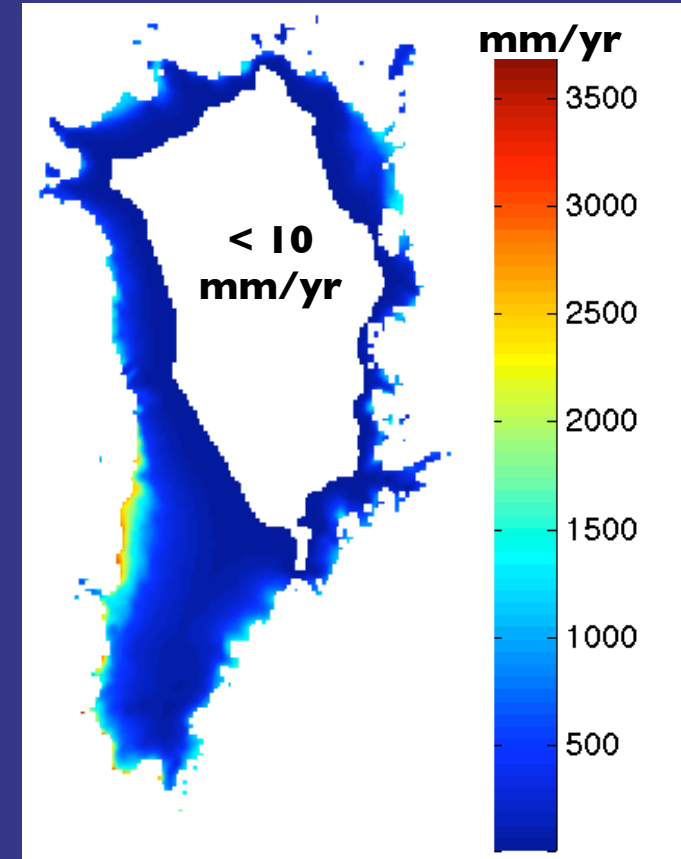


based on
monthly mean
temperatures



based on **daily**
mean temperatures

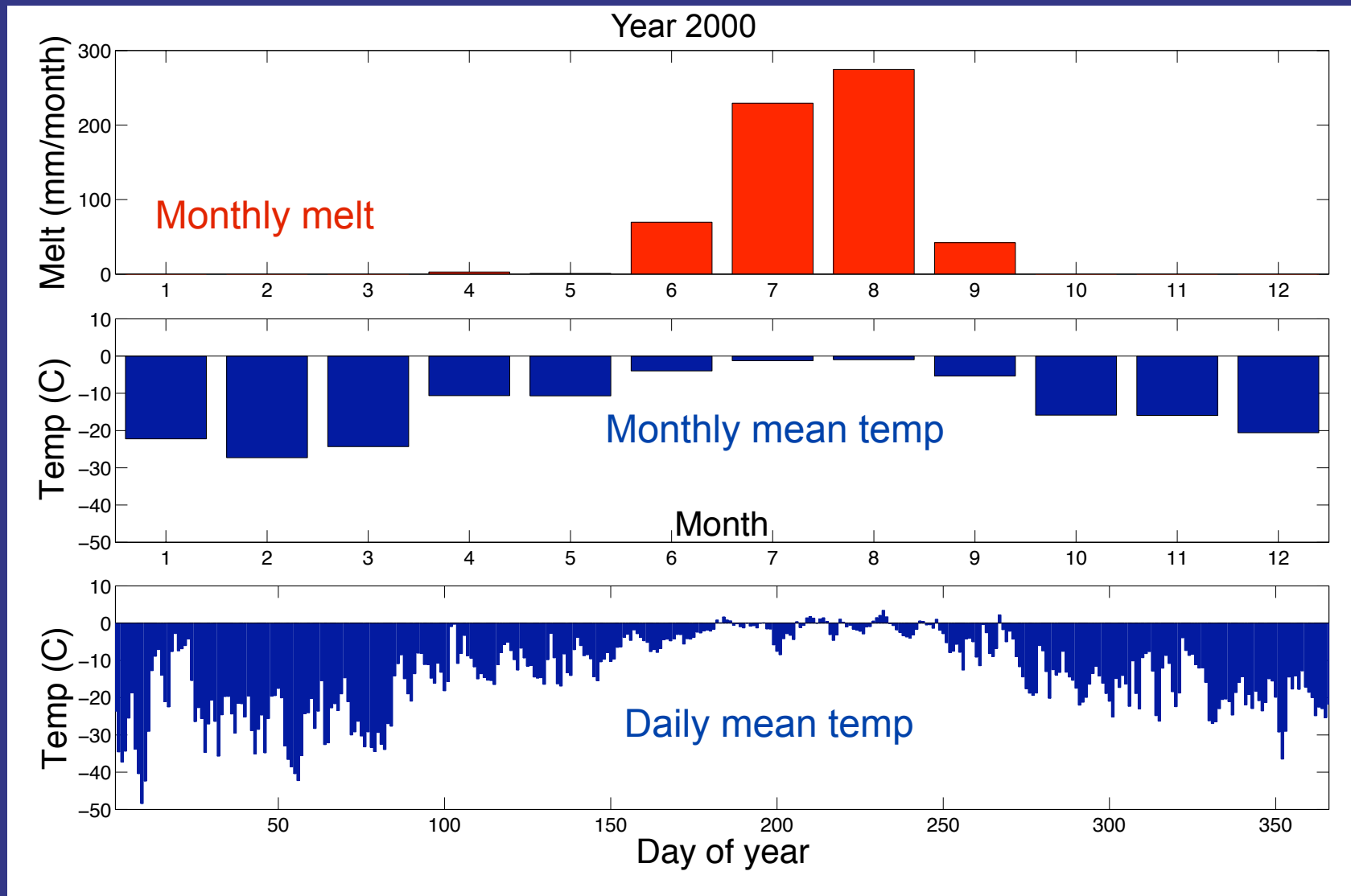
Annual melt (mm/yr)



$$\dot{M} = f_{snow/ice} T_{month}^+$$

$$\dot{M} = f_{snow/ice} \sum_{1}^n (T - T_0)$$

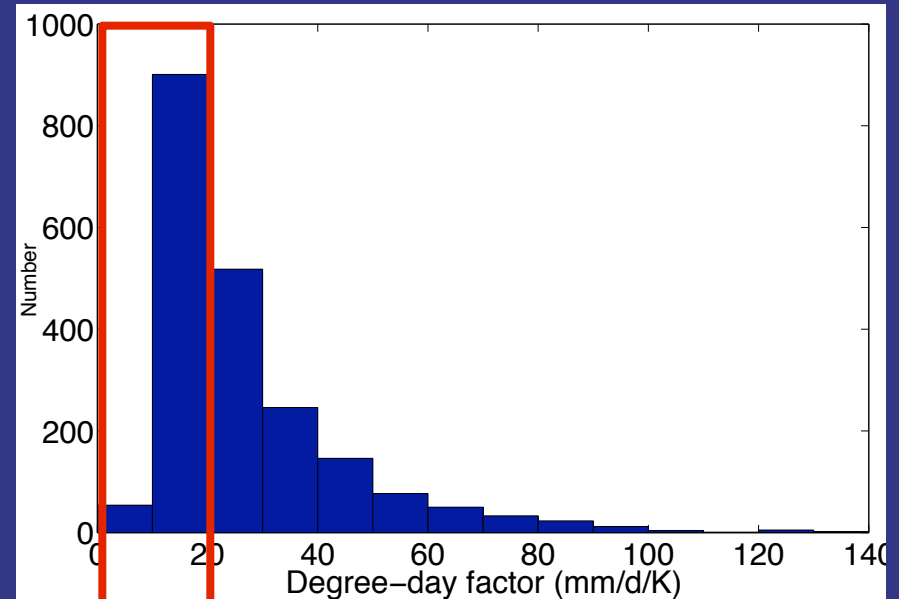
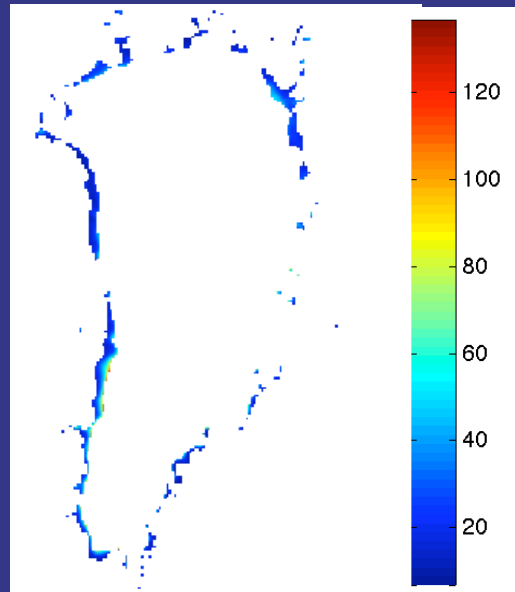
■ Daily and monthly mean temperature and monthly melt for one grid cell



