

# Greenland ice sheet flow computations

scaling-up to high spatial resolution and fast boundary processes

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*with help from*

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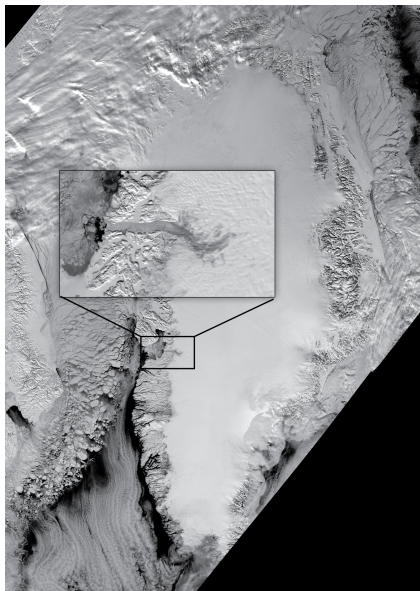
# Outline

**why compute Greenland's flow?**

ice sheets: modeling and observations

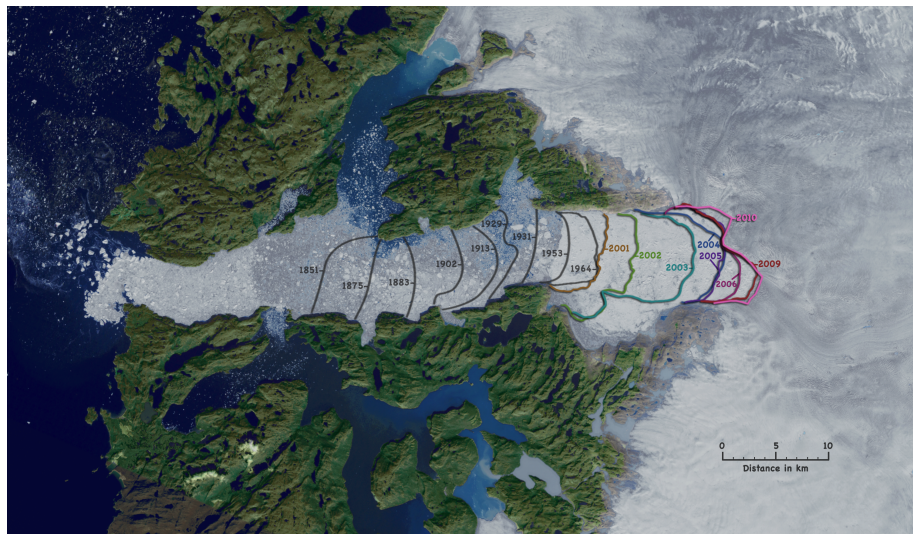
scaling-up: how to get more ISM from HPC

# Jakobshavn Isbræ, west Greenland



*MODIS image  
M. Fahnestock*

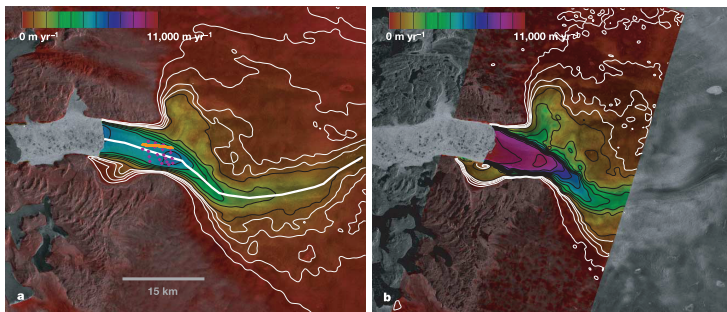
# Jakobshavn Isbræ, west Greenland



*NASA/Goddard Space Flight Center Scientific Visualization Studio*

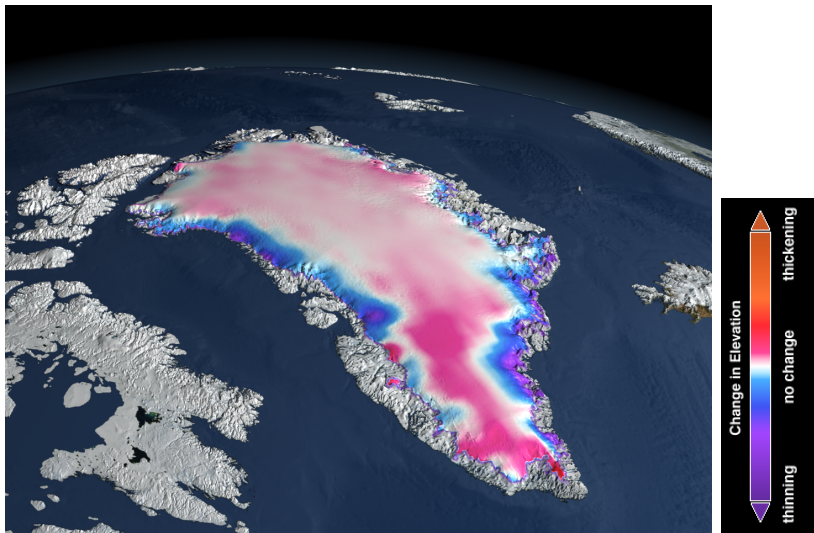
# Speed-up of Jakobshavn Isbræ

- ▶ almost doubled its flow speed between the 1992 and 2000:
  - ▷ probably started by increase in ocean temperature from 1.7 C° in 1995 to 3.3 C° in 1998
  - ▷ ... thus increased melting under floating tongue
  - ▷ loss of floating tongue and its “backpressure” on upstream grounded ice
  - ▷ speed-up of grounded ice
- ▶ now drains about 7% of the entire ice sheet



*Joughin et al. (2004)*

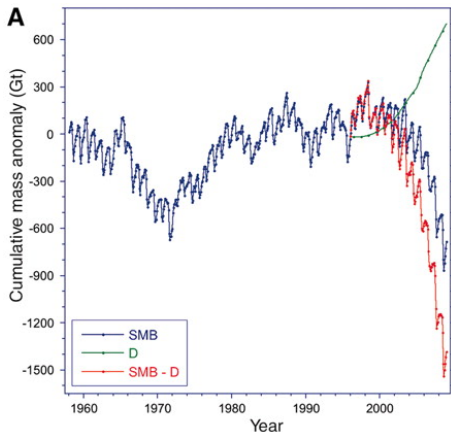
# Elevation changes: surface melt and “discharge”



*IceSAT observations over 2003–2006 period; NASA/Goddard Space Flight Center Scientific Visualization Studio*

# The future of Greenland is the question

- ▶ before mid-90s mass loss was dominated by surface mass balance (= precipitation minus surface melt/runoff)
- ▶ since 2000, mass balance has been persistently negative
  - ▷ decrease in surface mass balance (**more melting beats more precipitation**)
  - ▷ increase in discharge (**calving**) from ice flow
- ▶ future mass loss partitioning: **unknown**
- ▶ models need to predict which climate changes have which effects



*van den Broeke et al. (2009)*

## Why Greenland?

- ▶ its changes affect future sea level rise
  - ▷ 7 m rise if completely melted ... unlikely ... is 1 or 2 m likely?
- ▶ observations over the past decades show:
  - ▷ rapid acceleration of outlet glaciers
  - ▷ thinning around the margin
  - ▷ increased mass loss
- ▶ it's a testbed for ice sheet modeling:
  - ▷ recent observational attention: lots of flights, ground measurements
  - ▷ exhibits the kind of worrying dynamics we want to "explain"
  - ▷ Antarctic ice sheet has  $10\times$  the area thus  $10\times$  the cost