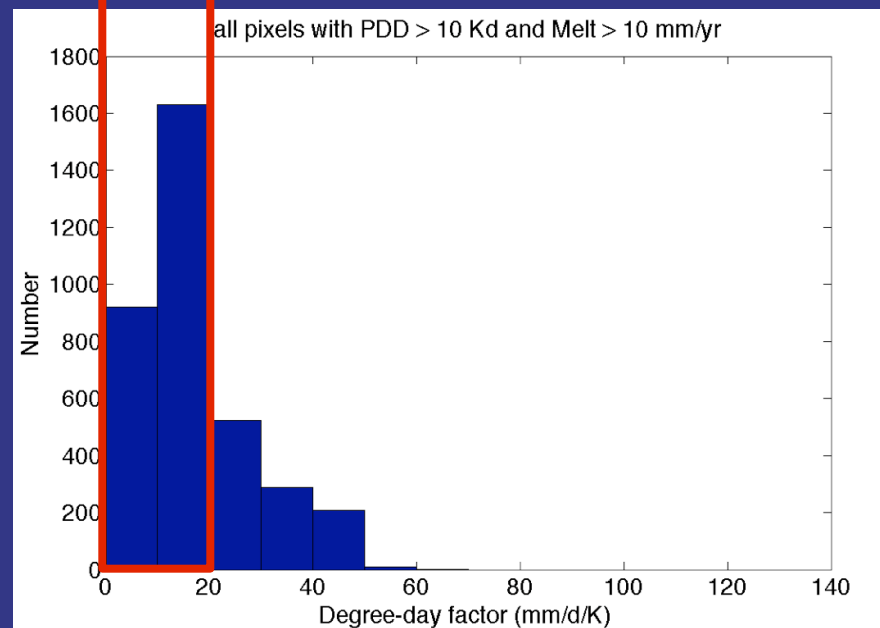
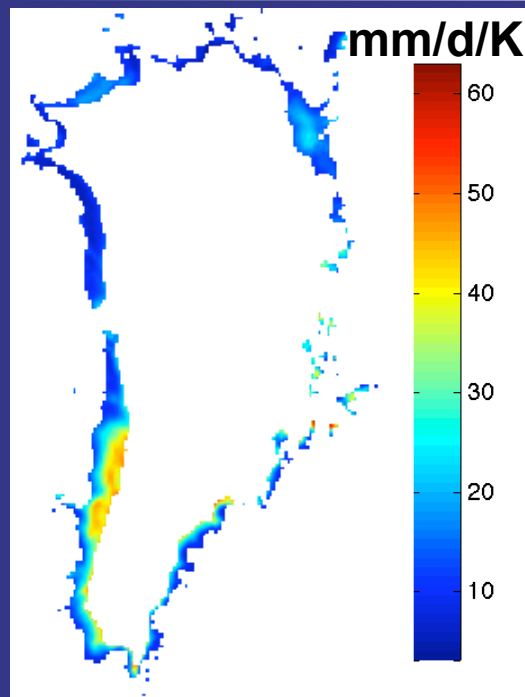
Degree-days factors averaged over 1957-2008

DDF = total melt/PDD over whole period, only for pixels with > 10 mm/yr melt and annual PDD > 10 dK

using
monthly
mean data



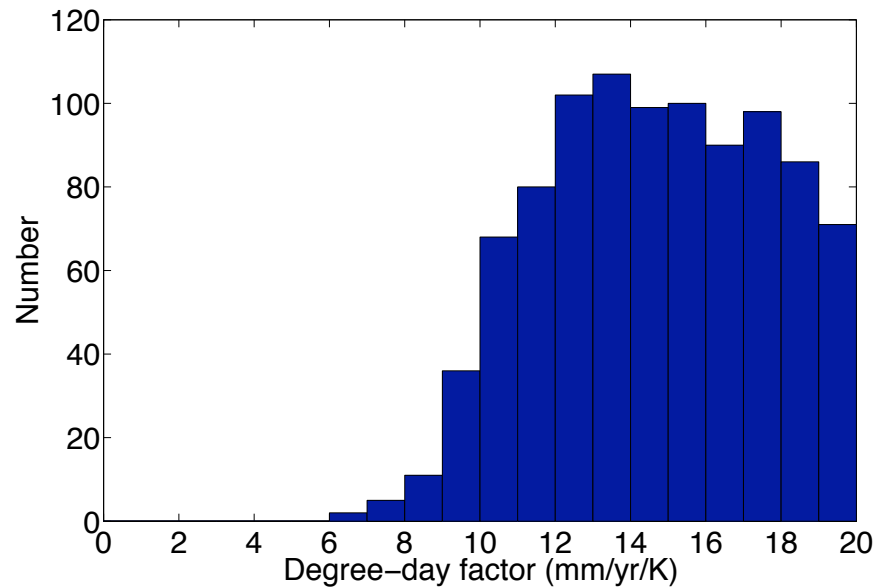
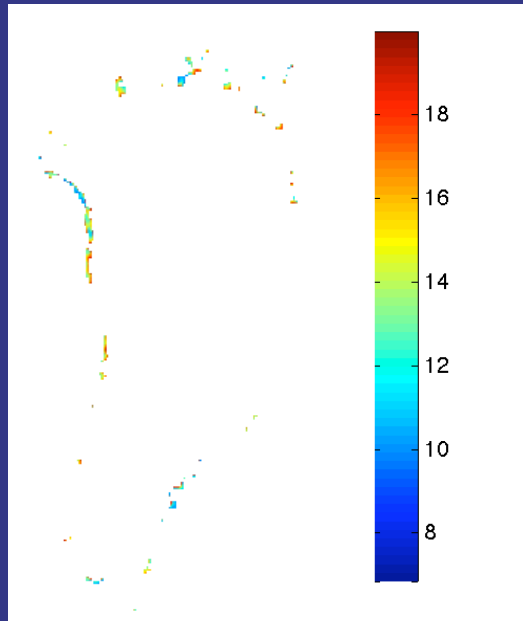
using
daily
mean data



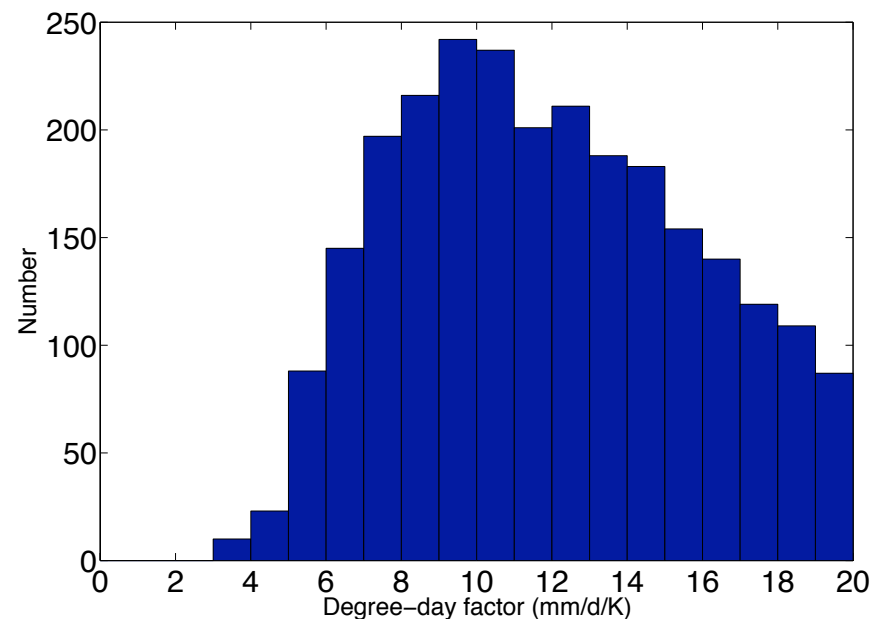
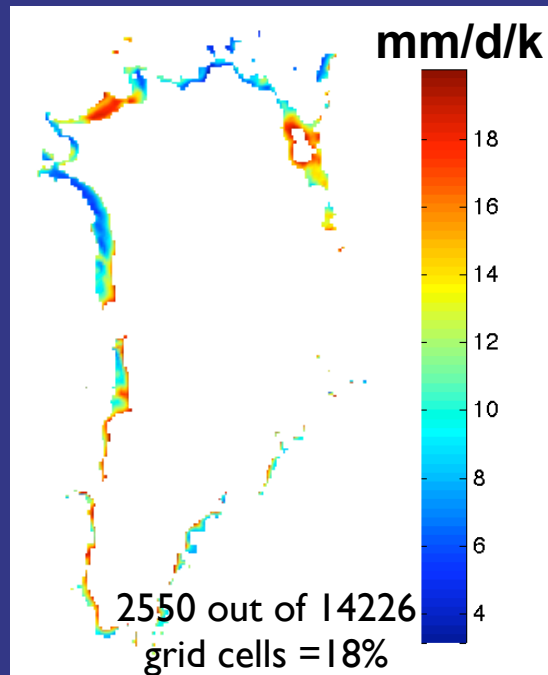
Degree-days factors averaged over 1957-2008