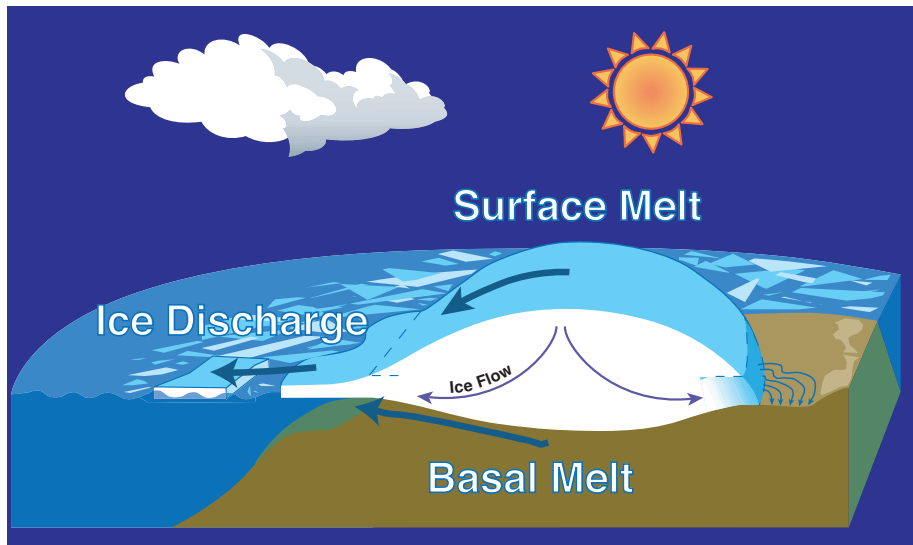
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why compute Greenland's flow?

**ice sheets: modeling and observations**

scaling-up: how to get more ISM from HPC

# How does an ice sheet lose mass?



*modified from ICESat brochure*

# IPCC and ice sheet models

## IPCC (2007), Box 4.1: Ice Sheet Dynamics and Stability

“...but recent changes in ice sheet margins and ice streams cannot be simulated accurately with these models, ...”

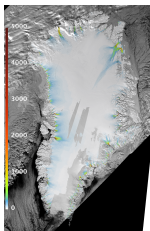
- ▶ IPCC = Intergovernmental Panel on Climate Change  
= {2007 Nobel Peace Prize winners} \ {Al Gore}
- ▶ above statement  $\implies$  lots of attention from modelers

## progress report 2011:

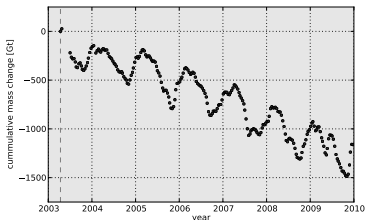
- ▶ PISM is doing a decent job reproducing the past two decades
  - ▷ before anything else, get the present, observed period right!
  - ▷ [model validation](#)

# Ice sheet model validation using

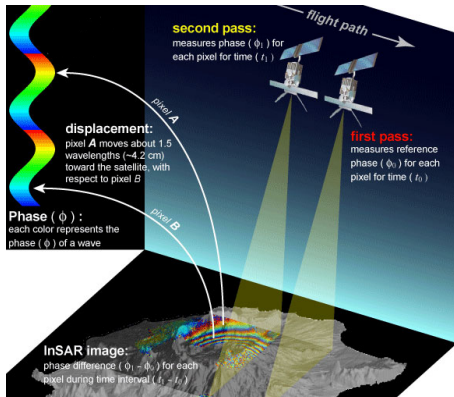
- ▶ observed mean flow speed from 2000, 2006–2008 (InSAR)



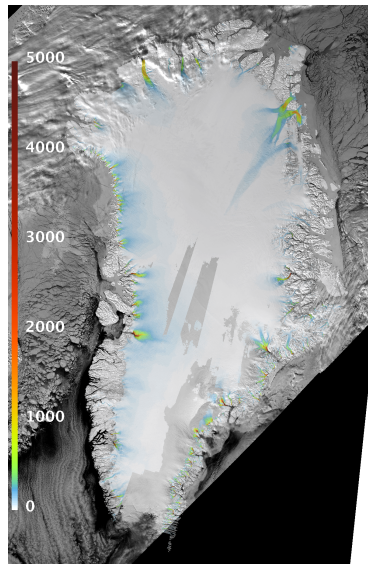
- ▶ observed cumulative mass change from 2003–2009 (GRACE)