DDF < 20 mm/d/K

using
monthly
mean data



using
daily
mean data

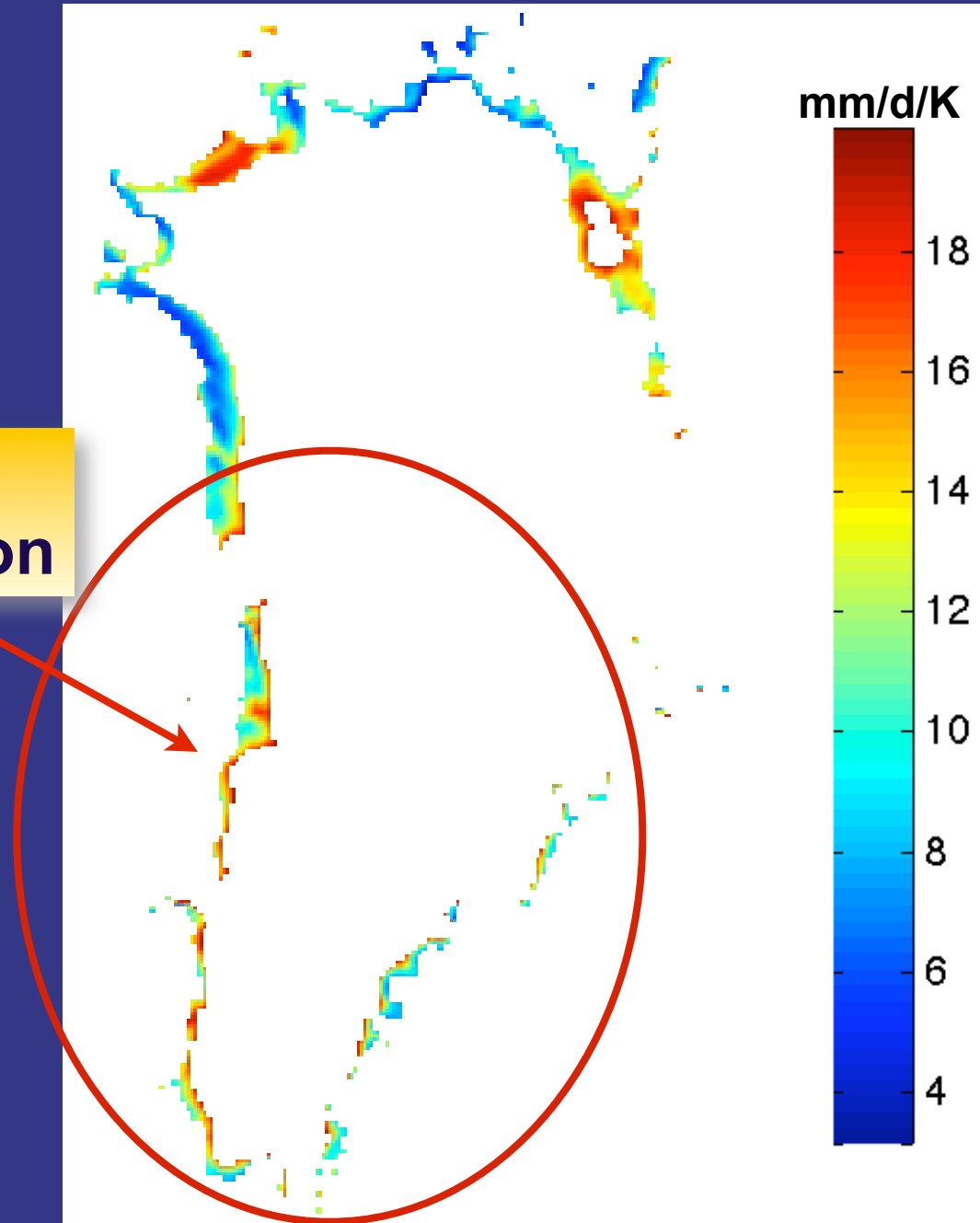


■ Degree-days factors averaged over 1957-2008

DDF for grid cells with > 10 mm/yr melt and annual PDD > 10 dK, and DDF < 20 mm/d/K

using **daily**
mean data

**Degree-day factors
increase with elevation**



■ Lowering the threshold temperature T_0

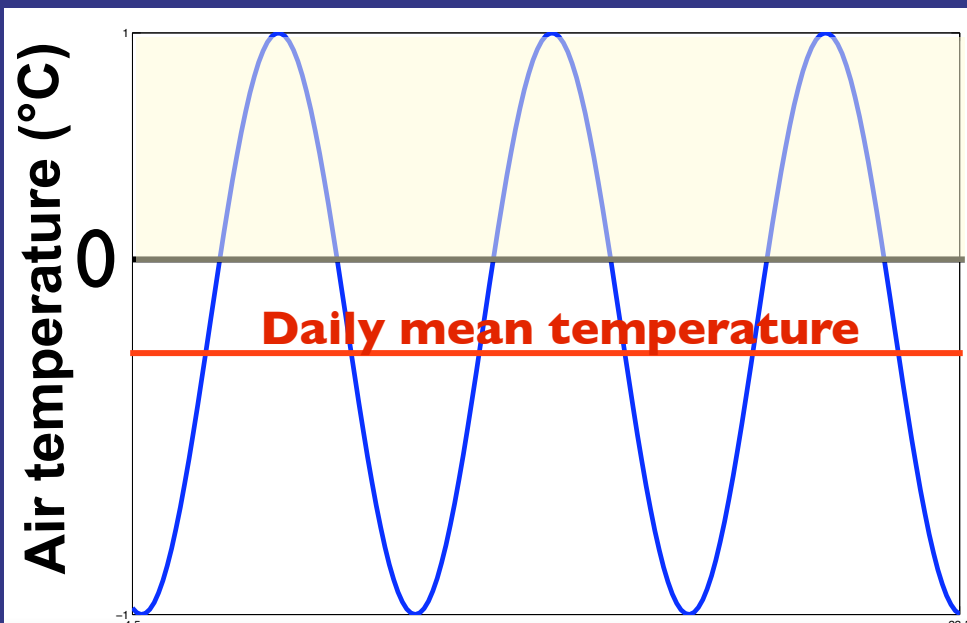
- Van den Broeke et al. (2010, GRL in press) suggest lowering the temperature threshold from 273.15 K to 268 K

$$\dot{M} = f_{\text{snow/ice}} \sum_{1}^n (T - T_0)$$

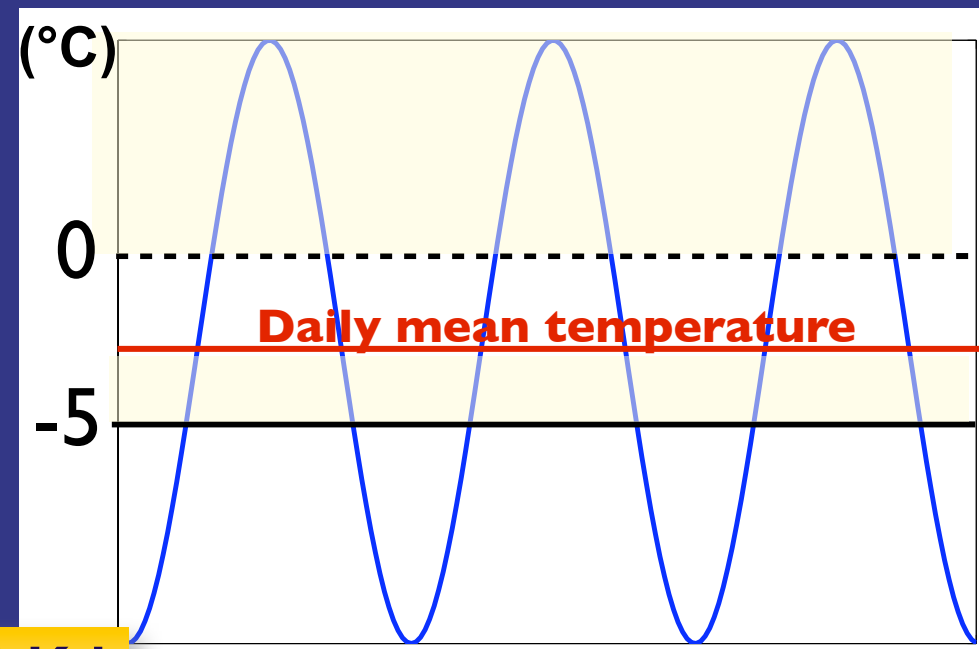
Degree-day factor

Degree-day sum

- --> more realistic pattern of DDF, i.e. high DDF at low elevations and vice versa
- degree-day sums based on daily temperatures underestimate melt because of hourly temperatures above freezing while daily mean temp is below freezing.



Degree-day sum (based on daily mean T) = 0 Kd
Melt is underestimated

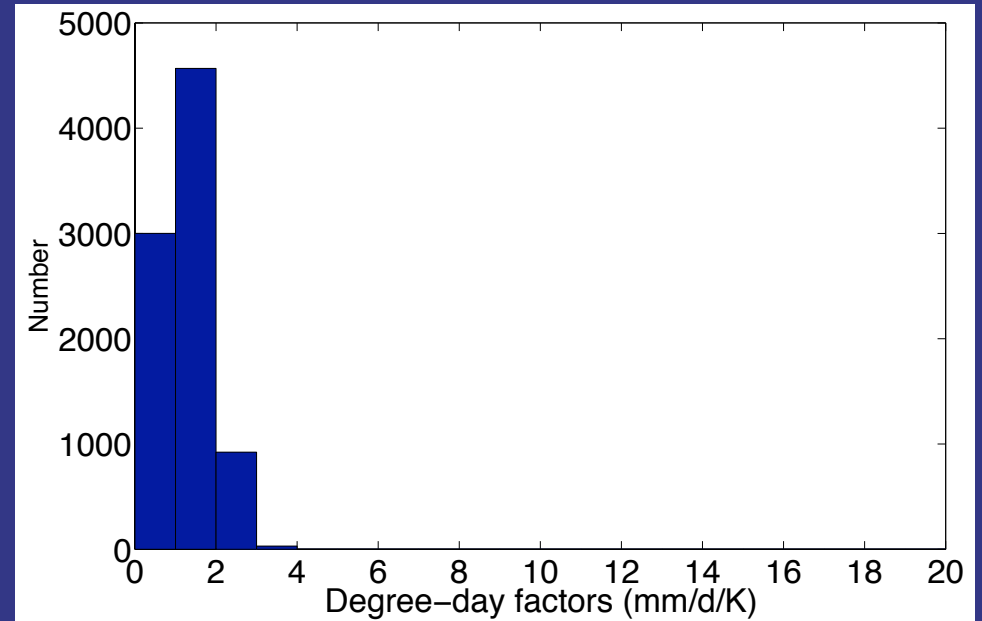
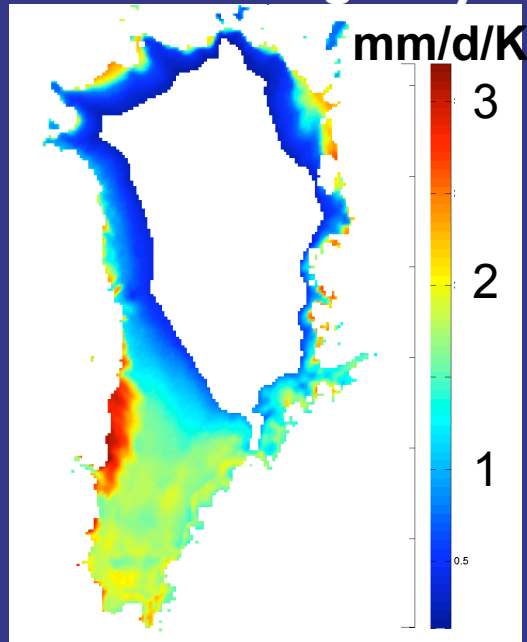