# Flow speed from InSAR

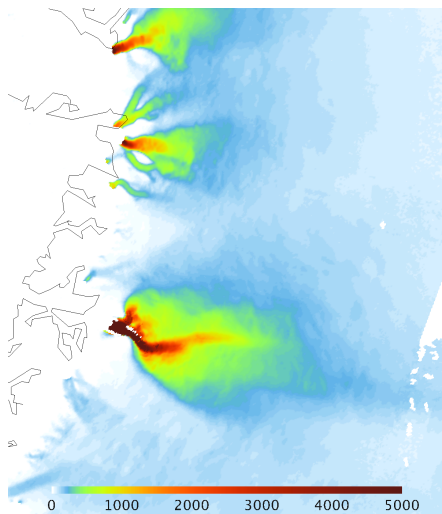


*credit: USGS*

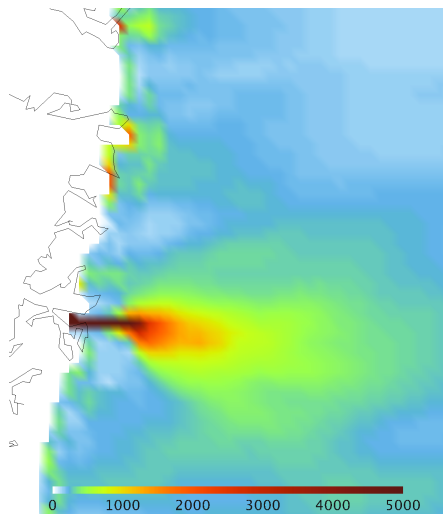


*credit: I. Joughin*

# Results: Jakobshavn Isbræ

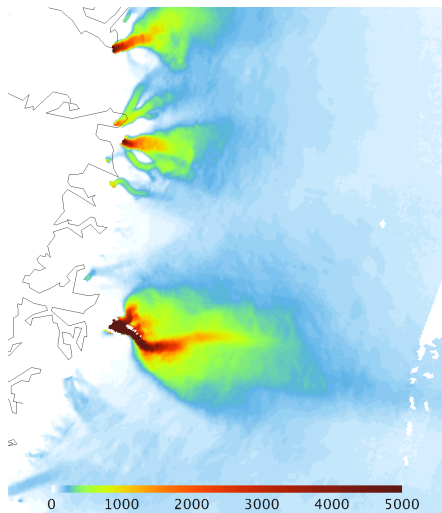


InSAR (*Joughin et al., 2010*)

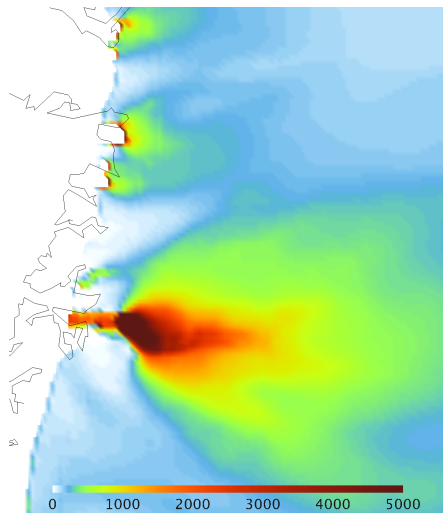


PISM: 5 km grid resolution

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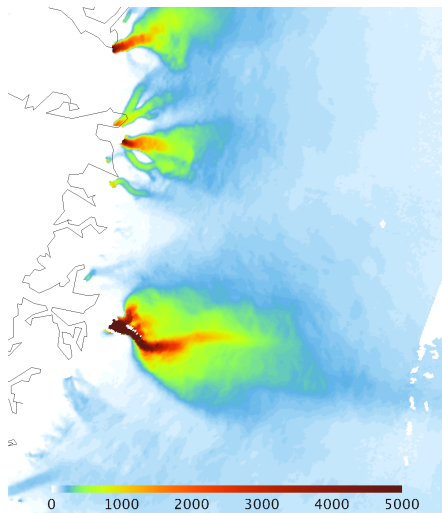


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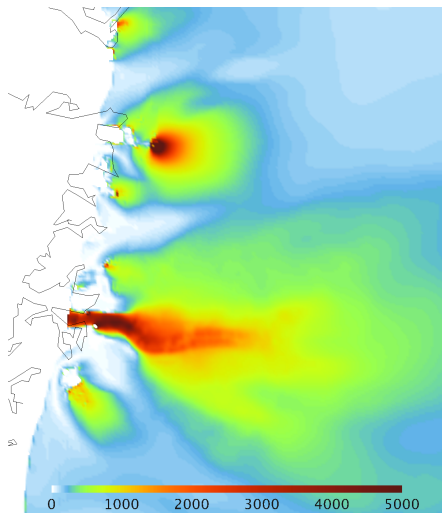