Degree-day sum > 0 Kd

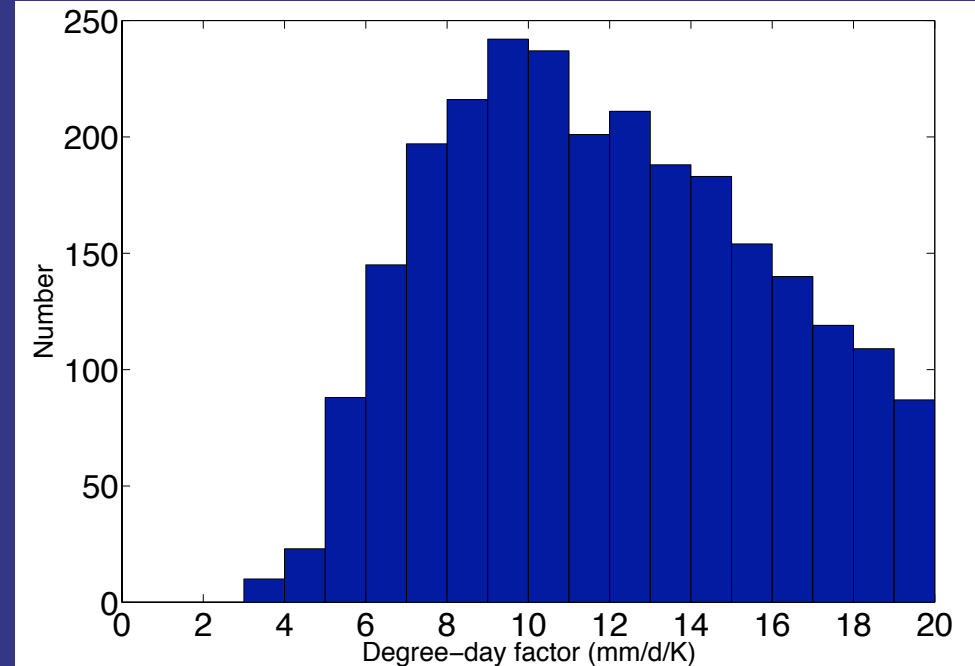
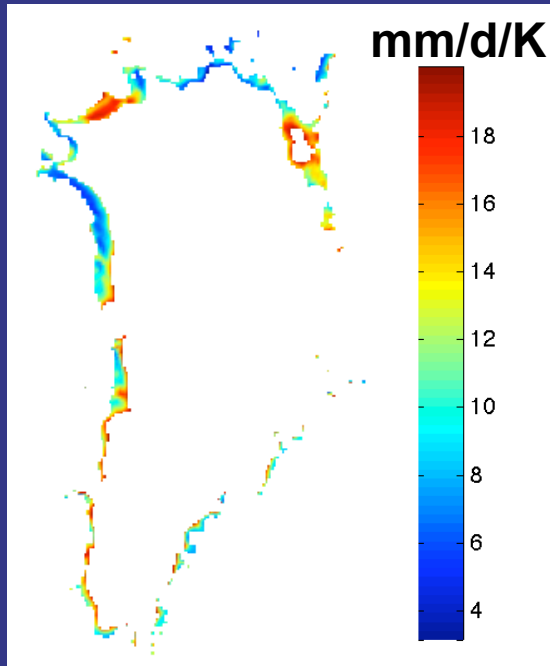
Degree-days factors averaged over 1957-2008 using daily mean temperatures

$$T_0 = 268 \text{ K}$$

*Van den Broeke et al.,
2010. Temperature
thresholds for degree-
day modelling of
Greenland ice sheet
melt rates. GRL in
press*

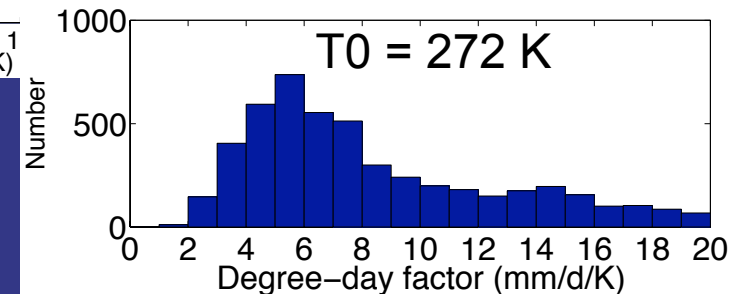
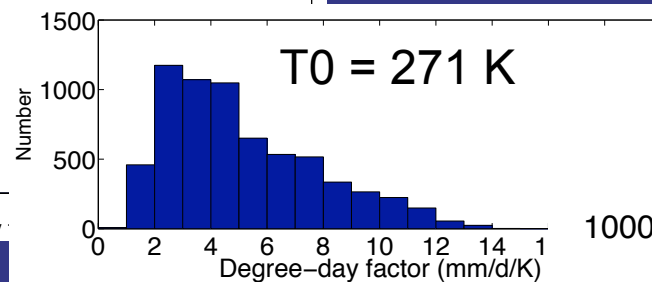
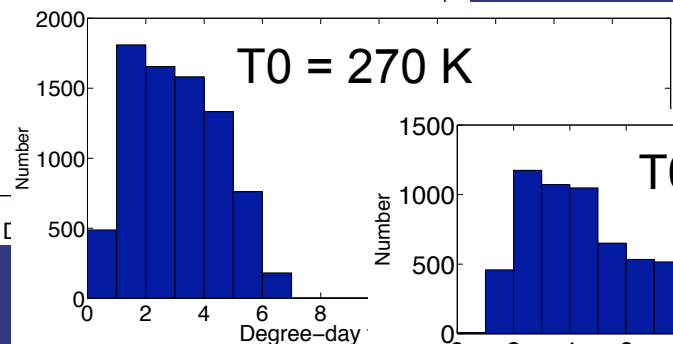
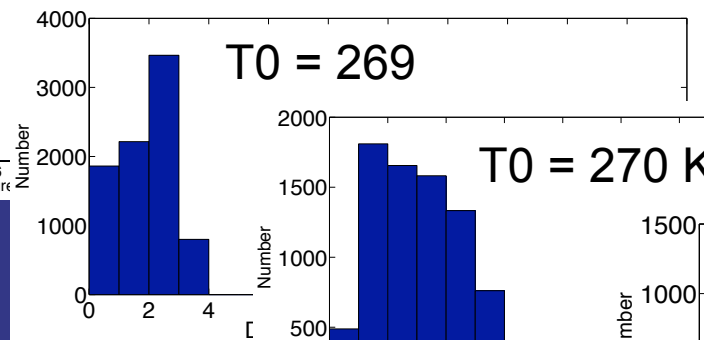
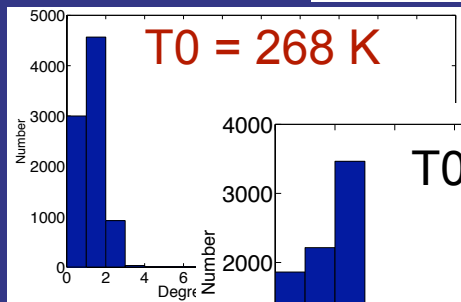
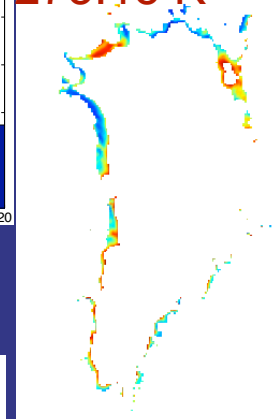
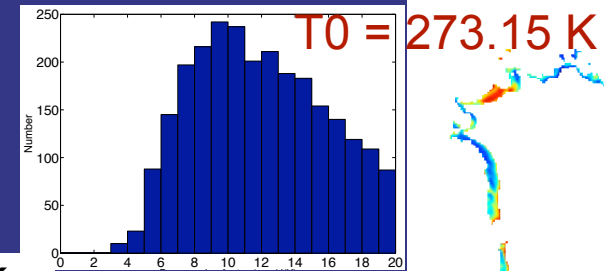
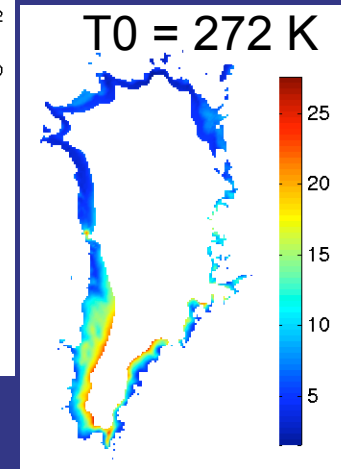
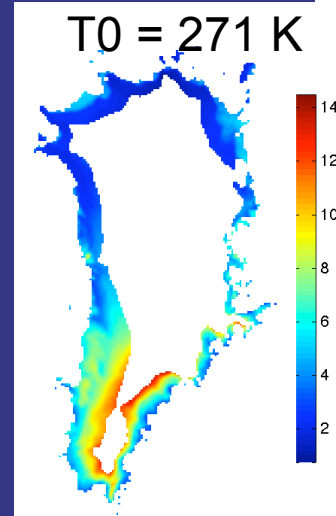
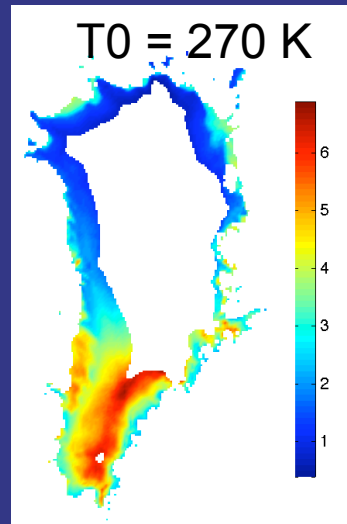
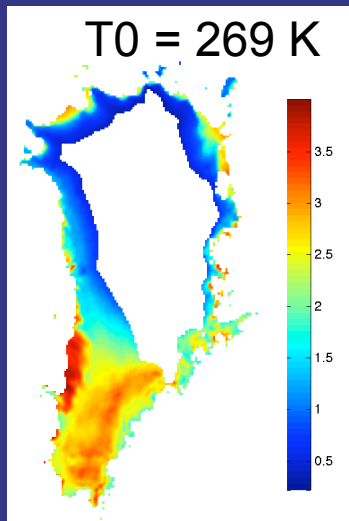
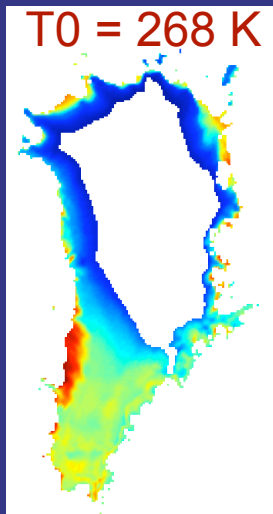


$$T_0 = 273.15 \text{ K}$$

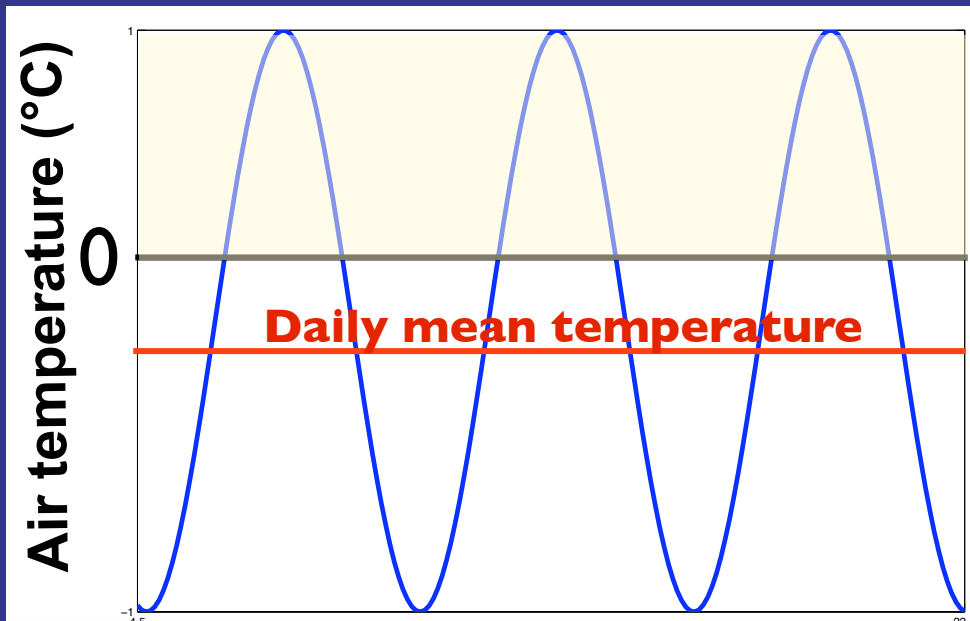


Degree-days factors for various threshold temperatures

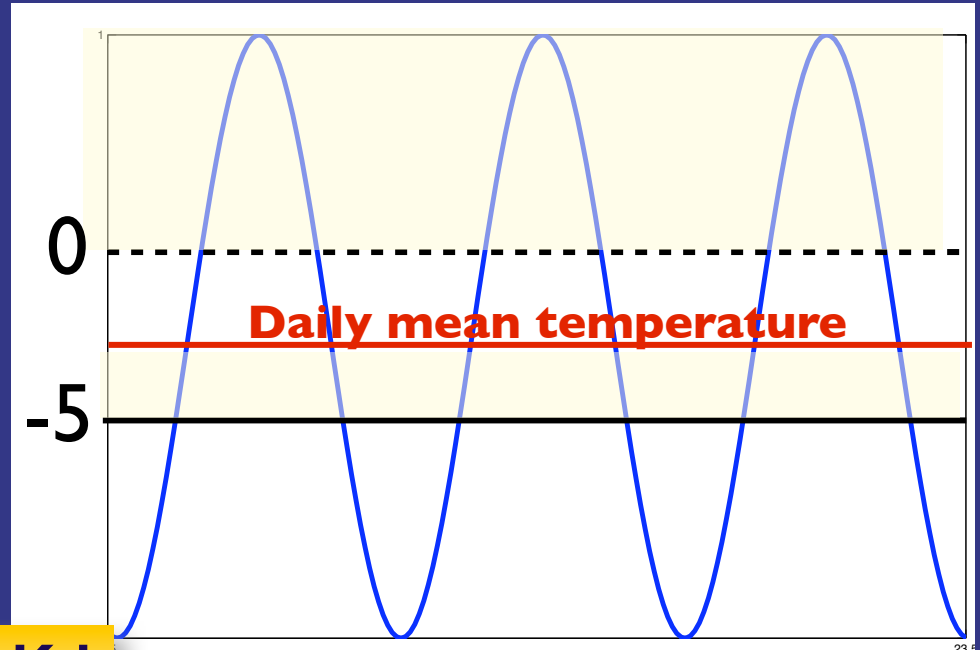
$$\dot{M} = f_{\text{snow/ice}} \sum_{i=1}^n (T - T_0)$$



■ How does the temp threshold affect degree-day factors?

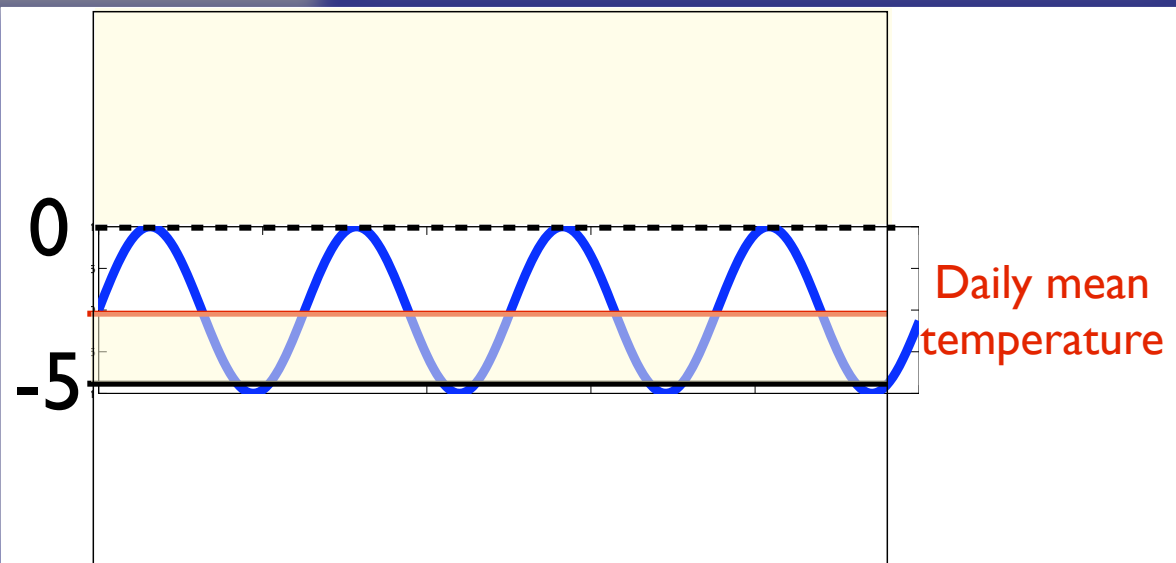


Degree-day sum (based on daily mean T) = 0 Kd
Melt is underestimated



Degree-day sum > 0 Kd

Degree-day sum = positive
but there is no melt
--> Melt is overestimated



■ Purpose

to improve the degree-day model in PISM:

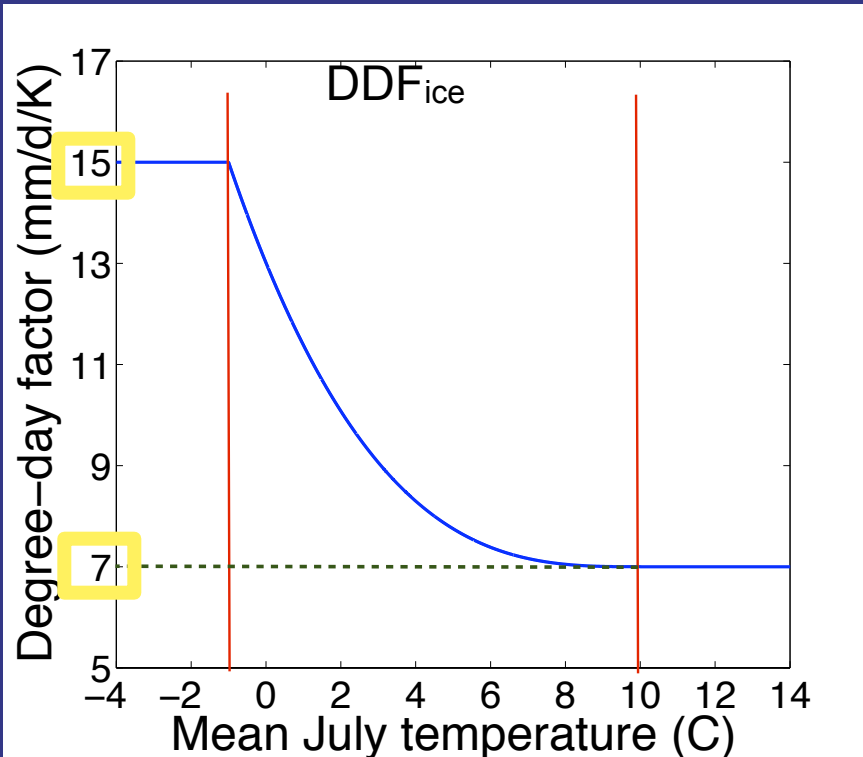
- **How do degree-day factors vary spatially ?**
- How do they vary in time: seasons, trends ?
- What do they depend on ?
- **How good is the degree-day model that is currently implemented in PISM ?**
- How can they be parameterized in a way that can be implemented into PISM ?