PISM: 2 km grid resolution

# Results: Jakobshavn Isbræ

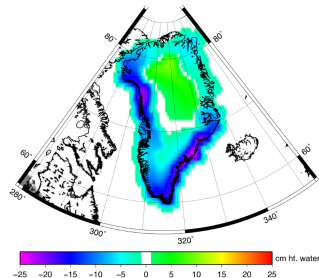
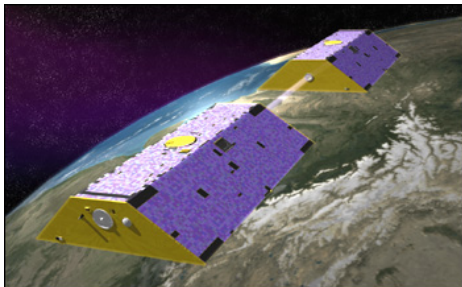


InSAR (*Joughin et al., 2010*)



PISM: 1 km grid resolution

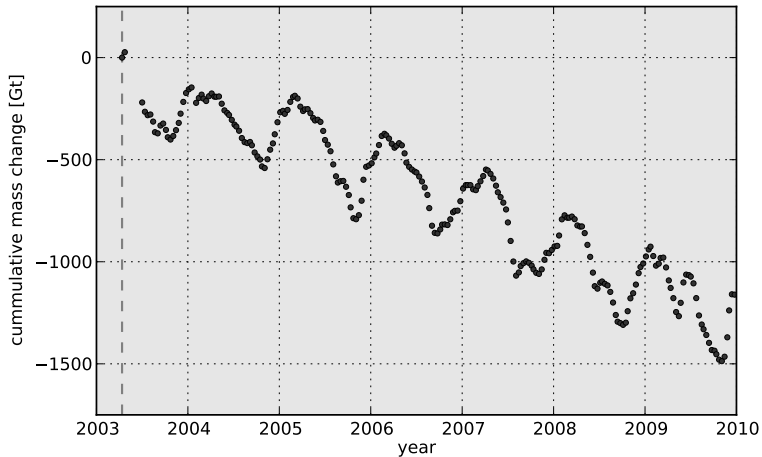
# Gravity Recovery and Climate Experiment (GRACE)



*thanks to A. Arendt*

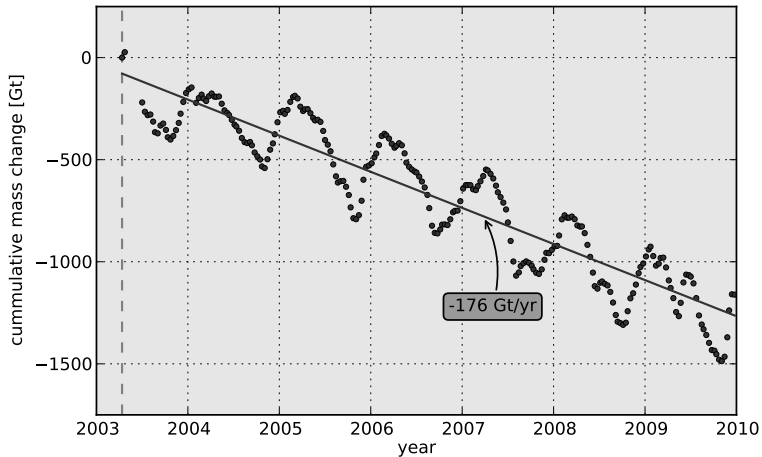
- ▶ precisely measures distance between pair of satellites
- ▶ estimates deviation of gravity field from uniform sphere shape

# Observed mass changes



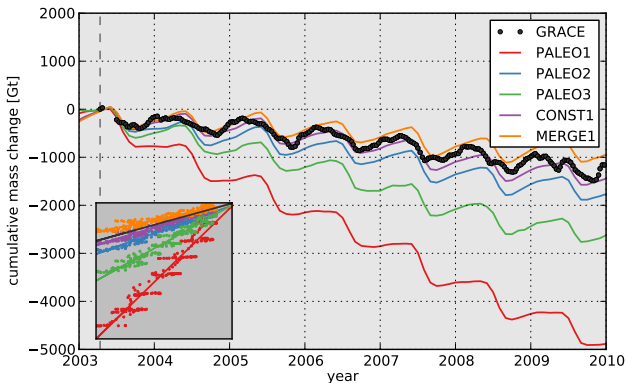
Luthcke, et al. (unpublished; new high-resolution solutions)