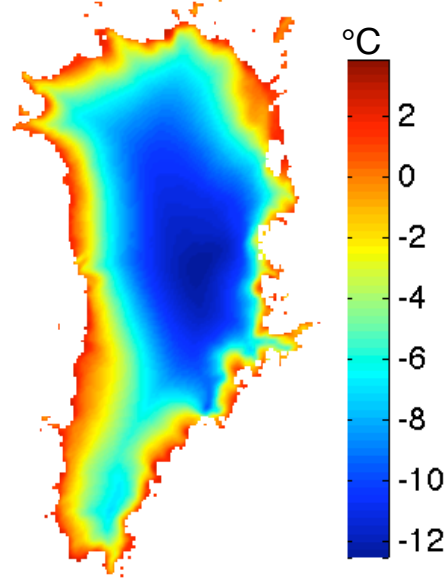
Degree-day factors after Greve (2005)

- $\text{DDF}_{\text{snow}} = 3 \text{ mm/d/K}$ for entire Greenland
- DDF_{ice} :
 - South of 72°N : 7 mm/d/K
 - North of 72°N : function of mean July temperature

$$\beta_{\text{ice}} = \begin{cases} \beta_{\text{ice}}^{\text{w}} & T_{\text{mj}} \geq T_{\text{w}}, \\ \beta_{\text{ice}}^{\text{w}} + \frac{\beta_{\text{ice}}^{\text{c}} - \beta_{\text{ice}}^{\text{w}}}{(T_{\text{w}} - T_{\text{c}})^3} (T_{\text{w}} - T_{\text{mj}})^3 & T_{\text{c}} \leq T_{\text{mj}} \leq T_{\text{w}}, \\ \beta_{\text{ice}}^{\text{c}} & T_{\text{mj}} \leq T_{\text{c}}, \end{cases}$$

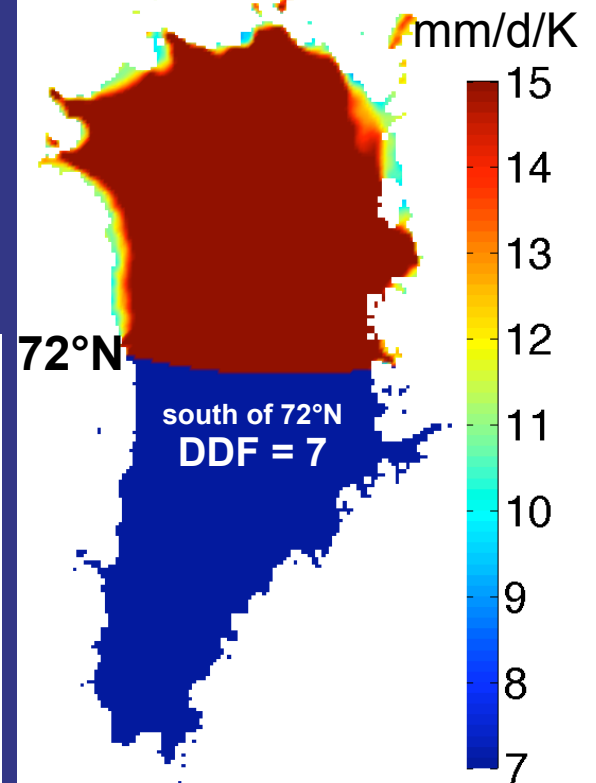


Mean July temperature
1958 - 2008



based on Tarasov and Peltier, 1999

Degree-day factor ice



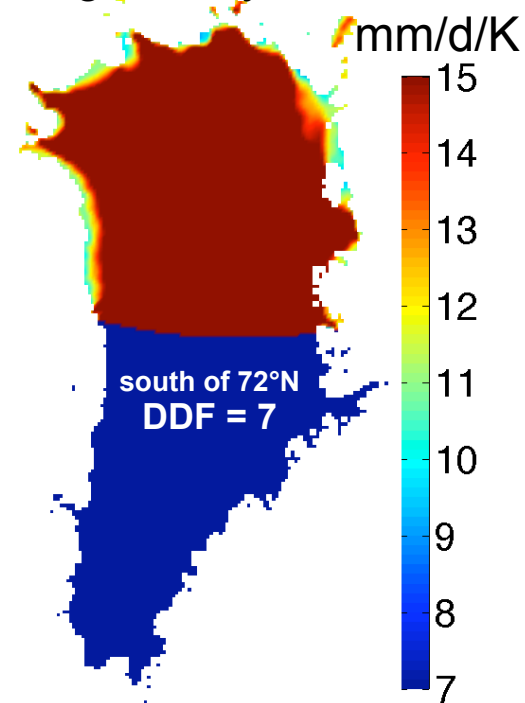
■ PISM: Melt after Greve (2005)

$$\dot{M} = f_{\text{snow/ice}} \sum_{1}^n (T - T_0)$$

Degree-day
factor

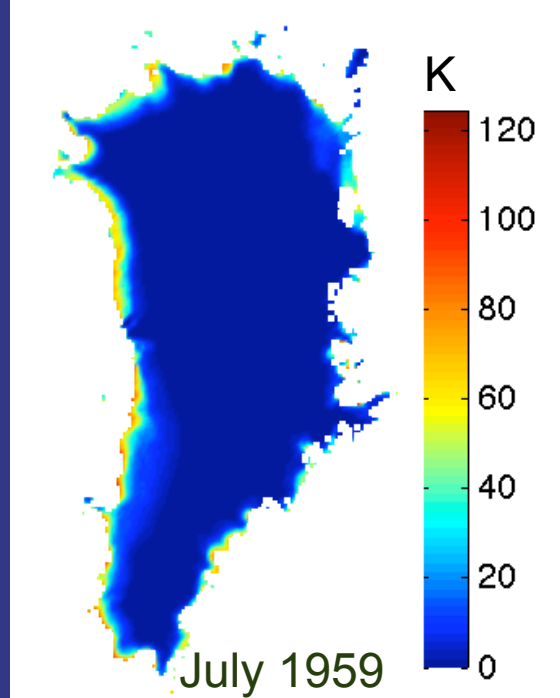
Degree-day sum

Degree-day factor ice

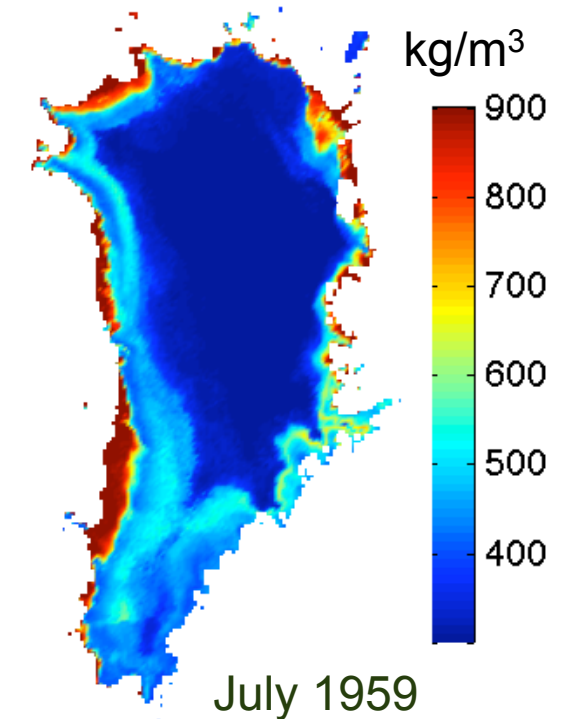


$f_{\text{snow}} = 3 \text{ mm/d/K}$
over entire Greenland

Pos. degree-days



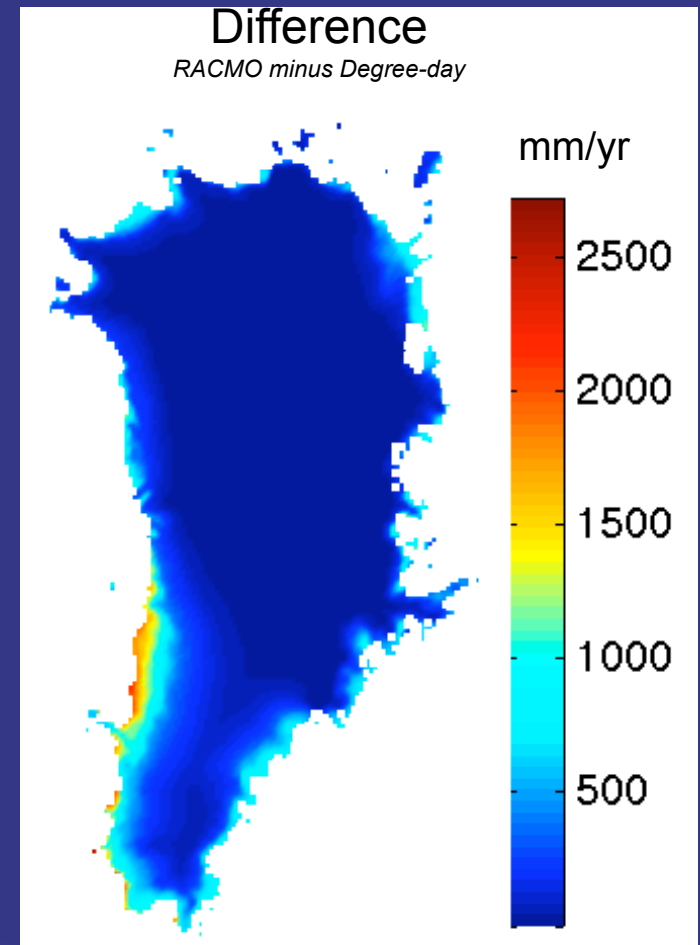
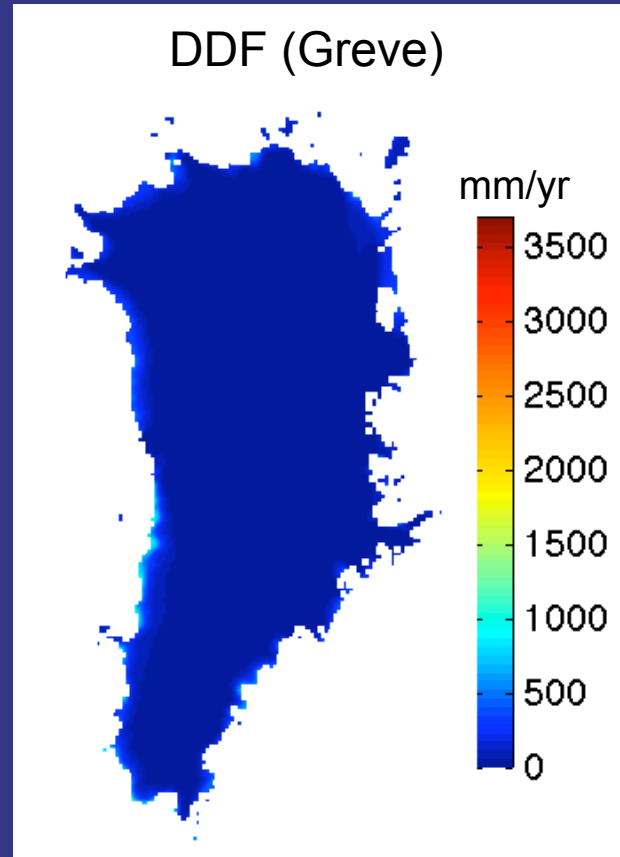
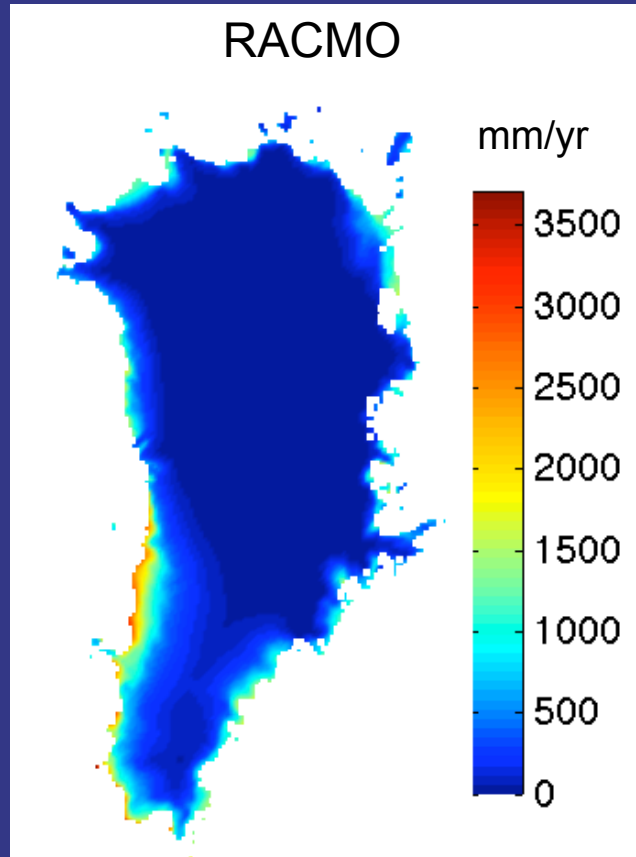
Surface layer density



density fields used to decide
whether surface is ice or snow
<350 kg/m³ = snow: f_{snow} ,
>850 kg/m³ = ice: f_{ice}
linear interpolation in between

■ How does the PDD model (Greve, 2005) compare to RACMO ?

Mean over 1957-2008



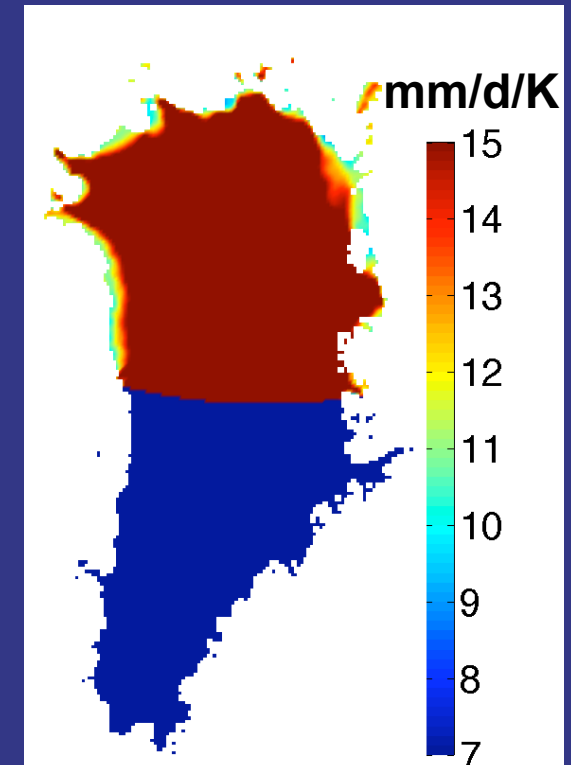
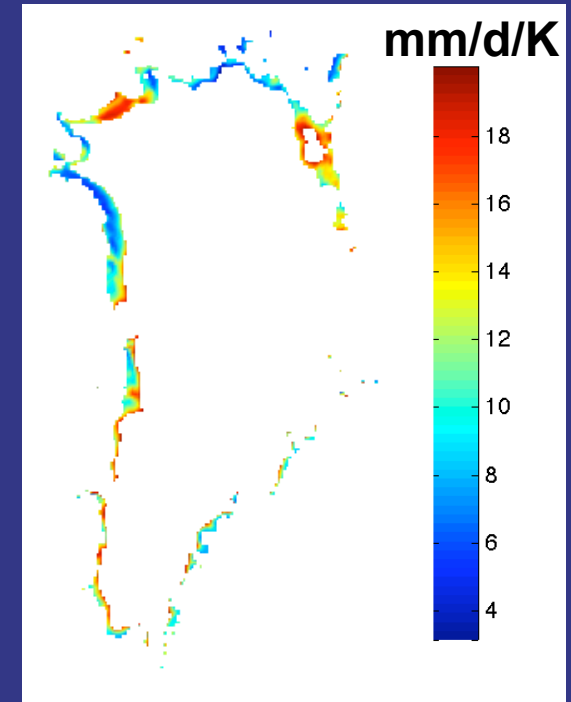
Mean annual melt
243 mm/yr
427 Gt

Mean annual melt
55 mm/yr
93 Gt

Difference
190 mm/yr
333 Gt !!!

■ Conclusions

- Degree-day factors vary strongly in space; no clear geographical pattern
- Factors depend on the way the PDD sum is computed (averaging interval, threshold temperatures)
- Parameterization by Greve (2005) applied to RACMO temperature fields leads to considerable underestimation of melt compared to RACMO (>300 Gt/yr)



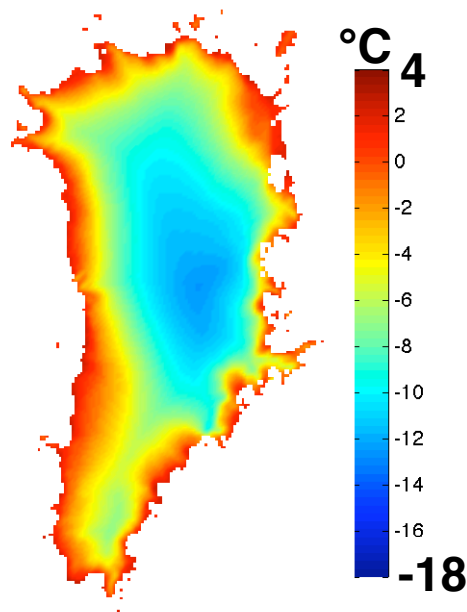
The project is funded by the NASA Modeling, Analysis, and Prediction program (grant # NNX09AJ38G)



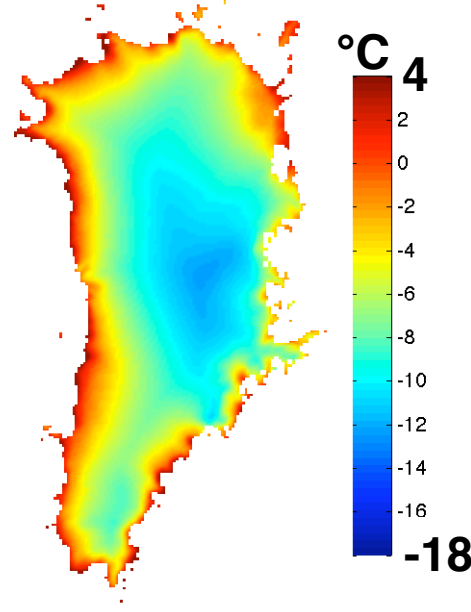
Mean July temperature 1996 - 2006

Comparison RACMO - Fausto-parameterization

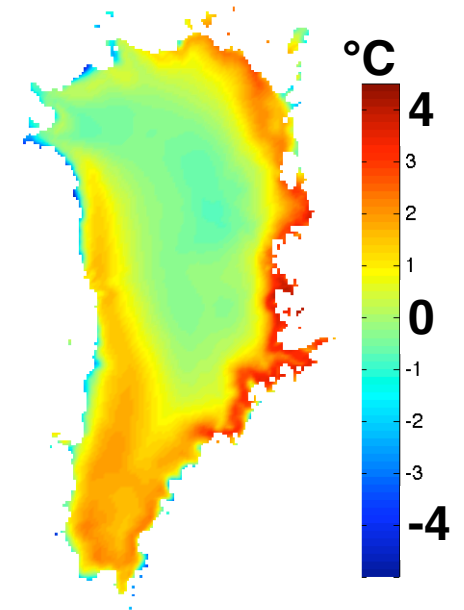
RACMO
(Ettema et al., 2009)



Parameterization
(Fausto et al., 2009)