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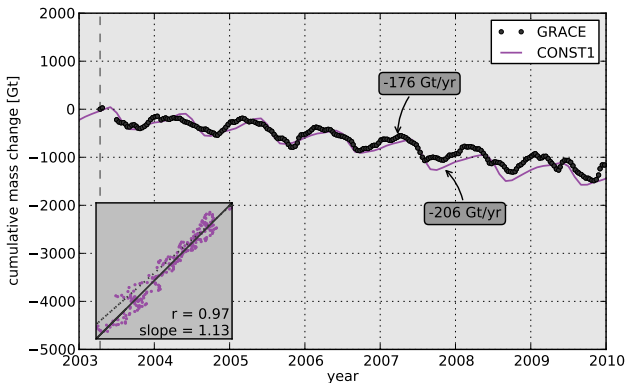
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# Modeled and observed mass changes



- ▶ new coupled models of Greenland
  - ▷ PISM + regional climate model (HIRHAM at DMI Copenhagen)

# Modeled and observed mass changes

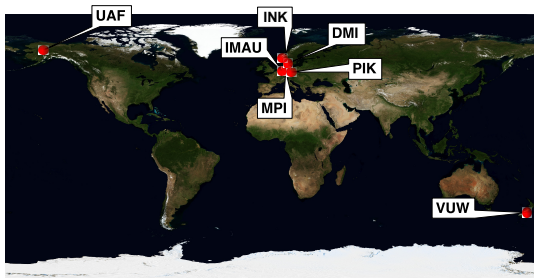


- new coupled models of Greenland
  - ▷ PISM + regional climate model (HIRHAM at DMI Copenhagen)

# What is PISM?

- ▶ PISM = Parallel Ice Sheet Model [www.pism-docs.org](http://www.pism-docs.org)
- ▶ open source (C++, python), PETSc-over-MPI, regular grid
- ▶ adaptive time-stepping
- ▶ supported by NASA; now a joint project with PIK in Germany
- ▶ the best ice sheet model in the world
- ▶ ... was developed in Fairbanks

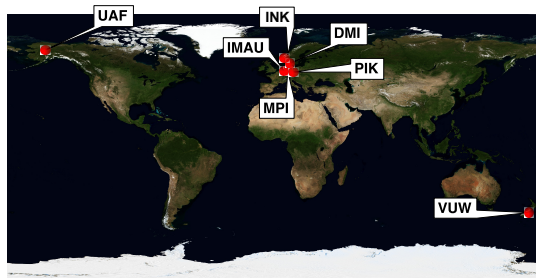
user base:



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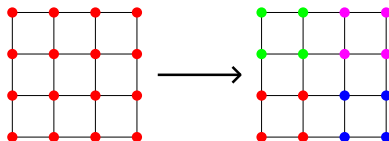
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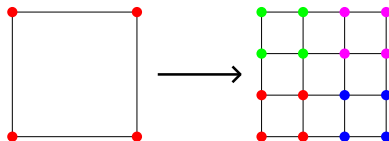
**scaling-up: how to get more ISM from HPC**

# Scaling

- ▶ plan for the rest of my talk: beat up PISM because it scales badly
- ▶ ... though it scales way better than any other current ISM
- ▶ definitions in convenient 2D grid case:
  - ▷ **strong scaling**: for fixed problem,  
 $4\times$  the number of processors  $\Rightarrow$  (1/4)th the execution time



- ▷ **weak scaling**: for fixed number of d.o.f.s *per processor*,  
 $4\times$  the number of processors  $\Rightarrow$  *same* execution time



# Min prerequisite for weak scaling: convergence

- ▶ six runs, each 100 model year with same data
- ▶ on refining grids: 40, 20, 10, 5, 2.5 km
- ▶ surface velocity (m/year) →
- ▶ my first informal study

- ▶ results:

res	procs	wall clock
40 km	1	8 sec
20 km	1	75 sec
10 km	64	57 sec
5 km	64	14 min
3 km	128	56 min
2 km	128	285 min