Difference
RACMO - Parameterization

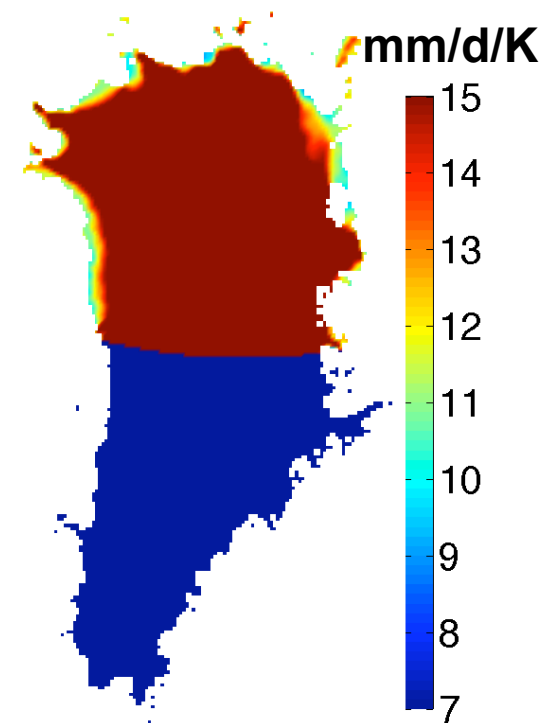
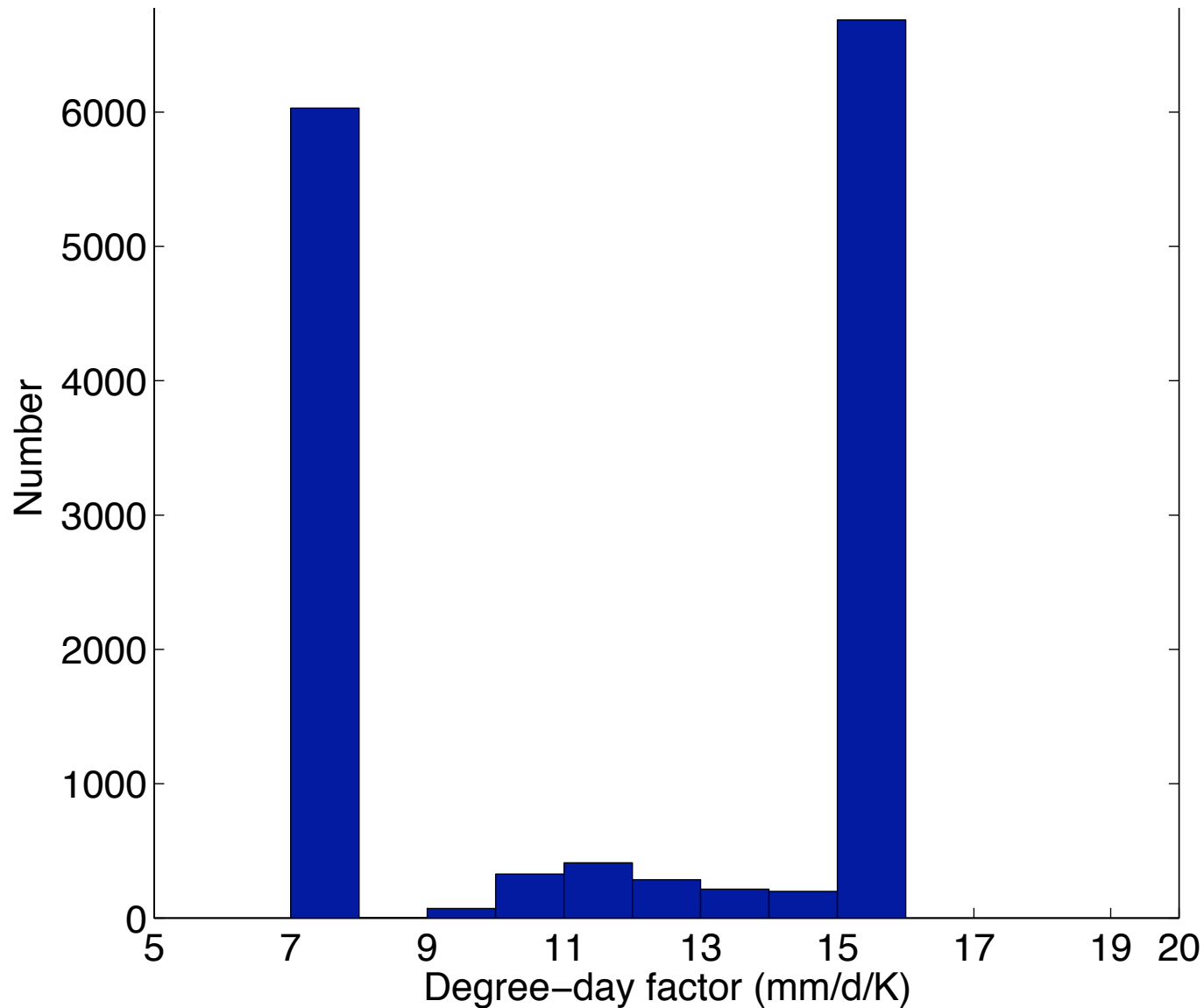


mean = 0.63
max = 4.48
min = -5.00
std.dev = 1.11

Parameterization (Fausto et al., 2009)

$$T_{\text{July}} = d + a z + b \text{ lat} + c \text{ lon}$$

DDF according to Greve (2005) using RACMO positive degree-day sums based on daily data



Degree-days factors for various threshold temperatures

$T_0 = 268 \text{ K}$

$T_0 = 269 \text{ K}$

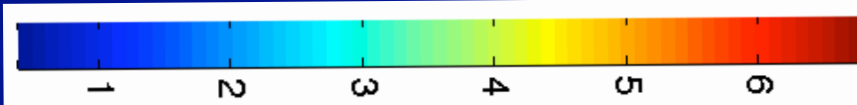
$T_0 = 270 \text{ K}$

$T_0 = 271 \text{ K}$

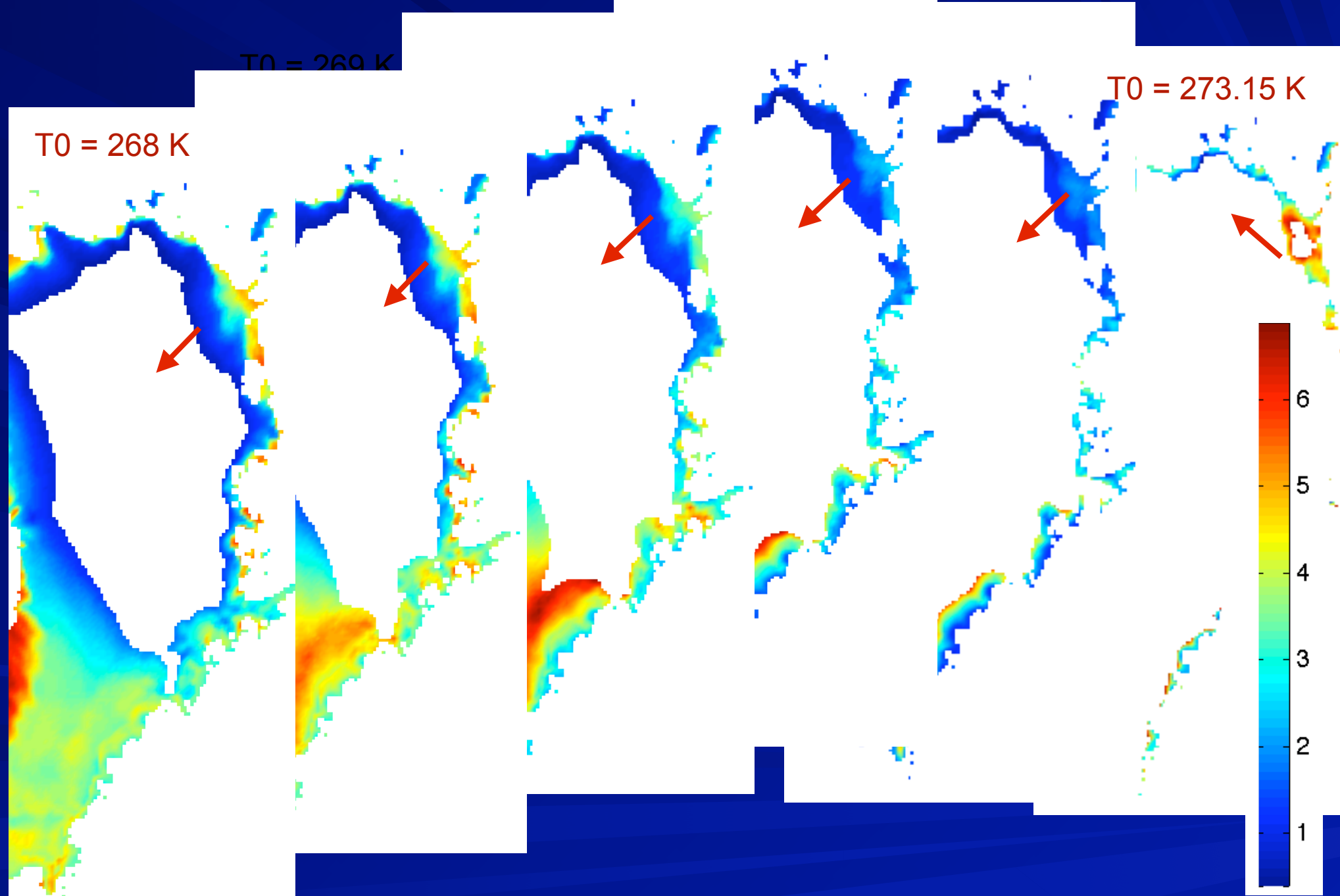
$T_0 = 272 \text{ K}$

$T_0 = 273.15 \text{ K}$

Arrow up means DDF increase with increasing elevation
Arrows down is opposite



■ Degree-days factors for various threshold temperatures



Degree-days factors derived from $T_0=268$ to 270 versus $T_0 = 273.15$ K