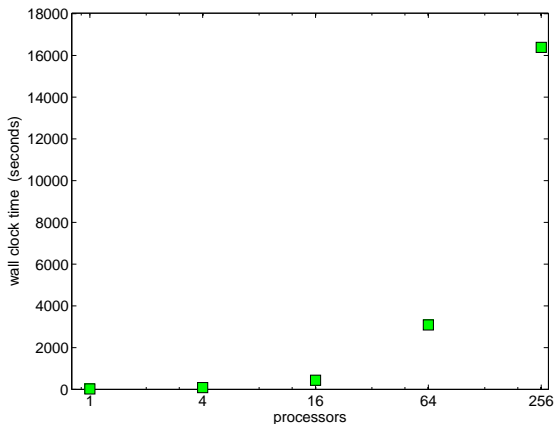
- ▶ on Cray XT5
  - ▷ `pingo.arsc.edu`

# Weak scaling: the reality

- ▶ here's the problem →

- ▷ 100 model year runs
- ▷ increase d.o.f.s and processors in proportion
  - ▶ a la weak scaling
- ▷ it is **not** giving constant-time for whole run
- ▷ it is giving constant-time per model time step
  - ▶ but who cares

- ▶ we observe: short time steps on fine grids blocks weak scaling

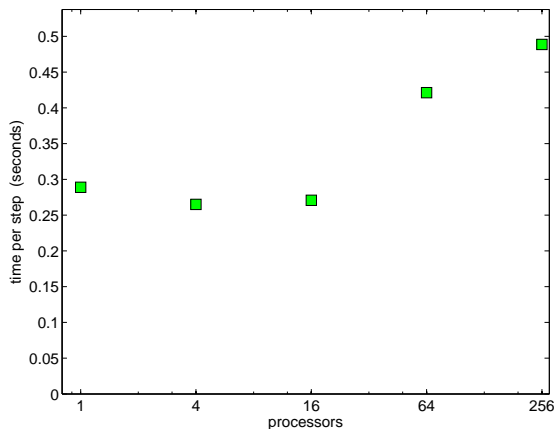


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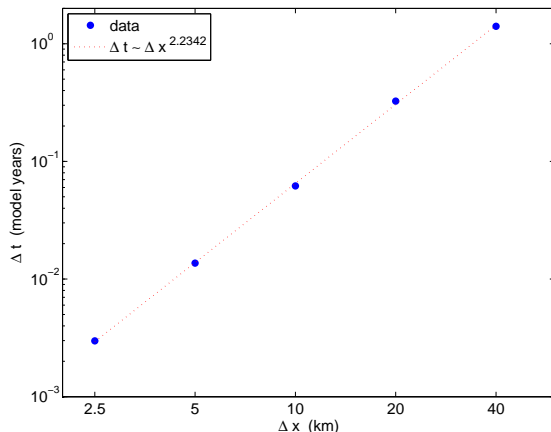


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# Weak scaling: the troubles

## 1 PISM evolves temperature and geometry by **explicit** time-stepping

- ▷ major evolution equation is wildly-nonlinear diffusion
- ▷ ice thickness  $H$  changes by

$$\frac{\partial H}{\partial t} \doteq \nabla \cdot (CH^5 |\nabla H|^2 \nabla H)$$

- ▷ explicit method scales badly because

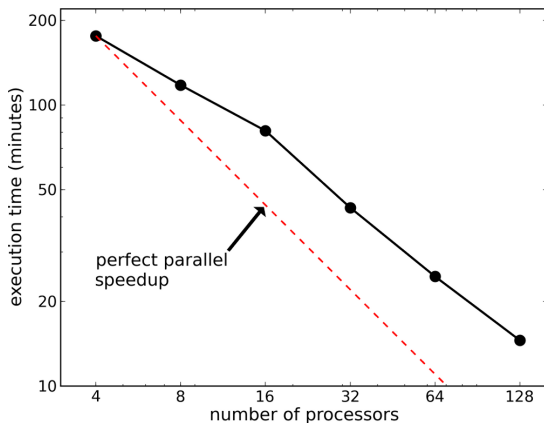
$$\Delta t \sim \Delta x^2$$

- ▷ *implicit time steps, you idiot!*
- ▷ but we are not solving PDEs; boundary value problem is \* subject to inequality

$$H \geq 0$$

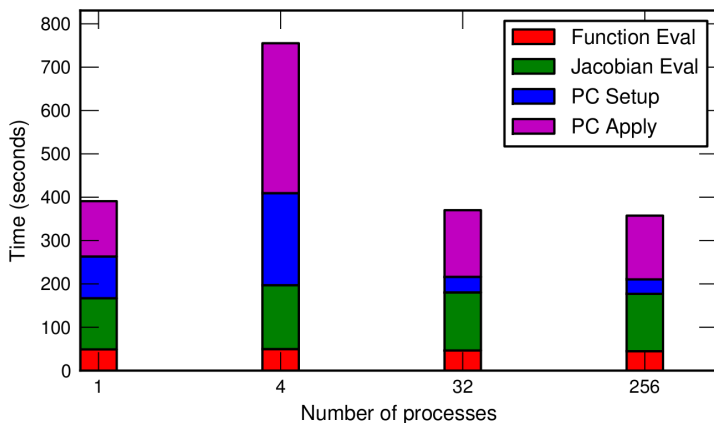
- ▷ so we don't really know how to solve well-posed implicit time steps

## Scaling: results so far; idealized ice sheets



- ▶ PISM: strong scaling on time-dependent run including many 2D stress solutions
- ▶ Jed Brown's hydrostatic ice solver [*submitted 2011*]: awesome weak scaling on time-independent 3D stress solver; *not yet in PISM!*

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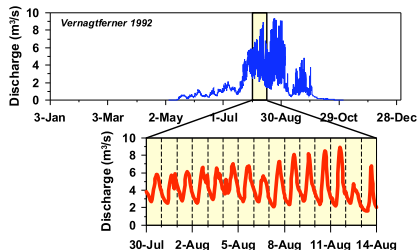
# Weak scaling: the troubles

## 2 liquid water at boundaries

- ▷ big lakes form and drain ... in 90 minutes (upper)
- ▷ hydrograph shows brief summer period of surface melt (lower)
- ▷ ice flow model must “see” liquid runoff at surface *and* its effect on subglacial resistance
  - ▶ boundary liquid timescales are minutes–weeks
  - ▶ ice sheet model runs are decades–millenia



*S. Das*

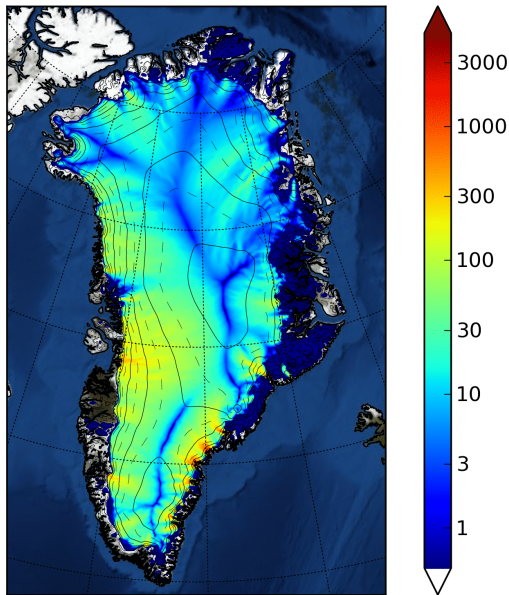


*R. Hock et al. (2005)*

# Weak scaling: the troubles

## 3 solve PDEs on domain with fractal boundary

- ▷ velocity is big near the boundary
- ▷ boundary is a [coastline](#) ... Mandelbrot warned us about those things
- ▷ at each timestep, want to solve nonlinear elliptic problems on this fractal



## Summary

- ▶ model Greenland ice sheet flow! it is on the move!
- ▶ PISM is getting good fit to observed flow speeds, mass changes
- ▶ challenges to scaling:
  - ▷ equations need new thinking
    - need well-posed implicit time steps
    - and better solvers too
  - ▷ short time-scale processes on all ice sheet surfaces
    - liquid water
  - ▷ fast ice dynamics along fractal boundaries
- ▶ much bigger Antarctic ice sheet in the background
- ▶ thanks for your attention!